[40] Homework 3: Big-Oh

Due: September 27 by the end of the class.

[10] Which function grows faster (justify your answer):

- (i) $n^{\ln n}$ or $(\ln n)^n$?
- (ii) $n^{\ln \ln \ln n}$ or $(\ln n)!?$
- [10] Prove or disprove

$$\sum_{i=1}^{n} i^5 = \Theta(n^5).$$

[10] Evaluate

$$\left(n+2+O(n^{-1})\right)^n$$

with the relative error $O(n^{-1})$ (i.e., your answer should look like

$$(n+2+O(n^{-1}))^n = f(n) (1+O(n^{-1}))$$

for some function f(n).

[10] For the following pseudo-code determine the value returned in terms of n. Use big-Oh notation. Show your work.

int function sqr (int n) if $(n \le 2)$ then return(1) else return $(1 + sqr(\sqrt{n}))$