Chapter 7
Intermediate Representation
Motivation

• ASTs are too high level and grammar dependent
  – Different languages entail different implementations.
  – Different machines entail different implementations.
  – We need something lower, closer to machine code so that
    • The ASTs from various languages can be translated into this uniform IR.
    • Translations to various machine code can be done with the IR.
What are the difference between AST and low level IR

- **Conditionals**
  - If-then-else does not exist in machine level instructions. Instead, comparisons and conditional jumps (to only one target).

- **Array and field references**
  - At low level, we need to think about heap/stack, and decide the corresponding addressing mechanism.

- **Method calls**
  - In AST, we may have various numbers of arguments.
  - At low level, we have only one “call” instruction.
Low Level Tree Representations

• Such tree representation is also used in compilers such as GCC (called RTL and RTX there).

• Translation to Intermediate Code is indeed a process of tree rewriting.
## IR trees: Expressions

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CONST i</td>
<td>Integer constant $i$</td>
</tr>
<tr>
<td>NAME n</td>
<td>Symbolic constant $n$</td>
</tr>
<tr>
<td>TEMP t</td>
<td>Temporary $t$, [one of any number of “registers”]</td>
</tr>
</tbody>
</table>
| BINOP $e_1$ $e_2$ | Application of binary operator:  
  ADD, SUB, MUL, DIV   
  AND, OR, XOR   
  SLL, SRL  
  SRA  
  to integer operands $e_1$ (evaluated first) and $e_2$ (evaluated second) |
| MEM e  | Contents of a word of memory starting at address $e$ |
| CALL $f$ [$e_1$, …, $e_n$] | Procedure call; expression $f$ is evaluated before arguments $e_1, \ldots, e_n$ |
| ESEQ $s$ $e$ | Expression sequence; evaluate $s$ for side-effects, then $e$ for result |
IR trees: Statements

MOVE
  TEMP  e
  t
Evaluate e into temporary t

MOVE
  MEM  e_2
  e_1
Evaluate e_1 yielding address a, e_2 into word at a

EXP
  e
Evaluate e and discard result

JUMP
  e  [l_1, \ldots, l_n]
Transfer control to address e; l_1, \ldots, l_n are all possible values for e

CJUMP
  e_1 e_2 t f
Evaluate e_1 then e_2, yielding a and b, respectively; compare a with b using relational operators:
  BEQ, BNE [signed and unsigned integers]
  BLT, BGT, BLE, BGE [signed]
  jump to t if true, f if false

SEQ
  s_1 s_2
Statement s_1 followed by s_2

LABEL
  n
Define constant value of name n as current code address; NAME(n) can be used as target of jumps, calls, etc.

CS352 Translating ASTs to IR trees
Some Examples

• A[i]=x+y;

• if (x>y)
  
  x=2

  else

  x=3
Things are Not That Easy

• The translations for \((x>3)\) in
  – \(y = x>3\)
  – \(\text{if } (x>3) \ s1 \ \text{else } s2\)

• The translations for \(x=3\) in
  – \(x=3; \ldots\)
  – \(\text{if } (x=3)\)

• Solution:
  – Let expressions, statements, and conditionals share the same base class `Translate.exp` so that one can be converted to the other in various contexts.
Kinds of expressions

Expression kinds indicate “how expression might be used”

**Ex**(exp) expressions that compute a value

**Nx**(stm) statements: expressions that compute no value

**Cx** conditionals (jump to true and false destinations)

\[
\text{RelCx.} \quad \text{op}(\text{left, right}) \quad \text{eq, ne, gt, lt, ge, le}
\]

**IfThenElseExp** expression or statement, depending on use

Conversion operators allow use of one form in context of another:

**unEx** convert to tree expression that computes value of inner tree

**unNx** convert to tree statement that computes inner tree but returns no value

**unCx**(t, f) convert to statement that evaluates inner tree and branches to true destination if non-zero, false destination otherwise
Translating MiniJava

Local variables: Allocate as a temporary $t$

\[
\begin{array}{c}
\text{TEMP} \\
\text{Ex(TEMP $t$)} \\
\text{$t$}
\end{array}
\]

Array elements: Array expression is reference to array in heap.
For expressions $e$ and $i$, translate $e[i]$ as:

\[
\text{Ex(MEM(ADD(e.unEx(), } \times (i.unEx(), \text{CONST($w$))))})
\]

where $w$ is the target machine’s word size: all values are word-sized (scalar) in MiniJava
Array bounds check: array index $i < e$.size; runtime will put size in word preceding array base

Object fields: Object expression is reference to object in heap.
For expression $e$ and field $f$, translate $e.f$ as:

\[
\text{Ex(MEM(ADD(e.unEx(), CONSTR(o))})}
\]

where $o$ is the byte offset of the field $f$ in the object
Null pointer check: object expression must be non-null (i.e., non-zero)
Translating MiniJava

String literals: Allocate statically:

```
.word 11
label: .ascii "hello world"
```

Translate as reference to label:

```
Ex(NAME(label))
```

Object creation: Allocate object in heap.

For class $T$, translate $\text{new } T()$ as:

```
Ex(CALL(NAME("new"), CONST(fields), NAME(label for $T$’s vtable)))
```

Array creation: Allocate array in heap.

For type $T$, array expression $e$, translate $\text{new } T[e]$ as:

```
Ex(ESEQ(MOVE(TEMP($s$), $e$.unEx()),
         CALL(NAME("new"), MUL(TEMP($s$), CONST($w$)), TEMP($s$))))
```

where $s$ is a fresh temporary, and $w$ is the target machine’s word size.
Control structures

Basic blocks:

- a sequence of straight-line code
- if one instruction executes then they all execute
- a maximal sequence of instructions without branches
- a label starts a new basic block

Overview of control structure translation:

- control flow links up the basic blocks
- ideas are simple
- implementation requires bookkeeping
- some care is needed for good code
while loops

while \((c)\) \(s\):

1. evaluate \(c\)
2. if false jump to next statement after loop
3. evaluate loop body \(s\)
4. evaluate \(c\)
5. if true jump back to loop body

e.g.,

if not\((c)\) jump done

body:

\(s\)

if \(c\) jump body

done:

\(N_x(SEQ(SEQ(c.unCx(b, x), SEQ(LABEL(b), s.unNx())), SEQ(c.unCx(b, x), LABEL(x))))\)
for loops

for \((i, c, u)\) 

1. evaluate initialization statement \(i\)
2. evaluate \(c\)
3. if false jump to next statement after loop
4. evaluate loop body \(s\)
5. evaluate update statement \(u\)
6. evaluate \(c\)
7. if true jump to loop body

\[
Nx(SEQ(i.unNx(),
    SEQ(SEQ(c.unCx(b, x), SEQ(LABEL(b), SEQ(s.unNx(), u.unNx()))),
    SEQ(c.unCx(b, x), LABEL(x)))))
\]

For \textbf{break} statements:

- when translating a loop push the \textit{done} label on some stack
- \textbf{break} simply jumps to label on top of stack
- when done translating loop and its body, pop the label
Method calls

\[ e_0.m(e_1, \ldots, e_n): \]

\[ \text{Ex(CALL(MEM(MEM(e_0.unEx(), -w), m.index \times w), e_1.unEx(),} \]
\[ \ldots e_n.unEx()))) \]

Null pointer check: expression \( e_0 \) must be non-null (i.e., non-zero)
Comparisons

Translate $a \ op \ b$ as:

$$ \text{RelCx.}\ op(a.\text{unEx}(), \ b.\text{unEx}()) $$

When used as a conditional $\text{unCx}(t, f)$ yields:

$$ \text{CJUMP}(a.\text{unEx}(), \ b.\text{unEx}(), \ t, \ f) $$

where $t$ and $f$ are labels.

When used as a value $\text{unEx}()$ yields:

$$ \text{ESEQ}(\text{SEQ}(\text{MOVE}(\text{TEMP}(r), \ \text{CONST}(1)), \ 
\text{SEQ}(\text{unCx}(t, f), \ 
\text{SEQ}(\text{LABEL}(f), \ 
\text{SEQ}(\text{MOVE}(\text{TEMP}(r), \ \text{CONST}(0)), \ \text{LABEL}(t)))))), \ 
\text{TEMP}(r)) $$
Conditionals

Translate short-circuiting Boolean operators (&&, ||, !) as if they were conditionals.

E.g., \( x < 5 \land a > b \) is treated as \( (x < 5) \text{ ? } (a > b) : 0 \)

We translate \( e_1 \text{ ? } e_2 : e_3 \) into IfThenElseExp(\( e_1, e_2, e_3 \))

When used as a value IfThenElseExp.unEx() yields:

\[
\begin{align*}
\text{ESEQ(SEQ(SEQ(} & e_1\text{.unCx}(t, f), \\
& \text{SEQ(SEQ(LABEL}(t), \\
& \text{SEQ(SEQ(MOVE(TEMP}(r), e_2\text{.unEx}()), \\
& \text{JUMP}(j))), \\
& \text{SEQ(LABEL}(f), \\
& \text{SEQ(MOVE(TEMP}(r), e_3\text{.unEx}()), \\
& \text{JUMP}(j)))), \\
& \text{LABEL}(j)), \\
& \text{TEMP}(r))
\end{align*}
\]

As a conditional IfThenElseExp.unCx(\( t, f \)) yields:

\[
\begin{align*}
\text{SEQ(} & e_1\text{.unCx}(tt, ff), \text{SEQ(SEQ(LABEL}(tt), e_2\text{.unCx}(t, f)), \\
& \text{SEQ(LABEL}(ff), e_3\text{.unCx}(t, f))))
\end{align*}
\]
Conditionals: Example

Applying \text{unCx}(t,f) \text{ to } (x < 5) \ ? \ (a > b) : 0:

\text{SEQ(BLT}(x.\text{unEx}(), \text{CONST}(5), tt, ff),
\text{SEQ(SEQ(LABEL}(tt, \text{BGT}(a.\text{unEx}(), b.\text{unEx}(), t, f)),
\text{SEQ(LABEL}(ff, \text{JUMP}(f)))))

or more optimally:

\text{SEQ(BLT}(x.\text{unEx}(), \text{CONST}(5), tt, f),
\text{SEQ(LABEL}(tt, \text{BGT}(a.\text{unEx}(), b.\text{unEx}(), t, f))))
var a : array [2..5] of integer;
...
a[e]

translates to:

MEM(ADD(TEMP(FP), ADD(CONST k − 2w, ×(CONST w, e.unEx))))

where k is offset of static array from the frame pointer FP, w is word size

In Pascal, multidimensional arrays are treated as arrays of arrays, so A[i,j] is equivalent to A[i][j], so this translation works for subarrays. Not so in Fortran.
Multidimensional arrays

Array allocation:

constant bounds
  - allocate in static area, stack, or heap
  - no run-time descriptor is needed

dynamic arrays: bounds fixed at run-time
  - allocate in stack or heap
  - descriptor is needed

dynamic arrays: bounds can change at run-time
  - allocate in heap
  - descriptor is needed
Multidimensional arrays

Array layout:

Contiguous:

1. Row major
   Rightmost subscript varies most quickly:
   
   \[ A[1,1], A[1,2], \ldots \]
   
   \[ A[2,1], A[2,2], \ldots \]
   
   Used in PL/1, Algol, Pascal, C, Ada, Modula, Modula-2, Modula-3

2. Column major
   Leftmost subscript varies most quickly:
   
   \[ A[1,1], A[2,1], \ldots \]
   
   \[ A[1,2], A[2,2], \ldots \]
   
   Used in FORTRAN

By vectors

Contiguous vector of \textit{pointers} to (non-contiguous) subarrays
Multi-dimensional arrays: row-major layout

array [1..N,1..M] of T
≡ array [1..N] of array [1..M] of T

no. of elt’s in dimension \( j \): \( D_j = U_j - L_j + 1 \)

position of \( A[i_1, \ldots, i_n] \):

\[
\begin{align*}
& (i_n - L_n) \\
& + (i_{n-1} - L_{n-1})D_n \\
& + (i_{n-2} - L_{n-2})D_nD_{n-1} \\
& + \cdots \\
& + (i_1 - L_1)D_n \cdots D_2
\end{align*}
\]

which can be rewritten as

\[
\begin{align*}
\text{variable part} & \quad i_1D_2\cdots D_n + i_2D_3\cdots D_n + \cdots + i_{n-1}D_n + i_n \\
\text{constant part} & \quad -(L_1D_2\cdots D_n + L_2D_3\cdots D_n + \cdots + L_{n-1}D_n + L_n)
\end{align*}
\]

Address of \( A[i_1, \ldots, i_n] \):

\[
\text{address}(A) + ((\text{variable part} - \text{constant part}) \times \text{element size})
\]
case (switch) statements

\[ \text{case } E \text{ of } V_1: S_1 \ldots V_n: S_n \text{ end} \]

1. evaluate the expression
2. find value in case list equal to value of expression
3. execute statement associated with value found
4. jump to next statement after case

Key issue: finding the right case

- sequence of conditional jumps (small case set)
  \[ O(| \text{cases} |) \]
- binary search of an ordered jump table (sparse case set)
  \[ O(\log_2 | \text{cases} |) \]
- hash table (dense case set)
  \[ O(1) \]
case (switch) statements

case $E$ of $V_1$: $S_1$ . . . $V_n$: $S_n$ end

One translation approach:

$t := expr$
jump test

$L_1$: code for $S_1$
jump next

$L_2$: code for $S_2$
jump next

. . .

$L_n$: code for $S_n$
jump next
test: if $t = V_1$ jump $L_1$
if $t = V_2$ jump $L_2$

. . .

if $t = V_n$ jump $L_n$
code to raise run-time exception

next:
Labels and gotos

A little complicated!

Resolving references to labels multiply-defined in different scopes:

```
begin
  L: begin
    goto L;
    ...{ possible definition of L }
  end
end
```

- Scope labels like variables
- On use, label definition is either resolved or unresolved
- On definition, backpatch previous unresolved label uses

Jumping out of blocks or procedures:

1. Pop run-time stack
2. Fix display (if used); static chain needs no fixing
3. Restore registers if jumping out of a procedure
Parameter passing

Place information in formal parameter location for callee to access actual parameter:

- value
- address
- dope vector

Parameter passing modes:

*value* *(copy-in)*, *result* *(copy-out)*, *value-result*
  
  Copy actual into formal on call, formal into actual on return

*reference* *(var)*, *read-only*
  
  Copy address of actual into formal

*name*, *formal procedures*, *label parameters*
  
  Name parameters are re-evaluated on every reference

Data objects distinguish:

- values (constants)
- locations (ordinary variables)
- addresses of locations containing values (indirect references, *var* parameters)
Value, result, value-result parameters

Value:

- treat formal as a local variable initialized with actual
- actual can be any expression of correct type

Result:

- treat formal as uninitialized local variable
- on return formal is copied into actual
- actual must be an l-value

Value-result:

- treat formal as local variable initialized with actual
- on return formal is copied to actual
- actual must be an l-value
Value, result, value-result parameters

Implementation:

Scalars:

- result/value-result \(\Rightarrow\) pass address of actual, copy value to/from local copy
- value \(\Rightarrow\) simply pass value directly

Arrays:

- pass dope vector
- static arrays \(\Rightarrow\) pass pointer to base of array
- result/value-result \(\Rightarrow\) two local dope vectors
- value \(\Rightarrow\) one local dope vector

Records:

- handle as scalar (since fixed in size)
- best to pass address, let callee copy (more compact calling sequences)
Reference and read-only parameters

Usually pass address

Scalars:

- reference $\Rightarrow$ pass address of actual
- read-only $\Rightarrow$ pass value (rather than address): copy actual into read-only local

Arrays: pass dope vector (simple pointer if static)

Records: pass base address