Towards Algorithmic Synthesis of Synchronization for Shared-Memory Concurrent Programs

Roopsha Samanta

Computer Engineering Research Centre,
The University of Texas at Austin.

`roopsha@cs.utexas.edu`

We present a framework that takes a concurrent program composed of unsynchronized processes, along with a temporal specification of their global concurrent behaviour, and *automatically* generates a concurrent program with synchronization ensuring *correct* global behaviour. Our methodology supports finite-state concurrent programs composed of processes that may have local and shared variables, may be straight-line or branching programs, may be ongoing or terminating, and may have program-initialized or user-initialized variables. The specification language is an extension of propositional Computation Tree Logic (CTL) that enables easy specification of safety and liveness properties over control and data variables. The framework also supports synthesis of synchronization at different levels of abstraction and granularity.

1 Introduction

Shared-memory concurrent programs are ubiquitous in today's era of multi-core processors. Unfortunately, these programs are hard to write and even harder to verify. We assert that one can simplify the design and analysis of (shared-memory) concurrent programs by, first, manually writing synchronization-free concurrent programs, followed by, automatically synthesizing the synchronization code necessary for ensuring the programs' correct concurrent behaviour. This particular approach to synthesis of concurrent programs was first developed in [7, 3] and was revisited more recently in [13, 24, 25]. The early synthesis papers focused on propositional temporal logic specifications and restricted models of concurrent programs such as synchronization skeletons. Even when dealing with finite-state programs, it is highly cumbersome to express properties over functions and predicates of program variables using propositional temporal logic. Besides, synchronization skeletons that suppress data variables and computations are often inadequate abstractions of real-world concurrent programs. The more recent synthesis approaches have fairly sophisticated program models. However, they are applicable for restricted classes of specifications such as safety properties, and entail some possibly restrictive assumptions. For instance, it is almost always assumed that all data variables are initialized within the program to specific values, thereby disallowing any kind of user or environment input to a concurrent program. The presence of local data variables is also rarely accounted for or treated explicitly. Finally, there has been limited effort in developing adaptable synthesis frameworks that are capable of generating synchronization at different levels of abstraction and granularity.

In this paper, we present a comprehensive treatment of synthesis of synchronization for concurrent programs with CTL-like specifications over program variables. We support finite-state concurrent programs composed of processes that may have local and shared variables, may be straight-line or branching, may be ongoing or terminating, and may be executed as a closed system (with no external environment) or with an external environment that may initialize the values of the program variables or read the values

of the program variables at any point in the programs' execution. We propose an extension to propositional CTL that helps express properties over program locations and data variables. These properties may be syntactic, e.g., $\mathsf{AG}\,\neg(loc_1 = l_1 \land loc_2 = l_2)$, specifying that the first and the second process cannot simultaneously be in locations l_1 and l_2, respectively, or semantic, e.g., $\mathsf{AG}\,(v_1 = \upsilon \Rightarrow \mathsf{AF}(v_2 = \upsilon + 1))$, specifying that if the value of variable v_1 is υ, then it is inevitable that the value of variable v_2 be $\upsilon + 1$, or both syntactic and semantic. Furthermore, as is evident from the above examples, these properties may express safety as well as liveness requirements. Finally, we support the synthesis of synchronization in the form of conditional critical regions (CCRs), or based on lower-level synchronization primitives such as locks and condition variables. In the latter case, the synthesized synchronization can be either coarse-grained or fine-grained.

Given a concurrent program P composed of synchronization-free processes, $P_1, P_2, \ldots, P_k$, and a temporal logic specification ϕ_{spec} specifying the expected concurrent behaviour, the goal is to obtain synchronized processes, $P_1^s, P_2^s, \ldots, P_k^s$, such that the concurrent program P^s resulting from their *asynchronous composition* satisfies ϕ_{spec}. This is effected in several steps in our proposed approach. The first step involves specifying the concurrency and operational semantics of the unsynchronized processes as a temporal logic formula ϕ_P. We help mitigate the user's burden of specification-writing by automatically generating ϕ_P. The second step involves construction of a tableau T_ϕ, for ϕ given by $\phi_P \land \phi_{spec}$. If the overall specification is found to be satisfiable, the tableau yields a global model M, based on $P_1, P_2, \ldots, P_k$ such that $M \models \phi$. The next step entails decompositon of M into the desired synchronized processes $P_1^s, \ldots, P_k^s$ with synchronization in the form of *CCRs*. The last step comprises a mechanical compilation of the synthesized CCRs into both coarse-grained and fine-grained synchronization code based on locks and condition variables.

To construct the tableau T_ϕ, we adapt the tableau-construction for propositional CTL to our extended specification language over variables, functions and predicates. When there exist environment-initialized variables, we present an initial brute-force solution for modifying the basic approach to ensure that P^s satisfies ϕ_{spec} for all possible initial values of such variables. Also, we address the effect of local variables on the permitted behaviours in P^s due to limited observability of global states, and discuss solutions.

The paper is structured as follows. We begin by introducing our specification language and program model in Sec. 2. We present a basic algorithmic framework in Sec. 3, focussing on the formulation of ϕ_P, tableau construction, model generation and extraction of CCRs. We then address extensions of the basic framework to deal with uninitialized variables, local variables, different synchronization primitives and multiple processes in Sec. 4. We conclude with a discussion of related and future work in Sec. 5.

2   Formal Framework

2.1   A vocabulary L

Symbols of **L**: We fix a vocabulary **L** that includes a set $\mathbf{L}^{\mathbb{V}}$ of variable symbols (denoted v, v_1 etc.), a set $\mathbf{L}^{\mathbb{F}}$ of function symbols (denoted f, f_1 etc.), a set $\mathbf{L}^{\mathbb{B}}$ of predicate symbols (denoted B, B_1 etc.), and a non-empty set $\mathbf{L}^{\mathbb{S}}$ of *sorts*. $\mathbf{L}^{\mathbb{S}}$ contains the special sort `bool`, along with the special sort `location`. Each variable v has associated with it a sort in $\mathbf{L}^{\mathbb{S}}$, denoted $sort(v)$. Each function symbol f has an associated arity and a sort: $sort(f)$ for an m-ary function symbol is an $m + 1$-tuple $< \sigma_1, \ldots, \sigma_m, \sigma >$ of sorts in $\mathbf{L}^{\mathbb{S}}$, specifying the sorts of both the domain and range of f. Each predicate symbol B also has an associated arity and sort: $sort(B)$ for an m-ary predicate symbol is an m-tuple $< \sigma_1, \ldots, \sigma_m >$ of sorts in $\mathbf{L}^{\mathbb{S}}$. Constant symbols (denoted c, c_1 etc.) are identified as the 0-ary function symbols, with each constant symbol c associated with a sort, denoted $sort(c)$, in $\mathbf{L}^{\mathbb{S}}$. The vocabulary **L** also explicitly

includes the distinguished equality predicate symbol $=$, used for comparing elements of the same sort.

Syntax of **L**-*terms and* **L**-*atoms*: Given any set of variables $V \subseteq \mathbf{L}^{\mathbb{V}}$, we inductively construct the set of **L**-terms and **L**-atoms over V, using sorted symbols, as follows:

- Every variable of sort σ is a term of sort σ.

- If f is a function symbol of sort $< \sigma_1, \ldots, \sigma_m, \sigma >$, and t_j is a term of sort σ_j for $j \in [1, m]$, then $f(t_1, \ldots, t_m)$ is a term of sort σ. In particular, every constant of sort σ is a term of sort σ.

- If B is a predicate symbol of sort $< \sigma_1, \ldots, \sigma_m >$, and t_j is a term of sort σ_j for $j \in [1, m]$, then $B(t_1, \ldots, t_m)$ is an atom.

- If t_1, t_2 are terms of the same sort, $t_1 = t_2$ is an atom.

Semantics of **L**-*terms and* **L**-*atoms*: Given any set of variables $V \subseteq \mathbf{L}^{\mathbb{V}}$, an *interpretation I* of symbols of **L**, and **L**-terms and **L**-atoms over V is a map satisfying the following:

- Every sort $\sigma \in \mathbf{L}^{\mathbb{S}}$ is mapped to a nonempty domain D_σ. In particular, the sort `bool` is mapped to the Boolean domain $D^{\mathtt{bool}} : \{\mathtt{T}, \mathtt{F}\}$, and the sort `location` is mapped to a domain of *control locations* in a program.

- Every variable symbol v of sort σ is mapped to an element v^I in D_σ.

- Every function symbol f, of sort $< \sigma_1, \ldots, \sigma_m, \sigma >$ is mapped to a function $f^I : D_{\sigma_1} \times \ldots D_{\sigma_m} \to D_\sigma$. In particular, every constant symbol c of sort σ is mapped to an element $c^I \in D_\sigma$.

- Every predicate symbol B of sort $< \sigma_1 \ldots \sigma_m >$ is mapped to a function $D_{\sigma_1} \times \ldots D_{\sigma_m} \to D^{\mathtt{bool}}$.

Given an interpretation I as defined above, the valuation $val^I[t]$ of an **L**-term t and the valuation $val^I[G]$ of an **L**-atom G are defined as follows:

- For a term t which is a variable v, the valuation is v^I.

- For a term $f(t_1, \ldots, t_m)$, the valuation $val^I[f(t_1, \ldots, t_m)] = f^I(val^I[t_1], \ldots, val^I[t_m])$.

- For an atom $G(t_1, \ldots, t_m)$, the valuation $val^I[G(t_1, \ldots, t_m)] = \mathtt{T}$ iff $G^I(val^I[t_1], \ldots, val^I[t_m]) = \mathtt{T}$.

- For an atom $t_1 = t_2$, $val^I[t_1 = t_2] = \mathtt{T}$ iff $val^I[t_1] = val^I[t_2]$.

In the rest of the paper, we assume that the interpretation of constant, function and predicate symbols in **L** is known and fixed. We further assume that the interpretation of sort symbols to specific domains is known and fixed. With some abuse of notation, we shall denote the interpretation of all constant, function and predicate symbols simply by the symbol name, and identify sorts with their domains. Examples of some constant, function and predicate symbols that may be included in **L** are: constant symbols $0, 1, 2$, function symbols $+, -$, and predicate symbols $<, >$ over the integers, function symbols $\vee, \neg$ over `bool`, the constant symbol φ (empty list), function symbol $\bullet$ (appending lists) and predicate symbol *null* (emptiness test) over lists, etc.. Finally, when the interpretation is obvious from the context, we denote the valuations $val^I[t]$, $val^I[G]$ of terms t and atoms G simply as $val[t]$, $val[G]$, respectively.

2.2   Concurrent Programs

In our framework, we consider a (shared-memory) concurrent program to be an asynchronous composition of a non-empty, finite set of processes, equipped with a finite set of program variables that range over finite domains. We assume a simple concurrent programming language with assignment, condition test, unconditional goto, sequential and parallel composition, and the synchronization primitive - conditional critical region (CCR) [12, 10]. A concurrent program P is written using the concurrent programming language, in conjunction with $\mathbf{L}$-terms and $\mathbf{L}$-atoms. We assume that the sets of (data and control) variables, functions and predicates available for writing P are each finite subsets of $\mathbf{L}^{\mathbb{V}}$, $\mathbf{L}^{\mathbb{F}}$ and $\mathbf{L}^{\mathbb{B}}$, respectively.

A concurrent program is given as $P :: [\texttt{declaration}]\,[P_1 \| \ldots \| P_k]$, with $k > 0$. The declaration consists of a finite sequence of declaration statements, specifying the set of shared data variables X, their domains, and possibly initializing them to specific values. For example, the declaration statement, $v_1, v_2 : \{0, 1, 2, 3\}$ with $v_1 = 0$, declares two variables v_1, v_2, each with (a finite integer) domain $\{0, 1, 2, 3\}$, and initializes the variable v_1 to the value 0. The initial value of any uninitialized variable is assumed to be a user/environment input from the domain of the variable.

A process P_i consists of a declaration of local data variables Y_i (similar to the declaration of shared data variables in P), and a finite sequence of labeled, *atomic* instructions, $l : inst$. We denote the unique instruction at location l as $inst(l)$. The set of data variables Var_i accessible by P_i is given by $X \cup Y_i$. The set of labels or *locations* of P_i is denoted $L_i = \{l_i^0, \ldots, l_i^{n_i}\}$, with l_i^0 being a designated start location. Unless specified otherwise[1], an atomic instruction $inst$ is an assignment, condition test, unconditional goto, or CCR. An assignment instruction A, given by $(v_{i_1}, \ldots, v_{i_q}) := (t_1, \ldots, t_q)$, is a parallel assignment of $\mathbf{L}$-terms $t_1, \ldots, t_q$, over Var_i, to the data variables $v_{i_1}, \ldots, v_{i_q}$ in Var_i. Upon completion, an assignment statement at l_i^r transfers control to the next location l_i^{r+1}. A condition test, if $(G)\ l_{if}, l_{else}$, consists of an $\mathbf{L}$-atom G over Var_i, and a pair of locations l_{if}, l_{else} in L_i to transfer control to if G evaluates to $\mathtt{T}$, $\mathtt{F}$, respectively. The instruction goto l is a transfer of control to location $l \in L_i$. A CCR is a guarded insruction block, $G \rightarrow inst\_block$, where the enabling guard G is an $\mathbf{L}$-atom over Var_i and $inst\_block$ is a sequence of assignment, conditional and goto statements. The guard G is evaluated atomically and if found to be $\mathtt{T}$, the corresponding $inst\_block$ is executed atomically, and control is transferred to the next location. If G is found to be $\mathtt{F}$, the process *waits* at the same location till G evaluates to $\mathtt{T}$. An unsynchronized process does not contain CCRs.

We model the asynchronous composition of concurrent processes by the nondeterministic interleaving of their atomic instructions. Hence, at each step of the computation, some process, with an enabled transition, is nondeterministically selected to be executed next by a scheduler. The set of program variables is denoted $V = Loc \cup Var$, where $Loc = \{loc_1, \ldots, loc_k\}$ is the set of control variables and $Var = Var_1 \cup \ldots \cup Var_k$ is the set of data variables. The semantics of the concurrent program P is given by a transition system (S, S^0, R), where S is a set of states, $S_0 \subseteq S$ is a set of initial states and $R \subseteq S \times S$ is the transition relation. Each state $s \in S$ is a valuation of the program variables in V. We denote the value of variable v in state s as $val^s[v]$, and the corresponding value of a term t and an atom G in state s as $val^s[t]$ and $val^s[G]$, respectively. $val^s[t]$ and $val^s[G]$ are defined inductively as in Sec. 2.1. The domain of each control variable $loc_i \in V$ is the set of locations L_i, and the domain of each data variable is determined from its declaration. The set of initial states S_0 corresponds to all states s with $val^s[loc_i] = l_i^0$ for all $i \in [1, k]$, and $val^s[v] = v_{init}$, for every data variable v initialized in its declaration to some constant v_{init}. There exists a transition from state s to s' in R, with $val^s[loc_i] = l_i$, $val^{s'}[loc_i] = l_i'$ and $val^{s'}[loc_j] = val^s[loc_j]$ for all $j \neq i$, iff there exists a corresponding *local move* in process P_i involving instruction $inst(l_i)$, such

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[1]A user may define an atomic instruction (block) as a sequence of assignment, conditional and goto statements

that:

1. $inst(l_i)$ is the assignment instruction: $(v_{i_1},\ldots,v_{i_q}) := (t_1,\ldots,t_q)$, for each variable v_{i_j} with $j \in [1,q]$: $val^{s'}[v_{i_j}] = val^s[t_j]$, for all other data variables v: $val^{s'}[v] = val^s[v]$, and l'_i is the next location in P_i after l_i, or,

2. $inst(l_i)$ is the condition test: $\mathtt{if}\ (G)\ l_{if}, l_{else}$, the valuation of all data variables in s' is the same as that in s, and either $val^s[G]$ is $\mathtt{T}$ and $l'_i = l_{if}$, or $val^s[G]$ is $\mathtt{F}$ and $l'_i = l_{else}$, or,

3. $inst(l_i)$ is $\mathtt{goto}\ l$, the valuation of all data variables in s' is the same as that in s, and $l'_i = l$, or,

4. $inst(l_i)$ is the CCR $G \to inst\_block$, $val^s[G]$ is $\mathtt{T}$, the valuation of all data variables in s' correspond to the atomic execution of $inst\_block$ from state s, and l'_i is the next location in P_i after l_i.

We assume that R is total. For terminating processes P_i, we assume that P_i ends with a special instruction, $halt : \mathtt{goto}\ halt$.

2.3 Specifications

Our specification language, **LCTL**, is an extension of propositonal CTL, with formulas composed from **L**-atoms. While one can use propositional CTL for specifying properties of finite-state programs, **LCTL** enables more natural specification of properties of concurrent programs communicating via typed shared variables. We describe the syntax and semantics of this language below.

Syntax: Given a set of variables $V \subseteq \mathbf{L}^{\mathbb{V}}$, we inductively construct the set of (**LCTL**) *formulas* over V, using **L**-atoms, in conjunction with the propositional operators $\neg, \vee$ and the temporal operators $\mathsf{A}, \mathsf{E}, \mathsf{X}, \mathsf{U}$, along with the process-indexed next-time operator X_i:

- Every **L**-atom over V is a formula.
- If ϕ_1, ϕ_2 are formulas, then so are $\neg\phi_1$ and $\phi_1 \vee \phi_2$.
- If ϕ_1, ϕ_2 are formulas, then so are $\mathsf{EX}\,\phi_1$, $\mathsf{EX}_i\,\phi_1$, $\mathsf{A}[\phi_1\,\mathsf{U}\,\phi_2]$ and $\mathsf{E}[\phi_1\,\mathsf{U}\,\phi_2]$.

We use the following standard abbreviations: $\phi_1 \wedge \phi_2$ for $\neg(\neg\phi_1 \vee \neg\phi_2)$, $\phi_1 \to \phi_2$ for $\neg\phi_1 \vee \phi_2$, $\phi_1 \leftrightarrow \phi_2$ for $(\phi_1 \to \phi_2) \wedge (\phi_2 \to \phi_1)$, $\mathsf{AX}\,\phi$ for $\neg\mathsf{EX}\,\neg\phi$, $\mathsf{AX}_i\,\phi$ for $\neg\mathsf{EX}_i\,\neg\phi$, $\mathsf{AF}\,\phi$ for $\mathsf{A}[\mathsf{T}\,\mathsf{U}\,\phi]$, $\mathsf{EF}\,\phi$ for $\mathsf{E}[\mathsf{T}\,\mathsf{U}\,\phi]$, $\mathsf{EG}\,\phi$ for $\neg\mathsf{AF}\,\neg\phi$, and $\mathsf{AG}\,\phi$ for $\neg\mathsf{EF}\,\neg\phi$.

Semantics: **LCTL** formulas over a set of variables V are interpreted over models of the form $M = (S, R, L)$, where S is a set of states and R is a a total, multi-process, binary relation $R = \cup_i R_i$ over S, composed of the transitions R_i of each process P_i. L is a labeling function that assigns to each state $s \in S$ a valuation of all variables in V. The value of a term t in a state $s \in S$ of M is denoted as $val^{(M,s)}[t]$, and is defined inductively as in Sec. 2.1. A path in M is a sequence $\pi = (s_0, s_1, \ldots)$ of states such that $(s_j, s_{j+1}) \in R$, for all $j \geq 0$. We denote the jth state in π as π_j.

The satisfiability of a **LCTL** formula in a state s of M can be defined as follows:

- $M, s \models G(t_1, \ldots, t_m)$ iff $G(val^{(M,s)}[t_1], \ldots, val^{(M,s)}[t_m]) = \mathtt{T}$.
- $M, s \models t_1 = t_2$ iff $val^{(M,s)}[t_1] = val^{(M,s)}[t_2]$.
- $M, s \models \neg\phi$ iff it is not the case that $M, s \models \phi$.
- $M, s \models \phi_1 \vee \phi_2$ iff $M, s \models \phi_1$ or $M, s \models \phi_2$.
- $M, s \models EX\,\phi$ iff for some s_1 such that $(s, s_1) \in R$, $M, s_1 \models \phi$.

- $M, s \models EX_i \phi$ iff for some s_1 such that $(s, s_1) \in R_i$, $M, s_1 \models \phi$.

- $M, s \models A[\phi_1 U \phi_2]$ iff for all paths π starting at s, $\exists j [M, \pi_j \models \phi_2$ and $\forall k (k < j \to M, \pi_k \models \phi_1)]$.

- $M, s \models E[\phi_1 U \phi_2]$ iff there exists a path π starting at s such that $\exists j [M, \pi_j \models \phi_2$ and $\forall k (k < j \to M, \pi_k \models \phi_1)]$.

Programs as Models: A program $P = (S, S^0, R)$ can be viewed as a model $M = (S, R, L)$, with the same set of states and transitions as P, and the identity labeling function L that maps a state to itself. Given an **L**CTL specification ϕ, we say $P \models \phi$ iff for each state $s \in S^0$, $M, s \models \phi$.

3   Basic Algorithmic Framework

In this section, for ease of exposition, we assume a simpler program model than the one described in Sec. 2.2. We restrict the number of concurrent processes k to 2. We assume that *all* data variables are initialized in the program to specific values from their respective domains. We further assume that all program variables, including control variables, are shared variables. We explain our basic algorithmic framework with these assumptions, and later describe extensions to handle the general program model in Sec. 4.

Let us first review our problem definition. Given a concurrent program P, composed of unsynchronized processes P_1, P_2, and an **L**CTL specification ϕ_{spec} of their desired global concurrent behaviour, we wish to automatically generate synchronized processes P_1^s, P_2^s, such that the resulting concurrent program $P^s \models \phi_{spec}$. If P_1, P_2 consist of atomic instructions, we wish to obtain synchronization in the form of CCRs, with each instruction enclosed in a CCR. In particular, the goal is to synthesize the guard for each CCR, along with any necessary (synchronization) assignments to be performed within the CCR.

We propose an automated framework to do this in several steps.

1. Formulate an **L**CTL formula ϕ_P to specify the semantics of the concurrent program P.

2. Construct a tableau T_ϕ for the formula ϕ given by $\phi_P \wedge \phi_{spec}$. If T_ϕ is empty, declare specification as inconsistent and halt.

3. If T_ϕ is non-empty, extract a model M for ϕ from it.

4. Decompose M to obtain CCRs to synchronize each process.

In what follows, we describe these steps in more detail.

3.1   Formulation of ϕ_P

A reader familiar with the early synthesis work in [7] will recall that the synthesis of a global model requires a complete specification, which includes a temporal description ϕ_P of the concurrency and operational semantics of the unsynchronized concurrent program P, along with its desired global behaviour ϕ_{spec}. We propose to automatically infer an **L**CTL formula for ϕ_P to help mitigate the user's burden of specification-writing. Let $Var = \{v_1, \ldots, v_h\}$ be the set of data variables. $\{\phi_P$ is then formulated as the conjunction of the following (classes of) properties:

1. Initial condition:
   $val[loc_1] = l_1^0 \wedge val[loc_2] = l_2^0 \wedge \bigwedge_{v \in Var} val[v] = v_{init}$.

2. At any step, only one process can make a (local) move:
$$\text{AG} \bigwedge_{j=1}^{j=n_1} ((val[loc_1] = l_1^j) \Rightarrow \text{AX}_2 (val[loc_1] = l_1^j)) \quad \wedge$$
$$\text{AG} \bigwedge_{j=1}^{j=n_2} ((val[loc_2] = l_2^j) \Rightarrow \text{AX}_1 (val[loc_2] = l_2^j)).$$

3. Some process can always make a (local) move:
$$\text{AG}(\text{EX}_1 \, \text{T} \vee \text{EX}_2 \, \text{T}).$$

4. A statement $l_i^r : \{v_{i1}, \ldots, v_{iq}\} := \{t_1, \ldots, t_q\}$ in P_i is formulated as:
$$\text{AG}(((val[loc_i] = l_i^r) \wedge \bigwedge_{j=1}^{j=h} val[v_j] = \upsilon_j) \Rightarrow$$
$$\text{AX}_i ((val[loc_i] = l_i^{r+1}) \wedge \bigwedge_{j=1}^{j=q} val[v_{ij}] = val[t_j] \wedge \bigwedge_{v_j \in Var \setminus \{v_{i1}, \ldots, v_{iq}\}} val[v_j] = \upsilon_j)).$$

5. A statement $l_i : \texttt{if} \ (G) \ l_{if}, l_{else}$ in P_i is formulated as:
$$\text{AG}(((val[loc_i] = l_i) \wedge (val[G] = \text{T})) \Rightarrow \text{AX}_i (val[loc_i] = l_{if})) \wedge$$
$$\text{AG}(((val[loc_i] = l_i) \wedge (val[G] = \text{F})) \Rightarrow \text{AX}_i (val[loc_i] = l_{else})).$$

6. A statement $l_i : \texttt{goto} \ l$ in P_i is formulated as:
$$\text{AG}((val[loc_i] = l_i) \Rightarrow \text{AX}_i (val[loc_i] = l))$$

3.2 Construction of T_ϕ

We assume the ability to evaluate **L**-atoms and **L**-terms over the set V of program variables. Note that since we restrict ourselves to a finite subset of the symbols in **L**, this is a reasonable assumption. Let us further assume that the formula $\phi = \phi_P \wedge \phi_{spec}$ is in a form in which only atoms appear negated.

An *elementary* formula of **LCTL** is an atom, negation of an atom or the formulas beginning with AX_i or EX_i (we do not explicitly consider formulas beginning with AX or EX since $\text{AX} \, \psi = \bigwedge_i \text{AX}_i \, \psi$, and $\text{EX} \, \psi = \bigvee_i \text{EX}_i \, \psi$. All other formulas are nonelementary. Every nonelementary formula is either a conjunctive formula $\alpha \equiv \alpha_1 \wedge \alpha_2$ or a disjunctive formula $\beta \equiv \beta_1 \vee \beta_2$. For example, $\psi_1 \wedge \psi_2$, $\text{AG}(\psi) = \psi \wedge \text{AXAG} \, \psi$ are α formulas, and $\psi_1 \vee \psi_2$, $\text{AF}(\psi) = \psi \vee \text{AXAF} \, \psi$ are β formulas.

The tableau T_ϕ for the formula ϕ is a finite, rooted, directed AND/OR graph with nodes labeled with formulas such that when a node B is viewed as a state in a suitable structure, $B \models \psi$ for all formulas $\psi \in B$. The construction for T_ϕ is similar to the tableau-construction for propositional CTL in [7], while accounting for the presence of **L**-atoms over V in the nodes of T_ϕ. Besides composite **L**-atoms and **LCTL** formulas, each node of T_ϕ is labeled with simple atoms of the type $loc = l$ and $v = \upsilon$ identifying the values of the control and data variables in each node. Two OR-nodes B_1 and B_2 are identified as being equivalent if B_1, B_2 are labeled with the same simple atoms, and the conjunction of all the formulas in B_1 is valid iff the conjunction of all the formulas in B_2 is valid. Equivalence of AND-nodes can be similarly defined. We briefly summarize the tableau construction first, before explaining the individual steps in more detail.

1. Initially, let the root node of T_ϕ be an OR-node labeled with ϕ.

2. If all nodes in T_ϕ have successors, go to the next step. Otherwise, pick a node B without successors. Create appropriately labeled successors of B such that: if B is an OR-node, the formulas in B are valid iff the formulas in some (AND-) successor node are valid, and if B is an AND-node, the formulas in B are valid iff the formulas in all (OR-) successor nodes are valid. Merge all equivalent AND-nodes and equivalent OR-nodes. Repeat this step.

3. Delete all *inconsistent* nodes in the tableau from the previous step to obtain the final T_ϕ.

Successors of OR-nodes: To construct the set of AND-node successors of an OR-node B, first build a temporary tree with labeled nodes rooted at B, repeating the following step until all leaf nodes are only labeled with elementary formulas. For any leaf node C labeled with a non-elementary formula ψ: if ψ is an α formula, add a single child node, labeled $C \setminus \{\psi\} \cup \{\alpha_1, \alpha_2\}$, to C, and if ψ is a β formula, add two child nodes, labeled $C \setminus \{\psi\} \cup \{\beta_1\}$ and $C \setminus \{\psi\} \cup \{\beta_2\}$, to C. Once the temporary tree is built, create an AND-node successor D for B, corresponding to each leaf node in the tree, labeled with the set of all formulas appearing in the path to the leaf node from the root of the tree. If there exists an atom of the form $v = t$ in D, where t is an **L**-term, and the valuation of t in D is υ, replace the atom $v = t$ by the simple atom $v = \upsilon$.

Successors of AND-nodes: To construct the set of OR-node successors of an AND-node B, create an OR-node labeled with $\{\psi\}$ for each $EX_i \psi$ formula in B and label the transition to the OR-node with i. Furthermore, label each such OR-node D (with an i-labeled transition into D) with $\bigcup_j \psi_j$ for each $AX_i \psi_j$ formula in B. If there exists an atom of the form $v = t$ in D, where t is an **L**-term, and the valuation of t in D is υ, replace the atom $v = t$ by the simple atom $v = \upsilon$. Note that the requirement that some process can always move ensures that there will be some successor for every AND-node.

Deletion rules: All nodes in the tableau that do not meet all criteria for a tableau for ϕ are identified as inconsistent and deleted as follows:

1. Delete any node B which is internally inconsistent, i.e., the conjunction of all non-temporal elementary formulas in B evaluates to F.

2. Delete any node all of whose original successors have been deleted.

3. Delete any node B such that $E[\psi_1 U \psi_2] \in B$, and there does not exist some path to an AND-node D from B with $\psi_2 \in D$, and $\psi_1 \in C$ for all AND-nodes C in the path.

4. Delete any node B such that $A[\psi_1 U \psi_2] \in B$, and there does not exist a full sub-DAG [2] such that for all its frontier nodes D, $\psi_2 \in D$ and for all its non-frontier nodes C, $\psi_1 \in C$.

   If the root node of the tableau is deleted, we halt and declare the specification ϕ as inconsistent (unsatisfiable). If not, we proceed to the next step.

3.3   Obtaining a model M from T_ϕ

A model M is obtained by joining together model fragments rooted at AND-nodes of T_ϕ: each model fragment is a rooted DAG of AND-nodes embeddable in T_ϕ such that all eventuality formulas labeling the root node are fulfilled in the fragment. We do not explain this step in more detail, as it is identical to the procedure in [7] [3]. After extracting M from T_ϕ, we modify the labels of the states of M by eliminating all labels other than simple atoms, identifying the values of the program variables in each state of M. If there exist n states $s_1, \ldots, s_n$ with the exact same labels after this step, we introduce an auxiliary variable

---

[2]A full sub-DAG T' is a directed acyclic sub-graph of a tableau T, rooted at a node of T such that all OR-nodes in T' have exactly one (AND-node) successor from T in T', and all AND-nodes in T' either have no successors in T', or, have all their (OR-node) successors from T in T'.

[3]There may be multiple models embedded in T_ϕ. In [7], in order to construct model fragments, whenever there are multiple sub-DAGs rooted at an OR-node B that fulfill the eventualities labeling B, one of minimal size is chosen, where size of a sub-DAG is defined as the length of its longest path. There are other valid criteria for choosing models, exploring which is beyond the scope of this paper.

x with domain $\{0,1,2,\ldots,n\}$ to distinguish between the states: x is assumed to be 0 in all states other than $s_1,\ldots,s_n$; for each $j \in \{1,\ldots,n\}$, we set x to j in transitions into s_j, and set x back to 0 in transitions out of s_j. This completes the model generation. M is guaranteed to satisfy ϕ by construction.

3.4   Decomposition of M into P_1^s and P_2^s

Recall that P_1 and P_2 are unsynchronized processes with atomic instructions such as assignments, condition tests and gotos, and no CCRs. In this last step of our basic algorithmic framework, we generate P_1^s and P_2^s consisting of CCRs, enclosing each atomic instruction of P_1 and P_2.

Without loss of generality, consider location l_1 in P_1. The guard for the CCR for $inst(l_1)$ in P_1^s corresponds to all states in M in which $inst(l_1)$ is *enabled*, i.e., states in which P_1 is at location l_1 and from which there exists a P_1 transition. To be precise, $inst(l_1)$ is enabled in state s in M iff there exists a transition $(s,s') \in R$ such that $val^s[loc_1] = l_1$, $val^{s'}[loc_2] = l_1'$ with l_1' being a valid next location for P_1, and, $val^s[loc_2] = val^{s'}[loc_2]$. The guard G_s corresponding to such a state s is the valuation of all program variables other than loc_1 in state s. Thus, if $val^s[loc_2] = l_2$ and for all $v_j \in Var = \{v_1,\ldots,v_h\}$, $val^s[v_j] = \upsilon_j$, then G_s is given by $(loc_2 = l_2) \wedge \bigwedge_{j=1}^{j=h} v_j = \upsilon_j$.

If M does not contain an auxiliary variable, then the CCR for $inst(l_1)$ in P_1^s is simply $G_{1,1} \rightarrow inst(l_1)$, where $G_{1,1}$ is the disjunction of guards G_s corresponding to all states s in M in which $inst(l_1)$ is enabled. However, if M contains an auxiliary variable x (with domain $\{0,1,2,\ldots,n\}$), then one may also need to perform updates to x within the CCR instruction block. In particular, if $inst(l_1)$ is enabled on state s in M, transition (s,s') in M is a P_1 transition, and if there is an assignment $x := j$ for some $j \in \{0,\ldots,n\}$ along transition (s,s'), then besides $inst(l_1)$, the instruction block of the CCR for $inst(l_1)$ in P_1^s includes instructions in our programming language corresponding to: `if` G_s $x := j$.

The synchronized process P_1^s (and similarly P_2^s) can be generated by inserting a similarly generated CCR at each location in P_1 (and P_2). The modified concurrent program P_s is given by $P_s ::$ `[declaration]` $[P_1^s \| P_2^s]$, where the declaration includes auxiliary variable x with domain $\{0,1,2,\ldots,n\}$ if M contains x with domain $\{0,1,2,\ldots,n\}$.

3.5   Correctness and Complexity

The following theorems assert the correctness of our basic algorithmic framework for synthesizing synchronization for unsynchronized processes P_1, P_2, as defined in Sec. 2.2, with the restriction that all program variables are shared variables that are initialized to specific values.

Theorem 1 *Given unsynchronized processes P_1, P_2 and an* **LCTL** *formula ϕ_{spec}, if our basic algorithm generates P^s, then $P^s \models \phi_{spec}$.*

Theorem 2 *Given unsynchronized processes P_1, P_2, and an* **LCTL** *formula ϕ_{spec}, if the temporal specification $\phi = \phi_{spec} \wedge \phi_P$ is consistent as a whole, then our method constructs P^s such that $P^s \models \phi_{spec}$.*

The complexity of our method is exponential in the size of ϕ, i.e., exponential in the size of ϕ_{spec} and the number of program variables V.

4   Extensions

In this section, we demonstrate the adaptability of our basic algorithmic framework by considering more general program models. In particular, we discuss extensions for synthesizing correct synchronization in

the presence of uninitialized variables and local variables. Furthermore, we extend our framework to programming languages with locks and `wait`/`signal` over condition variables by presenting an automatic compilation of CCRs into synchronization code based on these lower-level synchronization primitives. We conclude with an extension of the framework to multiple processes.

4.1   Uninitialized Variables

In Sec. 3, we assumed that all data variables are initialized to specific values over their domains. This assumption may not be satisfied in general as it disallows any kind of user or environment input to a concurrent program. In the program model presented in Sec. 2, only some (or even none) of the data variables may be initialized to specific values within the program. This is a more realistic setting, which allows a user or environment to choose the initial values of the remaining data variables. In this subsection, we present a simple, brute-force extension of our basic algorithm for synthesizing synchronization in the presence of uninitialized variables.

The formula ϕ_P, expressing the concurrency and operational semantics of P, remains the same, except for the initial condition. Instead of a single initial state, the initial condition in ϕ_P specifies the set of all possible initial states, with the control and initialized data variables set to their initial values, and the remaining data variables ranging over all possible values in their respective domains. Let us denote by Var_{inp} this remaining set of data variables, that are, essentially, inputs to the program P. The set of program-initialized data variables is then $Var \setminus Var_{inp}$. The initial condition in ϕ_P is expressed as:

$$\bigwedge_i val[loc_i] = l_i^0 \ \wedge \ \bigwedge_{v \in Var \setminus Var_{inp}} (v = v_{init}) \ \wedge \ \bigwedge_{v \in Var_{inp}} \bigvee_{v_j \in D_v} (v = v_j),$$

where D_v is the domain of v.

The root node of the tableau T_ϕ is now an AND-node with multiple OR-node successors, each corresponding to a particular valuation υ of all the data variables (the values of the control variable and initialized data variables are the same in any such valuation). Each such OR-node yields a model M_υ for the formula ϕ, and a corresponding decomposition of M_υ into synchronized processes $P_{1_\upsilon}^s$ and $P_{2_\upsilon}^s$.

To generate synchronized processes P_1^s and P_2^s such that for all possible initial valuations υ of the data variables, $P^s \models \phi_{spec}$, we propose to *unify* the CCRs corresponding to each valuation υ as follows:

1. Introduce a new variable $v0$ for every input data variable v in Var_{inp}. Declare $v0$ as a variable with the same domain as v. Assign $v0$ the input value of v.

2. Replace every CCR guard G in $P_{i_\upsilon}^s$ with the guard G_υ given by $\bigwedge_{v \in Var_{inp}} (v0 = v_\upsilon) \wedge G$, where the valuation of v in υ is v_υ. Similarly, update every conditional guard accompanying an auxiliary variable assignment within a CCR instruction block in $P_{i_\upsilon}^s$.

3. The unified guard for each CCR in P_1^s and P_2^s is given by the disjunction of the corresponding guards G_υ in all $P_{1_\upsilon}^s$ and $P_{2_\upsilon}^s$. The unified conditional guards for auxiliary variable updates in the CCR instruction blocks are computed similarly.

Note that the unified guards inferred above, as well as in Sec. 3.4, may not in general be *pleasant*. However, since each guard is expected to an **L**-term over a finite set of variable, function and predicate symbols with known interpretations, it is possible to obtain a simplified **L**-term with the same value as the guard. This translation is beyond the scope of this paper, but we refer the reader to [14] for a similar approach.

4.2 Local Variables

Another assumption in Sec. 3 was that all program variables, including control variables, were shared variables. Since one typically associates a cost with each shared variable access, it is impractical to expect all program variables to be shared variables. This is especially true of control variables, which are generally never declared explicitly or accessed in programs. Thus, the guards inferred in Sec. 3.4, ranging over locations of the other process, are somewhat irregular. Indeed, any guard for a process P_i must only be defined over the data variables Var_i accessible by P_i. In what follows, we discuss various solutions to address this issue.

Let us assume that we have a model $M = (S, R, L)$ for ϕ, with states labeled by the valuations of the control variables Loc, the shared data variables X, the local data variables $Y = \bigcup_i Y_i$, and possibly an auxiliary variable x. For the purpose of this subsection, let x be included in the set X. We first check if the set of states S of M has the property that for any two states s_1, s_2 in S: $[\bigwedge_{loc \in Loc} val^{s_1}[loc] = val^{s_2}[loc] \wedge \bigwedge_{y \in Y} val^{s_1}[y] = val^{s_2}[y]] \Leftrightarrow \bigwedge_{x \in X} val^{s_1}[x] = val^{s_2}[x]$. If this is true, then each state $s \in S$ is uniquely identified by its valuation of the shared data variables X. We can then simply factor out guards from M for each process that only range over X, without missing out on any permitted behaviour in M. If this is not true, we can perform other similar checks. For instance, we can check if for a particular i: any two states in S match in their valuations of the variables $\{loc_i\} \cup Y_i \cup X$ iff they match in their valuations of the other program variables. If this is true, then the process P_i can distinguish between states in S by the valuations of its variables $Var_i \cup \{loc_i\}$. Thus, we can infer guards for P_i, that are equivalent to the guards inferred in Sec. 3.4, but only range over Var_i.

In general, however, there will be states s_1, s_2 in S which cannot be distinguished by the valuations of a particular process's, or worse, by any process's variables. This general situation presents us with a trade-off between synchronization cost and concurrency: we can introduce additional shared variables to distinguish between such states, thereby increasing the synchronization cost and allowing more behaviours of M to be preserved in P^s, or, we can resign to *limited observability* [24] of global states, resulting in lower synchronization cost and fewer permitted behaviours of M. In particular, for the latter case, we implement a safe subset of the behaviours of M by inferring synchronization guards corresponding to the negation of variable valuations (states) that are not present in M. Since a global state $u \notin M$ may be indistinguishable over some Var_i from a state $s \in M$, when eliminating behaviours rooted at u, we also eliminate all (good) behaviours of M, rooted at s. We refer the reader to [24] for a detailed treatment of this trade-off.

4.3 Synchronization using Locks and Condition Variables

While CCRs provide an elegant high-level synchronization solution, many programming languages prefer and only provide lower-level synchronization primitives such as locks for mutual exclusion, and `wait/signal` over condition variables for condition synchronization. In what follows, we present an automatic compilation of the CCRs inferred in Sec. 3.4 for P_1^s, P_2^s into both coarse-grained and fine-grained synchronization code based on these lower-level primitives. The resulting processes are denoted as P_1^c, P_2^c (coarse-grained) and P_1^f, P_2^f (fine-grained).

In both cases, we declare locks and conditions variables for synchronization. For the program P^c, which has a coarser level of lock granularity, we declare a single lock l for controlling access to shared variables and condition variables. For the program $P_1^f \parallel P_2^f$ with a finer level of lock granularity, we declare separate locks l_v, l_x for controlling access to each shared data variable $v \in X$ and the shared auxiliary variable x, respectively. We further define a separate lock $l_{cv_{1,i}}$, $l_{cv_{2,j}}$ for each condition variable
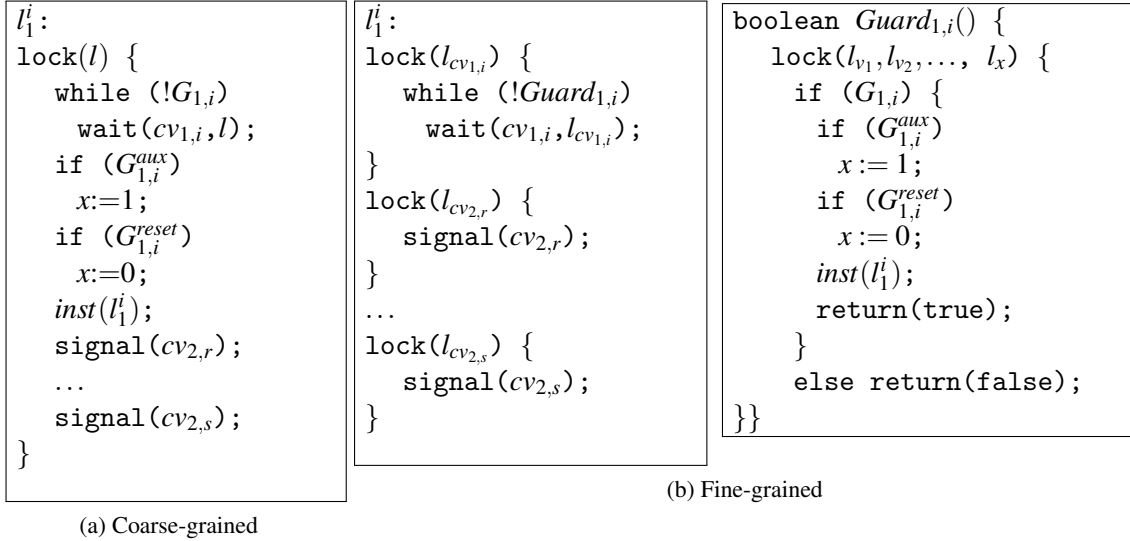
```
lⁱ₁:
lock(l) {
   while (!G₁,ᵢ)
     wait(cv₁,ᵢ,l);
   if (G₁,ᵢᵃᵘˣ)
     x:=1;
   if (G₁,ᵢʳᵉˢᵉᵗ)
     x:=0;
   inst(lⁱ₁);
   signal(cv₂,ᵣ);
   ...
   signal(cv₂,ₛ);
}
```

```
lⁱ₁:
lock(l_cv₁,ᵢ) {
   while (!Guard₁,ᵢ)
     wait(cv₁,ᵢ,l_cv₁,ᵢ);
}
lock(l_cv₂,ᵣ) {
   signal(cv₂,ᵣ);
}
...
lock(l_cv₂,ₛ) {
   signal(cv₂,ₛ);
}
```

```
boolean Guard₁,ᵢ() {
   lock(l_v₁,l_v₂,..., l_x) {
     if (G₁,ᵢ) {
       if (G₁,ᵢᵃᵘˣ)
         x:=1;
       if (G₁,ᵢʳᵉˢᵉᵗ)
         x:=0;
       inst(lⁱ₁);
       return(true);
     }
     else return(false);
}}
```

(a) Coarse-grained   (b) Fine-grained

Figure 1: Coarse and fine-grained synchronization code corresponding to an example CCR at location l^i_1 of P_1. Guards $G^{aux}_{1,i}$, $G^{reset}_{1,i}$ above corresponds to all states in M on which $inst(l^i_1)$ is enabled, and there's an assignment $x{:=}1$, $x{:=}0$, respectively, along a P_1 transition out of the states.

$cv_{1,i}$, $cv_{2,j}$ to allow simultaneous processing of different condition variables.

We refer the reader to Fig. 1a for an example of coarse-grained synchronization code corresponding to the CCR at location l^i_1 of P_1. Note that, for ease of presentation, we have used conventional pseudocode, instead of our programming language. Further note that we find it convenient to express locks, as lock(l){...} (in a manner similar to Java's synchronized keyword), wherein l is a lock variable, '{' denotes *lock acquisition* and '}' denotes *lock release*. This simple implementation involves acquiring the lock l and checking if the overall guard $G_{1,i}$ for executing $inst(l^i_1)$ is enabled. While the guard is F, P^c_1 *waits* for it to change to T. This is implemented by associating a condition variable $cv_{1,i}$ with the overall guard $G_{1,i}$: P^c_1 releases the lock l and waits till P^c_2 *signals* it that $G_{1,i}$ could be T; P^c_1 then reacquires the lock and rechecks the guard. If the overall guard is T, P^1_c enters the instruction block of the CCR and executes the instructions while holding the lock l. Finally, P^c_1 sends a notification signal corresponding to every guard (i.e. condition variable) of P^c_2 which may be changed to T by P^c_1's shared variables updates, and releases the lock.

While fine-grained locking can typically be achieved by careful definition and nesting of multiple locks, one needs to be especially cautious in the presence of condition variables for various reasons. For instance, upon execution of wait(c,l) in a nested locking scheme, a process only releases the lock l before going to sleep, while still holding all outer locks. This can potentially lead to a deadlock. The fine-grained synchronization code in P^f_1, shown in Fig. 1b, circumvents these issues by utilizing a separate subroutine to evaluate the overall guard $G_{1,i}$. In this subroutine, P^f_1 first acquires all necessary locks, corresponding to all shared variables accessed in the subroutine. These locks are acquired in a strictly nested fashion and in a predecided fixed order to prevent deadlocks. We use lock($l_1,l_2,...$){...} to denote the nested locks lock(l_1){ lock(l_2){ ...}}, with l_1 being the outermost lock variable. The subroutine then evaluates $G_{1,i}$ and returns its value to the main body of P^f_1. If found T, the subroutine also executes the instruction block of the CCR. The synchronization code in the main body of P^f_1 acquires

the relevant lock $l_{cv_{1,i}}$ and calls its guard-computing subroutine within a `while` loop till it returns `T`, after which it releases the lock. If the subroutine returns `F`, the process releases $l_{cv_{1,i}}$ and waits on the associated condition variable $cv_{1,i}$. Each notification signal for a condition variable, on which the other process may be waiting, is sent out by acquiring the corresponding lock.

We emphasize certain optimizations implemented in our compilations that potentially improve the performance of the synthesized concurrent program: (a) declaration of condition variables only when necessary, and (b) sending notification signals only when some guard in the other process may have changed. We refer the reader to [8] for more details of this compilation.

4.4   Multiple ($k > 2$) Processes

Our basic algorithmic framework can be extended in a straight-forward manner to the synthesis of synchronization for concurrent programs with an arbitrary (but fixed) number k of processes. But since this involves building a global model M, with size exponential in k, it exhibits a state explosion problem. There has, however, been work [3, 2] on improving the scalability of the approach by avoiding building the entire global model, and instead composing interacting process pairs to generate synchronized processes. Hence, for $k > 2$ processes, we can adapt the more scalable synthesis algorithms to the synthesis of **L**CTL formulas.

The compilation of CCRs into coarse-grained and fine-grained synchronization code can be extended in a straight-forward manner to $k > 2$ processes. We emphasize that this compilation acts on individual processes directly, without construction or manipulation of the global model, and hence circumvents the state-explosion problem for arbitrary k.

5   Discussion

Related work: Early work on synthesis of synchronization for shared-memory concurrent programs from temporal specifications [7] utilized a tableau-based decision procedure for extracting synchronization skeletons from unsynchronized process skeletons. While the core technique has great potential, the original work had little practical impact due to its remoteness from realistic concurrent programs and programming languages. The limited modeling of shared-memory concurrency in this work did not include local and shared data variables, and hence, could not support semantic specifications over the values of program variables. There was no explicit treatment of process skeletons with branching, observability of program counters or local variables, and no attempt to synthesize synchronization based on lower-level synchronization primitives.

More recently, practically viable synthesis of synchronization has been proposed for both finite-state [24] and infinite-state concurrent programs [25]. However, in both [24], [25], the authors only handle safety specifications; in fact, it can be shown that synthesis methods that rely on pruning a global product graph ([13, 24, 25]) cannot, in general, work for liveness. Moreover, these papers do not support any kind of external environment; in particular, these papers do not account for different (environment-enabled) initializations of the program variables. Finally, similar to [7], these papers only synthesize high-level synchronization in the form in CCRs [24] and atomic sections [25], and do not attempt to synthesize synchronization based on lower-level synchronization primitives available in commonly used programming languages.

On the other end of the spectrum, there has been some important work on automatic synthesis of lower-level synchronization, in the form of memory fences, for concurrent programs running on relaxed

memory models [16, 15]. There has also been work on mapping high-level synchronization into lower-level synchronization [6, 26] - these papers do not treat liveness properties, are not fully algorithmic, and are verification-driven. Among papers that address refinement of locking granularity, are [4], which translates guarded commands, into synchronization based on atomic reads and atomic writes, and papers on compiler-based lock inference for atomic sections ([9], [5] etc.). The lock-inference papers [9], [5] rely on the availability of high-level synchronization in the form of atomic sections, and do not, in general, support condition synchronization. Sketching [22], a search-based program synthesis technique, is a verification-driven approach, which can be used to synthesize optimized implementations of synchronization primitives, e.g. barriers, from partial program sketches.

A note on reactive systems: A shared-memory concurrent program can also be viewed as a *reactive system*. A *reactive system* [11, 19] is described as one that maintains an ongoing interaction with an external environment or within its internal concurrent modules. Such systems cannot be adequately described by relational specifications over initial and final states - this distinguishes them from transformational or relational programs. An adequate description of a reactive system must refer to its ongoing desired behaviour, throughout its (possibly non-terminating) activity - temporal logic [18] has been recognized as convenient for this purpose.

A reactive system may be terminating or not, sequential or concurrent, and implemented on a monolithic or distributed architecture. A reactive system can also be open or closed [20, 21]. This has been a somewhat overlooked dichotomy in recent years. We have observed that it is not uncommon to view reactive systems exclusively as open systems; this is especially true in the context of synthesis. While the first algorithms on synthesis of concurrent programs [7, 17, 3] were proposed for closed reactive systems, the foundational work in [20, 21] set the stage for an extensive body of impressive results on synthesis of open reactive systems (see [23] for a survey).

We contend that the relatively simpler problem of synthesis of closed reactive systems is an important problem in its own right. This is especially true in the context of shared-memory concurrent programs, where it is sometimes sufficient and desirable to model programs as closed systems and force the component processes to cooperate with each other for achieving a common goal. If one must model an external environment, it is also often sufficient to model the environment in a restricted manner (as in this paper) or optimistically assume a helpful environment (see [1]).

Concluding Remarks: In this paper, we have presented a general tableau-based framework for the synthesis of synchronization for shared memory concurrent programs. While we have identified and explored initial solutions for issues such as environment-initialized variables, limited observability of local variables, pleasantness of guards, much work remains to be done. We also wish to extend the basic program model to handle nondeterministic programs, infinite-state programs as well as dynamic allocation of threads. Finally, we want to investigate techniques to reduce the overall complexity of the method.

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