A Verified Protocol Buffer Compiler

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Abstract

The code responsible for serializing and deserializing untrusted external data is a vital component of any software that communicates with the outside world, as any bugs in these components can compromise the entire system. This is particularly true for verified systems which rely on trusted code to process external data, as any defects in the parsing code can invalidate any formal proofs about the system. One way to reduce the trusted code base of these systems is to use interface generators like Protocol Buffer and ASN.1 to generate serializers and deserializers from data descriptors. Of course, these generators are not immune to bugs.

In this work, we formally verify a compiler for a realistic subset of the popular Protocol Buffer serialization format using the Coq proof assistant, proving once and for all the correctness of every generated serializer and deserializer. One of the challenges we had to overcome was the extreme flexibility of the Protocol Buffer format: the same source data can be encoded in an infinite number of ways, and the deserializer must faithfully recover the original source value from each. We have validated our verified system using the official conformance tests.

CCS Concepts · Theory of computation → Program verification; · Software and its engineering → Software verification; Source code generation;

Keywords · Serialization, Program verification, Coq

ACM Reference Format:

1 Introduction

Serialization is the process of encoding structured data into a binary representation according to a standardized format, usually in order to communicate with some external client or for persistent storage. In the case of distributed systems, serialized data is used to exchange messages, perform remote procedure calls, and orchestrate synchronization. Failure to produce or correctly interpret encoded data can result in lost or corrupted data, potentially placing the system into an inconsistent state. Given their importance, serializers and deserializers are particularly ripe targets for formal verification.

This is especially true when serialization and deserialization code is included in the trusted code of a formally verified system, as bugs in those components can compromise the assurance case for the entire system [13].

There are no shortage of standardized serialization formats in the wild, including protocol-specific formats like TCP/IP and DNS [21, 23, 24], language-specific marshaling libraries [14, 20], human readable formats like JSON [6] and XML [7], and interface generators like ASN.1 [12] and Protocol Buffers [30]. Interface generators are particularly popular for application developers [16], because they offer a general-purpose, language-independent solution to serialization, while producing a more compact encoding than human readable formats. These systems provide a domain-specific language in which users can describe their application’s data types, as well as a compiler for building a library of data type definitions, methods to manipulate those data types, and serializer and deserializers in a desired target language. Delegating the generation of this library to a compiler removes the possibility of user-introduced bugs in serialization and deserialization code, but these compilers may themselves have bugs. Numerous security vulnerabilities have been reported for various ASN.1 compilers in MITRE’s Common Vulnerability Enumeration (CVE) [1–3]. Thus, removing the generated serializers and deserializers from the trusted code base is an important piece of building high-assurance systems that rely on interface generators.

In this paper, we do just that, verifying a Protocol Buffer compiler once and for all. This proof is parameterized over the data schema, such that we can derive functional correctness proofs for the serializer and deserializer generated for an arbitrary data description. One of the challenges here is that the Protocol Buffer standard was designed with flexibility, not verification, in mind. It imposes all the typical
challenges of verifying handwritten serializer and deserializer functions and more. Firstly, both the signature and the implementations of the generated functions are highly dependent on the supplied data description. Secondly, the format is highly flexible, such that the same structured data value can be encoded into many different binary strings; a correct deserializer must be able to recover this value from each of these. To overcome these challenges, we have made the following contributions:

- We have formalized a practical subset of version 3 of the Protocol Buffer standard in Coq [28], capturing its dependent data representations and its flexible encoding strategy.
- We have implemented serializer and deserializer generators, and proved them functionally correct with respect to the standard.
- We have evaluated our implementation by extracting OCaml implementations of a serializer and deserializer for the reference example in Protocol Buffer’s official repository [17]. In addition, we have used the official conformance tests to validate that our formalization faithfully captures Protocol Buffer’s informal specification.

Our system is available in an accompanying code supplement.

Key to our approach is a decomposition of the specification of the format into two separate layers which progressively relate a structured data value to its possible encodings. We then construct serializers and deserializers by composing together verified implementations for each of the intermediate layers, so that we are able to decompose the “end-to-end” correctness proof into proofs of correctness for each of the layers. This allows us to cleanly separate the representation of multiple encodings of a value from the specification of the bit-level representation of the encoded data, as Section 3 will discuss in more detail.

In order to concretize our discussion, we begin with an example of how our system can be used to derive serializers and deserializers from a data description. In Protocol Buffers, this description is typically called a message descriptor, and the structured values it describes are called messages. Consider the following simple descriptor for a timestamp message:

\[
\text{Message Timestamp} \quad \text{Descriptor} \quad := \quad \text{[[(Singular (Base int64), \text{"seconds"}, 1)]; (Singular (Base int32), \text{"nanos"}, 2)]}.
\]

Our “compilers” are simply functions which take a descriptor as an argument:

\[
\text{Definition encode_timestamp} : \text{[Timestamp]} \rightarrow \text{Bytes} := \quad \text{encode_message Timestamp}.
\]

\[
\text{Definition decode_timestamp} : \text{Bytes} \rightarrow \text{option \text{[Timestamp]} :=} \quad \text{decode_message Timestamp}.
\]

\[\text{[Timestamp]} \] is the Coq type of messages denoted by the descriptor Timestamp; Section 3 provides the complete details of this denotation function. We can use Coq’s extraction mechanism to extract executable OCaml implementations of encode_timestamp and decode_timestamp.

We have proven soundness theorems for encode_message and decode_message too, which can be instantiated with a concrete message descriptor:

\[
\text{Theorem} \quad \text{encode_timestamp_correct} \equiv \quad \text{encode_message_correct Timestamp}.
\]

\[
\text{Theorem} \quad \text{decode_timestamp_correct} \equiv \quad \text{decode_message_correct Timestamp}.
\]

The statements of these soundness theorems are given in Section 3. These theorems can be used to prove end-to-end correctness of a larger verified system that makes use of these implementations.

The rest of the paper proceeds as follows: we begin by highlighting the flexibility of the Protocol Buffer format before giving its complete specification. We then discuss the generation of and soundness proofs for serializers and deserializers in Section 4. In Section 5, we evaluate our system by implementing a reference example, which we validate using the official conformance test. Section 6 presents related work before a discussion of future work in Section 7, which is followed by the conclusion.

2 An Introduction to Protocol Buffers

We begin with a brief introduction to Protocol Buffers, in order to give readers an intuition of the format. To define the shape of a Protocol Buffer message, a user provides a message descriptor in a “.proto” file that is fed to a Protocol Buffer compiler. The message descriptor for the timestamp example from Section 1 is as follows:

```
message Timestamp {
  int64 seconds = 1;
  int32 nanos = 2;
}
```

In this example, the first line specifies the name of the data type: Timestamp. Inside the curly brackets, each line defines a field of this data type, which consists of the type, the name and the tag of this field. The next section will discuss the types of fields in more detail. Names of fields are only used by the users to access or update these fields of parsed, structured data, and do not appear in the serialized data. The message’s tags need to be unique numbers and they are used to identify the fields in the encoded binary format. From this description, a Protocol Buffer compiler will generate a data type implementation in a chosen target language, with an interface to manipulate, serialize, and deserialize messages.

2.1 Structured Data

Protocol Buffers support more types than just int32 and int64, including floating points, booleans, and strings. Types can
furthermore be either scalar or repeated. Scalar types include base types like integers, composite types like enumerations, and other user-defined types. The latter are typically called embedded messages or embedded fields. Repeated types are simply sequences of some scalar type, including embedded messages. The following data descriptor for a Person message includes examples of all these features:

```cpp
message Person {
  int32 id = 1;
  string name = 2;
  repeated int32 advisors = 3;
  Timestamp last_updated = 4;
}
```

The id and name fields are scalar fields of type 32-bit integer and string, respectively. The advisors field is a sequence of integers. last_updated is an example of an embedded field, whose type is the Timestamp message defined above.

Importantly, every Protocol Buffer type has a default value that is used when a field is not included in the encoded message. The use of default values can reduce the size of messages, since it is not necessary to encode a field that has a default value. Not surprisingly, the default value of numeric types is 0, of strings is the empty string, and of repeated fields is the empty list. The default value of embedded messages, e.g., last_updated, is underspecified in the Protocol Buffer documentation. In our implementation, we choose to use option types to represent embedded messages, so that the default value of an embedded message is None. This aligns with the value of null used by the official Protocol Buffer C++ implementation.

### 2.2 Serialized Data

An encoded Protocol Buffer message is a binary string which is essentially a sequence of key-value pairs. Each key-value pair represents a field or a part of a field, where the key includes both the field tag and the type of a value. As an example, a timestamp message whose seconds field is 1 and nanos field is 10 can be encoded as the binary string: 08 01 10 0A. The first byte, 08, is a package of the tag and the wire type of a field. At a first approximation, this byte signifies that the subsequent byte, 01, is an integer and has a field tag of 1, i.e. it is the value of the seconds field. Similarly, the third byte, 10, indicates that the following byte is the value of the nanos field.

The format includes the wire type as part of the key to ensure that every pair contains enough information to determine the length of its value. In version 3 of the Protocol Buffer standard, there are only four wire types: varint, 32-bit, 64-bit and length-delimited. Section 3 discusses how wire types map to field types in more detail. Each wire type is associated with a distinct number, and determines how subsequent bytes are to be deserialized. Variable-length integers (varint) are encoded as base 128 varints [15]. In this format, the lower seven bits of each encoded byte represent the corresponding seven bits of the integer, while the most significant bit indicates whether subsequent bytes should be included. Somewhat counterintuitively, variable length integers are even used as the wire type for fixed-width numbers, as this allows smaller values to be encoded with fewer bytes. The length-delimited wire type is used for string-like types, repeated types, and embedded messages. Values of this wire type are serialized by first encoding the number of bytes of the encoded value as a varint, followed by the actual value. This encoding of length-delimited wire types makes the Protocol Buffer format a non-context free language.

#### Figure 1. The encoded bits, 08 01, for seconds field

A field’s tag and its wire type are packed together into a variable-length integer, with the three lowest bits encoding the wire type of the value and the higher bits encoding the field’s tag. An example is shown in Figure 1. We can now consider how to encode various fields of the Person message:

- A name field with a value of “Bob” is encoded as 12 03 42 6F 62. The lower three bits of the tag are 3 this time, indicating this is a length-delimited wire type, while the higher bits are the tag of name. A length-delimited wire type indicates that next varint is the number of bytes in the value, three in this case of the “Bob” value.
- An advisors field with a value of [1;2;3] is encoded as 1A 03 01 02 03. The first varint is, again, the tag of advisors and the length-delimited wire type. The second varint is the number of bytes of the value and then the value of each element follows, in order.
- A last_updated field whose embedded message has a seconds field of 1 and a nanos field of 10 is encoded as 22 04 08 01 10 0A. The first varint is the tag of last_updated and the wire type length-delimited. The second varint is the number of bytes in the embedded message, which is recursively encoded using the same process, resulting in the same string as the first example.

We noted above that 08 01 10 0A is only one of many possible encodings. Since Protocol Buffer strives for maximum flexibility, structured data may be encoded in many different ways. The standard permits many kinds of flexibility:

- Fields can be serialized in arbitrary order. A Timestamp message can be encoded by first encoding name and then id, or the other way around.
- Fields can be absent, indicating that the absent field should have the default value associated with its type.
Thus, both 08 01 and 10 0A are valid encodings of a Timestamp.

- Scalar fields can occur multiple times, with only the last one taking effect. This allows clients to update a field by simply appending more bytes to the encoded representation. Thus, 08 02 08 01 is a valid encoding of a Timestamp whose seconds field is set to 01.
- A message may include unknown fields, whose tags do not appear in the message descriptor. This feature is for backward-compatibility: one client may update its descriptor with additional fields which are unknown to other clients. Instead of generating errors, the other clients will simply ignore the unknown fields when deserializing.
- Repeated fields can be broken up into pieces which are encoded individually. Each piece may be a single element of the original list encoded as a scalar type, or a few elements encoded as a repeated type. The corresponding value of this field is the concatenation of all the pieces in order. The encoding may interleave other fields between each piece. For example, the byte string 18 01 0A 02 02 03 is another valid encoding of the field advisors with its value set to [1;2;3]. Here, the first key-value pair has the advisors tag and a varint wire type, so the next byte is the first element of the list. The next key-value pair again has the advisors tag, but it has a length-delimited wire type to indicate the subsequent value is a slice of the list.
- Embedded messages can be similarly broken up into pieces, with each piece containing a few fields of the message. As an example, 22 02 08 01 22 02 10 0A encodes the last_updated field by individually encoding each of the fields of the embedded message.

In summary, there are many different ways to encode a particular message, all of which need to be captured by our specification of the Protocol Buffer format.

3 A Formalization of Protocol Buffers

This section presents a Coq formalization of a subset of the Protocol Buffer format that captures the key features of the standard. Our formalization includes a model of structured data built from a selection of base types, repeated and scalar fields, and embedded messages, as well as a precise specification of the valid binary encodings of a message. Section 7 discusses the missing features in more detail, but they represent a straightforward extension of this core. We present our formalization in pseudocode for clarity; the full implementation is included in the accompanying code supplement.

3.1 Encoding Descriptors and Messages

We begin by discussing our embedding of message descriptors and messages in Coq. Message descriptors are defined by the (mutually) inductive types shown in Figure 2.

\[
\text{Descriptor} : \text{Type} \Rightarrow \text{list Field} \\
\text{Field} : \text{Type} \Rightarrow \text{PBType} \times \text{string} \times \text{N} \\
\text{PBType} : \text{Type} \Rightarrow \text{Singular SingularType} | \text{Repeated SingularType} \\
\text{SingularType} : \text{Type} \Rightarrow \text{Base BaseType} | \text{Embedded Descriptor} \\
\text{BaseType} : \text{Type} \Rightarrow \text{int32} | \text{int64} | \text{fixed32} | \text{fixed64} | \text{string} \\
\text{WireType} : \text{Type} \Rightarrow \text{varint} | \text{32bit} | \text{64bit} | \text{length-delimited}
\]

A message descriptor is just a list of field descriptors\(^1\). Each field descriptor contains its Protocol Buffer type, denoted by PBType, its name, and its tag. Because the name is not used when encoding, a message descriptor is effectively a mapping from tags to their associated Protocol Buffer types. A Protocol Buffer type can be either a singular or repeated type. A singular type is either a base type or an embedded message, which takes another descriptor as its argument. Our implementation only supports a subset of Protocol Buffer base types, but it is a simple matter to add more base types. The Coq embedding of our Timestamp and Person message descriptors is straightforward:

\[
\text{Timestamp} : \text{Descriptor} \Rightarrow \\
[(\text{Singular (Base int64)}, \text{"seconds"}, 1); \\
(\text{Singular (Base int32)}, \text{"nanos"}, 2)] \\
\text{Person} : \text{Descriptor} \Rightarrow \\
[(\text{Singular (Base int32)}, \text{"id"}, 1); \\
(\text{Singular (Base string)}, \text{"name"}, 2); \\
(\text{Repeated (Base int32)}, \text{"advisors"}, 3); \\
(\text{Singular (Embedded Timestamp)}, \text{"last_updated"}, 4)]
\]

A particular message descriptor, desc, can be embedded as an inductive data type in Coq via a dependently-typed denotation function \(\llbracket\text{desc}\rrbracket\), so that the messages associated with desc are simply values of its denotation. Shallowly embedding messages in this way lets us leverage Coq’s type checker to ensure that messages are well-formed with respect to a particular message descriptor. Figure 3 shows the definition of the denotation function for message descriptors; we overload this notation to define denotation functions for all the data types in Figure 2.

Since Coq does not allow records to be defined programmatically, we denote the descriptor into a generic Tuple type. A Tuple is essentially a fixed-length heterogeneous list [8], indexed by a list of types. Each element in a Tuple corresponds to a field in the descriptor. For example, \(\llbracket\text{Timestamp}\rrbracket = \text{Tuple [N; N]}\). The first element, of type N, is the value of seconds and the second element is the value of nanos. Hence the tuple \(\llbracket\text{Timestamp}\rrbracket \Rightarrow [1, 10]\) is a message of Timestamp with seconds := 1 and nanos := 10. Because

\(^1\)Our implementation actually uses length-indexed vectors; we use lists here for presentation purposes.
A Verified Protocol Buffer Compiler

Subsection 2.1

the denotation of a single embedded defines some operations on message descriptors and

We are now equipped to specify the valid bit-level encodings of the messages associated with a particular descriptor.

The denotation of a field is just the denotation of the underlying Protocol Buffer type. The denotation of a Protocol Buffer type is also straightforward, although as we mentioned in Subsection 2.1 the denotation of a single embedded message is an option type. Base types are first mapped to a wire type via the toWireType function; these are then denoted to normal Coq types. Since all base types with the same wire type are encoded in the same way, we do not distinguish their embeddings in Coq.

Figure 3. Denotation of Message Descriptor

each Tuple type has a fixed-length, users can only access defined fields. As a convenience, we have defined special functions for accessing a particular field by name: ts!"seconds" = 1, for example. Attempting to access an unknown field will generate a type error.

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Figure 3. Denotation of Message Descriptor


toWireType fixed32 := toWireType fixed64
toWireType string := length–delimited

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</thead>
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</tr>
<tr>
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</tr>
<tr>
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<td>word 64</td>
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Figure 4. Operations on descriptors and messages. BoundedTag desc is a tag that must appear in desc: it is essentially a numeric tag, packed with a witness of its presence. We do not have to worry about the operations accepting a non-existing tag this way.

These specifications will form the correctness criteria for serializers and deserializers. One natural way to specify such an encoding is via a dependently-typed function: format : ∀ desc : Descriptor, desc → Bytes. Unfortunately, such a function can only capture one possible encoding of a particular message, which is insufficient for specifying the correctness of a Protocol Buffer deserializer. Instead, we chose to specify the valid encodings of a message as a relation: format : ∀ desc : Descriptor, desc → Bytes → Prop. We call such a relation a format of a particular message descriptor. More generally, given a source type S and a target type T, a format of type S → T → Prop is a relation that relates any source to its valid targets. Given a format fmt, if (s, t)∈ fmt, then t is a valid encoding for s.

Instead of building this format relation directly, we construct it as the composition of two intermediate relations, as illustrated in Figure 5. This structure allows us to decompose the proofs of correctness for serializers and deserializers, which rely on this relation, into more manageable pieces. The first of these layers covers the sources of flexibility of

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the Protocol Buffer standard described in Subsection 2.2 by relating a message to a set of valid intermediate representations. The intermediate representation, which will be called IR in the remainder of this paper, is a linearized representation of a message which fixes the logical sequence of key value pairs that will be included in the serialized bitstring. This IR is one step closer to the final bitstring, but defers bit-level details to the next layer. As an example, one possible representation of the previous Timestamp example at this layer would be \([(1, 1), (2, 10)]\). This format is encoded as an inductively defined data type in Coq:

\[
\text{format_to_ir : } \forall \text{desc : Descriptor} . \llbracket \text{desc} \rrbracket \rightarrow \text{IR} \rightarrow \text{Prop}.
\]

The second layer relates IR values to binary strings. This layer does not contain any non-determinism, so the format specification is quite straightforward: we sequentially format the elements in the IR list using a library of formats for wire types. For each element in the IR, we format its tag and its corresponding wire type, and finally the actual value according to its type. The resulting binary strings are concatenated to obtain the binary encoding of the entire message. The format for this layer has type:

\[
\text{format_ir_to_bs : Descriptor } \rightarrow \text{IR} \rightarrow \text{Bytes} \rightarrow \text{Prop}.
\]

Combining the intermediate formats from these two layers, we obtain an end-to-end specification format_message:

\[
\forall \text{desc : Descriptor} . \llbracket \text{desc} \rrbracket \rightarrow \text{Bytes} \rightarrow \text{Prop},
\]

as the composition of the relations given the descriptor:

\[
(s, t) \in \text{format_message} \iff \\
\exists t_1, (s, t_1) \in \text{format_to_ir} \land (t_1, t) \in \text{format_ir_to_bs}
\]

**Figure 6** shows an encoding of the Person message from before which is permitted by this format. We first relate the encoding of this message as an inductive data type to its IR. The non-deterministic format relation allows infinitely many IRs from this message; **Figure 6** shows one such IR. Note that the value of field last_updated is itself an IR value representing the embedded Timestamp message. The next layer relates this particular IR value to its binary encoding.

**Relating structured message to intermediate values** To explain how the first layer relates a structured message to its possible intermediate representations, we first provide a precise type definition for IR:

\[
\text{IR} : \text{Type} := \text{list IRElm}
\]

\[
\text{IRElm} : \text{Type} := N \times (\Sigma (w : \text{WireType}) . \llbracket w \rrbracket) \\
+ \Sigma (ty : \text{BaseType}) . \llbracket ty \rrbracket \\
+ \Sigma (ty : \text{BaseType}) . \text{list} \llbracket ty \rrbracket \\
+ \text{IR}
\]

The elements of an IR value are simply pairs of tags and a disjoint sum of values. We omit the constructors of the sum type and the first component of the dependent products when they are obvious from the context. Thus, we will write \((1, 1)\) for an element representing the second field with value 1 of Timestamp, instead of \((1, \text{in}_4(\text{in}_9(\text{int}64, 1)))\).

Readers may wonder why values are not simply the denotation of tag’s associated type, i.e. \(\llbracket \text{desc}[\text{tag}] \rrbracket\), where desc is the descriptor of the source message. One reason is that such an encoding does not allow for unknown tags. This is the motivation for including the first component of the sum type, which represents fields of arbitrary wire types \(\llbracket w \rrbracket\). Another reason is that fields of repeated type can be broken up into pieces, where each piece might be a single value or a list of values, so the type of this tag can be either \(\llbracket ty \rrbracket\) or \(\text{list} \llbracket ty \rrbracket\). The IR for the advisors field of the previous example could be \([3, [1; 2; 3]]\) or \([3, 1, (3, 2), (3, 3)]\), for example. In addition, if a field is an embedded message, its value will be a nested IR. For example, the IR for person’s last_updated field is \((4, [(1, 1); (2, 10)])\), whose value is the IR for the message of Timestamp.

Note that this definition allows an IR to be inconsistent with a message descriptor: if \(\text{desc}[\text{tag}]\) is Singular (Embedded desc), for example, the associated value has to be an IR value. For this reason, we have developed a well-formedness property for IR values with respect to a message descriptor desc. This property formalizes the set of valid sequences of key-value pairs allowed by the Protocol Buffer documentation. The well-formedness property serves two purposes: it is the criterion that deserializers use to discard nonsensical sequences, and it allows the format in the second layer to assume all the sources are valid, simplifying the soundness proofs for that layer.
Definition 3.2 (Well-formedness of IR and IRElm). We say an IR value is well-formed if all of its elements are well-formed, where an element (tag, v) is well-formed if it satisfies the following rules:

1. If tag \notin desc, v's type is \([w]\) for some wire type w.
2. If tag \in desc and desc[tag] = Singular (Base ty), v's type is \([ty]\).
3. If tag \in desc and desc[tag] = Repeated (Base ty), v's type is either \([ty]\) or list \([ty]\). In the case that toWireType ty = length-delimited, only \([ty]\) is permitted.
4. If tag \in desc, and desc[tag] = Singular (Embedded d') or desc[tag] = Repeated (Embedded d') for some descriptor d', v is a well-formed IR value.

The third rule ensures that if ty has a length-delimited wire type, v's type cannot be list \([ty]\). Otherwise, it would not be possible to tell whether the encoded value is a list of strings or a single string. For example, assume we have a field with a tag of 1, type of Repeated (Base string), and a value of ["Alice", "Bob"]. If this value can be formatted as (1, ["Alice", "Bob"]), it is impossible to tell if the on-the-wire value represents a single string or a list of strings. Hence, the standard disallows this case. Similarly, if desc[tag] = Repeated (Embedded desc'), v's type can only be IR.

Given this definition of IR, the intermediate format can be directly expressed as an inductively defined relation. We say msg' \vdash ir \simeq msg if ir correctly represents a "path" from msg' to msg. We call msg' the initial message and msg the result message, with ir explaining how to update the fields of msg' to arrive at msg. Figure 7 gives the definition of this relation. A complete message with descriptor desc can be related to its intermediate representations using an "default" initial message:

\[ir \simeq msg \equiv \text{default desc} \vdash ir \simeq msg\]

Intuitively, these rules spell out how to update the initial message to produce the result message by interpreting the IR as a series of updates. Seen in this manner, the IRNil rule is the base case of this process: an empty IR does not update the message, resulting in the same initial and result messages. The remaining rules explain how to perform a single update using the last element of the IR, with each rule updating the initial message according to the tag and the type of the value. Each judgment handles one aspect of the flexible encoding described in Subsection 2.2. For example, IRUnknown encodes the possibility of unknown fields, while IRSingular encodes the possibility of overwriting values. The treatment of missing fields is slightly more subtle: if a field is missing in ir, then there is no rule to update this particular field, so the field will retain the same value as the initial message. This is the reason the relation for complete messages uses a default initial message.

These rules can be used to define the relation used by the first layer:

format_to_ir (desc : Descriptor) (msg : [desc]) (ir : IR) : Prop :=
\text{default desc} \vdash ir \simeq msg

We prove the following lemma regarding well-formedness of intermediate values, in order to allow the second layer to safely assume that its source value is always well-formed.

Lemma 3.3. Given descriptor desc, for any message msg : [desc] and ir : IR, if \text{default desc} \vdash ir \simeq msg, then ir is well-formed.
• format_varint. The format for varints.
• format_word. The format for words, which takes an extra argument as its size. E.g., format_word 32 formats a 32-bit word to binary string.
• format_list. The format for list, which takes another format for its underlying types. E.g., format_list format_varint formats a list of varints.
• format_length_delimited. This format is just a composition of previous formats. It formats a list to a binary string and then prepends the size of this string as varint before it. E.g., format_length_delimited format_varint formats a list of varints with the size of the resulting string.

**Figure 8.** Formats for denotation types

\[
\frac{\text{(ir, bs)} \in \text{format_list format ir elm to bs}}{\text{(ir, bs)} \in \text{format ir to bs}} \quad \text{(IRFORMAT)}
\]

\[
\frac{\text{v : [ty]} \quad \text{(pack tag (toWireType ty), bs')} \in \text{format varint}}{\text{((tag, v), bs)} \in \text{format ir elm to bs}} \quad \text{(IRElmSINGULAR)}
\]

\[
\frac{\text{ir : IR} \quad \text{(pack tag length--delimited, bs')} \in \text{format varint}}{\text{((tag, ir), bs' + bs)} \in \text{format ir elm to bs}} \quad \text{(IRElmIR)}
\]

\[
\frac{\text{v : [ty]} \quad \text{(v, bs)} \in \text{format singular val}}{\text{(v, bs)} \in \text{format ir val to bs}} \quad \text{(IRValSINGULAR)}
\]

\[
\frac{\text{ir : IR} \quad \text{(ir, bs)} \in \text{format length--delimited format ir elm to bs}}{\text{(ir, bs)} \in \text{format ir val to bs}} \quad \text{(IRValIR)}
\]

**Figure 9.** A subset of format ir to bs relation

**Relating intermediate values to binary strings** The second layer of the relation relies on subformats that relate each of the denoted types to binary strings. The most important of these are listed in Figure 8.

A subset of this relation is shown in Figure 9. The relation format_singular_val relates a singular wire type value to a bitstring by using the formats corresponding to the value’s type. The pack function makes a package of tag and wire type, as explained in Subsection 2.2. Figure 9 shows the cases when the value of an IR element is a singular type or an IR value, but other cases can be derived in a similar manner. Note that the rules in Figure 9 do not have to check if the tag matches the type in descriptor, thanks to the well-formedness guarantee provided by the first layer.

**Figure 10.** Definition of encode_to_ir

### 4 Sound Generation of Serializers and Deserializers

This section first discusses how we generate serializers and deserializers from a message descriptor. We then show how the specification of the Protocol Buffer format from the previous section is used to state and prove these functions correct.

#### 4.1 Generating Serializers

A serializer for a particular message descriptor maps messages of that descriptor type to bitstrings:

\[
\text{encode_message : \forall desc : Descriptor, [desc] \rightarrow Bytes.}
\]

Much like the Protocol Buffer format, encode_message is implemented as a composition of functions to and from intermediate values. The first of these functions: encode_to_ir: \forall desc : Descriptor, [desc] \rightarrow IR is straightforward, and shown in Figure 10: each field in the given message is encoded in turn. Although the format admits many possible intermediate encodings of a message, encode_to_ir chooses the "canonical" one, in that it makes the same choices as the reference implementation when possible. In particular, it encodes a repeated field as a length-delimited list, unless the field is a repeated string. The function implementing the last layer, encode_ir_to_bs: Descriptor \rightarrow IR \rightarrow Bytes, is identical to the format relation, which dictates a single encoding for each IR value. The end-to-end serializer is simply a composition of these functions:

\[
\text{encode_message (desc : Descriptor) : [desc] \rightarrow Bytes = (encode_ir_to_bs desc) \circ (encode_to_ir desc)}
\]

**Correctness of Generated Serializers** A correct serializer for a message descriptor is a refinement of the format for that descriptor, in the sense that it settles on a single target value allowed by the format relation for every message:

**Theorem 4.1 (Soundness of Protocol Buffer Serializer).** For all well-formed descriptors, desc, encode_message desc will
map each source message to a target encoding permitted by format_message desc:

\[ \forall s \ t. \ encode_message \ desc \ s = t \rightarrow (s, t) \in format_message \ desc \]

This soundness proof is decomposed into proofs of correctness for the intermediate functions. The proof of correctness for encode_to_ir is the most interesting of the two, and proceeds by nested induction on both the intermediate representation and the message descriptor. The key lemma needed for this proof is:

**Lemma 4.2.** Given desc, msg msg’ : ⟦desc⟧, ta and ty. If the following assumptions hold:
1. msg’ ⊢ ir = msg
2. descriptorOK (tg, ty)::desc
3. every tag in ir is also in desc

we can conclude that v::msg’ ⊢ ir = v::msg for any v : ⟦ty⟧ .

This lemma captures the fact that when a descriptor is augmented with a new field, and a new value is accordingly added to its message, if the tag of this new field is not present in ir, this ir will preserve the transition to the new message modulo the new value. The second assumption ensures that tg ≠ desc, since tags are unique, while the third ensures that tg is not in ir.

### 4.2 Generating Deserializers

A deserializer for a particular message descriptor is a partial function from bitstrings to messages:

\[ decode_message : \forall desc : Deserializer, Bytes \rightarrow \text{option } \langle desc \rangle . \]

A decoder should signal an error via None if the input bitstring is malformed, i.e. not permitted by the format for the message descriptor. Similar to the implementation of serializers, decode_message is defined as a composition of intermediate functions. The functions are algorithmically straightforward, although ensuring their termination requires some care. The function for the first layer, decode_from_ir: ∀ desc : Deserializer, IR \rightarrow \text{option } \langle desc \rangle closely mirrors the inference rules in Figure 7, iteratively updating the default message using the key-value pairs in the intermediate representation. The second function, decode_from_bs: Descriptor \rightarrow Bytes \rightarrow \text{option IR} inverts encode_to bs by decoding the fields from the bitstring using counterparts to the formats in Figure 8 and concatenating them to build the intermediate representation. The functions rely on a fuel parameter to guarantee termination.

In order to ensure that decoders have enough fuel, they rely on measure functions for binary strings and IR values, with the measurement of a binary string being its length. The measurement of an intermediate representation is the total number of elements it contains, including the elements from any embedded messages. For example, the IR in Figure 6 has six total elements: four for the outermost IR value and two for the inner IR value in last_updated. Another consideration is that decode_ir_from bs needs to check whether a bitstring is malformed, e.g., the decoded wire type has to be consistent with the decoded tag.

The implementation of decode_message is the composition of these two functions:

\[ decode_message (desc : Deserializer) (bs : Bytes) : \text{option } \langle desc \rangle := \]

\[ \text{let ir := decode_ir_from_bs desc bs in} \]

\[ \text{match ir with} \]

\[ | \text{Some ir’} \Rightarrow \text{decode_from_ir desc ir’} \]

\[ | \text{None} \Rightarrow \text{None} \]

end.

**Correctness of Generated Deserializers** A correct decoder should recover a message from all of its possible encodings, and signal an error if the input bitstring does not encode any message:

**Theorem 4.3** (Soundness of Protocol Buffer Deserializers). For all well-formed descriptors, desc, decode_message desc will map every bitstring in the codomain of format_message desc to a related source value, returning None otherwise:

\[ \forall s \ t. \ (s, t) \in format_message desc \rightarrow decode_message \ t = \text{Some } s \land \]

\[ \forall s \ t. \ decode_message \ t = \text{Some } s \rightarrow (s, t) \in format_message desc \]

The proof of this theorem is derived from lemmas about the correctness of decode_ir_from bs and decode_from_ir. The proof of correctness for decode_ir_from bs requires a proof that it preserves the well-formedness of intermediate messages. Since its format assumes that the source IR is always well-formed, the deserializer needs to discard any invalid IRs.

**Lemma 4.4.** For any descriptor desc and binary string bs, if descriptorOK desc and decode_ir_from bs desc bs = Some ir, then ir is well-formed.

The soundness proof for decode_from_ir is by induction on the fuel. Recall that the value of an IR element can itself be an IR value, so inducting on the fuel parameter provides a strong enough induction hypothesis to handle any embedded IR values.

### 5 Evaluation

To demonstrate the utility of our system, we have reimplemented an example from the Protocol Buffer official repository.

2 This example can be found in /examples/(addressbook.proto, add_person.cc, list_people.cc).
in the Protocol Buffer format and prints all the contacts in it. The message descriptor has a straightforward embedding as a
Descriptor:

**Definition** Timestamp : Descriptor :=
[(Singular (Base int64), "seconds", 1);
(Singular (Base int32), "nanos", 2)].

**Definition** PhoneNumber : Descriptor :=
[(Singular (Base string), "number", 1);
(Singular (Base int32), "type", 2)].

**Definition** Person : Descriptor :=
[(Singular (Base string), "name", 1);
(Singular (Base int32), "id", 2);
(Singular (Base string), "email", 3);
(Repeated (Embedded PhoneNumber), "phones", 4);
(Singular (Embedded Timestamp), "last_updated", 5)].

**Definition** AddressBook : Descriptor :=
[Repeated (Embedded Person), "people", 1].

To implement the serializer and deserializer for AddressBook messages, we simply concretize the parametrized descriptor:

**Definition** encode_addressbook := encode_message AddressBook.

**Definition** decode_addressbook := decode_message AddressBook.

To execute these functions, we used Coq’s extraction mechanism to produce OCaml modules with message serialization and deserialization functions. We then linked these modules with OCaml implementations of "add_person" and "list_people" which handled IO operations. To show that our functions can serve as a replacement for the official implementation, we read and write to the same address book database with both our implementation and the reference implementation. Unsurprisingly, both implementations successfully process the serialized file and print out the expected information.

5.1 Conformance Tests

We have mechanically certified that our compiler meets its specification, but it is possible that our specification does not conform to Protocol Buffer’s informal specification. In order to validate our specification, we tested our implementation against Protocol Buffer’s official conformance test suite. These tests consist of a test runner and a client. The runner creates a test client process and sends it requests for each test case in the suite. The test client receives each request, decodes the payload, encodes the data back to the requested output format, and then sends the result back to the test runner. Clients may also respond with an error, as some test cases are intentionally malformed. The test runner accumulates all the test responses and eventually reports both the successful and failing tests.

Each request includes the message that the client should process, as well as the input and output format. Protocol Buffers support encoding not only to its binary format but also to JSON, so the test runner may ask the client to decode the data from JSON or encode the data to JSON, although clients are usually asked to use the binary format. We skipped all the JSON tests and Protocol Buffer version 2 tests, as we do not support those formats. Some tests require some features that we do not yet support, such as the oneof type. We modified and used the official Python test client as a proxy to process the requests and responses, and sent the payload to our OCaml client to perform the real tests. Our OCaml client reads the message from standard input, deserializes and serializes the message, and then writes the result to standard output. Our OCaml client uses extracted Coq code in a similar manner to the aforementioned address book example.

Our implementation successfully passed 179 of 194 test cases. The fifteen failing test cases are not surprising: ten of these failing tests use oneof types, which we do not support. Another failing test uses version 3.5 of Protocol Buffers, which requires the unknown fields to be retained during parsing and included in the serialized output, another feature we currently do not support. Our implementation fails the final four tests because in base 128 varints format, the most significant bit can be set to 1 if the next byte is 0. For example, 0 can be encoded as 0, 80 0, and 80 80 0, but our current implementation only handles the canonical encoding. These results suggest that our specification is a correct formalization of Protocol Buffer’s informal description.

6 Related Work

**Formally Verified Parsers for Context-Free Languages**

In order to reduce the trusted code base of formally verified compilers, there have been a number of efforts to verify standalone parsers for context-free languages. These are not sufficient to build a Protocol Buffer compiler for two key reasons: firstly, Protocol Buffer’s binary format is not context-free, due to its length-delimited wiretype. Secondly, these parsers would constitute only half a solution to deserialization, as semantic actions are also needed to build a message from a parse tree. Our deserializers handle both parsing the binary string and building an in-memory message from the parsed data. Barthwal and Norrish formally verified an SLR parser generator in HOL [5], showing every generated automaton is both sound and complete with respect to the grammar it was generated from. In contrast, Jourdan et. al formally verified a validator for LR(1) automata produced by an untrusted parser generator [18] to avoid formally verifying the generator itself. Koprowski andBinsztok [19] developed an operational semantics of partial expression grammars (PEGs) with semantic actions and proved that an interpreter was sound with respect to those semantics. In other related work, the authors of RockSalt [22], a formally verified Native Client sandbox-policy checker, developed a regular-expression DSL in order to specify and generate parsers from bitstrings into
various instruction sets. This DSL was equipped with a rela-
tional denotational semantics that the authors used to prove
correctness of their parser. Subsequent work [27] extended
this DSL to support bidirectional grammars in order to pro-
vide a uniform language for specifying and generating both
decoders and encoders, proving a similar notion of consis-
tency to what we present here.

Extensible Format Description Languages Alternative
interface generators include XDR [26], ASN.1 [12], and Apache
Avro [4], each of which provide their own domain-specific
data description languages and compilers for their respective
languages. There has been limited work on verified interface
generators. One notable exception is the work of Collins et. al [9] to verify that the encoders and decoders gener-
ated by an untrusted ASN.1 compiler satisfy a round-trip
This round-trip property states that the encoder and decoder
functions are inverses of each other. Notably, this specification
uses functions, not relations, as their compiler uses the
deterministic distinguished encoding strategy. Much of the
work in that project was getting the ASN.1 compiler to
generate code amenable to automatic analysis by SAW, and
there are no guarantees regarding other formats specified in
ASN.1.

The Verdi [31] framework for building verified distributed
systems originally used OCaml’s (unverified) Marshal library
to serialize data. In order to reduce the trusted code base,
Verdi’s authors are developing a verified serialization library
for Coq called Cheerios [25]. The framework packages a
type and its associated encoder and decoder functions into a
typeclass, along with a proof that the deserializer is sound
with respect to the encoder function. Typeclass resolution
is used to automatically build encoders and decoders in a
type-directed manner. Once again, this library strategy does
not consider the possibility of noncanonical encodings.

Geest et. al [29] proposed a verified system to describe
data formats in an embedded domain-specific language and
to derive serializers and deserializers from these descriptions.
They modeled the data schema as an universe, which is a col-
lection of types in some structure, and defined a denotation
function to map the universes to the actual types in Agda.
This is similar to our definition of message descriptor as data
schema, which dictates the actual types of the messages by
denotation function. They also decomposed the transforma-
tion into two layers: the high-level data, such as the struc-
tured data containing natural numbers, is first converted to
low-level data, the same structured data with corresponding
words, and then the low-level data is serialized to strings.
While our system also has a similar architecture and the
intermediate representation has a similar role as their low-
level data, our first layer handles the non-determinism rather
than type conversion. Unlike our system, their encoding and
decoding process is canonical, thus cannot handle Protocol
Buffer’s flexibility.

Our implementation builds upon the Narcissus frame-
work [10] for synthesizing serializers and deserializers from
relational specifications. The framework includes a user-
extensible library of format combinators and a set of tactics
for deriving implementations of serializers and deserializ-
ers from these specifications. In Narcissus, serializers and
deserializers are derived directly from arbitrary format speci-
fications, and proofs of correctness are constructed alongside
the functions. In contrast, our compiler takes a fixed data de-
scription language and produces serializers and deserializers
that conform to the Protocol Buffers standard. By sacrificing
flexibility, however, we are able to prove our compiler correct
once and for all, although our proofs are mostly manual. Our
statements of correctness use Narcissus’ specifications for se-
rializers and deserializers. The second layer of our compiler
relies on Narcissus’ definitions of common data structures
and fixed-width word format in order to serialize IR val-
ues, although we had to extend the library with additional
formats specific to Protocol Buffers, e.g., varints.

7 Future work
This section discusses the missing features and possible fu-
ture improvements for our formalization. As noted in Sec-
tion 1, the subset of Protocol Buffer version 3 we currently
support is realistic enough to be used in most applications.
However, there are a number of features that are needed to
make our compiler fully functional.

- We do not support oneof types, which are essentially
  sum types. To support this feature, we have to extend
  the definitions of message descriptor and its denota-
  tion, and also the inference rules of the first layer to
  capture the behavior of oneof types. Since all the mem-
bers of a oneof type have their own tags but share the
same field, the main difficulty is probably that we need
to "group" the tags and manipulate the message by
this group, instead of a single tag. Unsurprisingly, we
should not have to change the second layer at all.

- We do not support recursive and mutually recursive
  embedded messages. That is, the fields of a message
cannot have the same type as the message itself. This
feature is rarely used in practice: the official confor-
mance suite does not include any tests for this feature.

- Our current work focuses on serializers and deserial-
izers, so all the base types are denoted into the Coq
types that are actually used in serialization. While we
still provide a usable programming interface, it is not
so pleasant for end-users. As one example, bool is de-
noted into the integer type, but users will probably
expect to use booleans when manipulating a bool field.
One potential solution is to have another denotation
that maps the base types to more user-friendly Coq
types. We could then add another layer on top of the current architecture which relates the new denotation to the one used in this paper, and develop encoders and decoders for that layer.

- In Protocol Buffers version 3, unknown fields are discarded. However, in version 3.5, such fields are retained during parsing and included in the serialized output.

- The encoding of varints is also non-deterministic: the most significant bit can be set to 1 if the next byte is 0. To support this feature, we could extend the format to non-deterministically choose between these two cases, although this would complicate the proof of deserializer correctness.

8 Conclusion

We have presented a formally verified compiler for a realistic subset of the Protocol Buffer serialization format, which can generate provably correct serializers and deserializers for an arbitrary message descriptor. We can extract the resulting implementations to OCaml, and the soundness proofs can be used as part of verifying a larger system. We have demonstrated the usability of our system on an example drawn from Protocol Buffer’s official repository, and shown that our implementation satisfies all the official conformance tests whose features we support.

Acknowledgments

We thank Robert Dickerson, and the anonymous reviewers for their valuable input. This research was supported through a faculty startup package from Purdue University.

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