

Congestion control methods: A, B, C and D

**Method A:**

- if  $Q(t) = Q^*$  then  $\lambda(t+1) \leftarrow \lambda(t)$
- if  $Q(t) < Q^*$  then  $\lambda(t+1) \leftarrow \lambda(t) + a$
- if  $Q(t) > Q^*$  then  $\lambda(t+1) \leftarrow \lambda(t) - a$

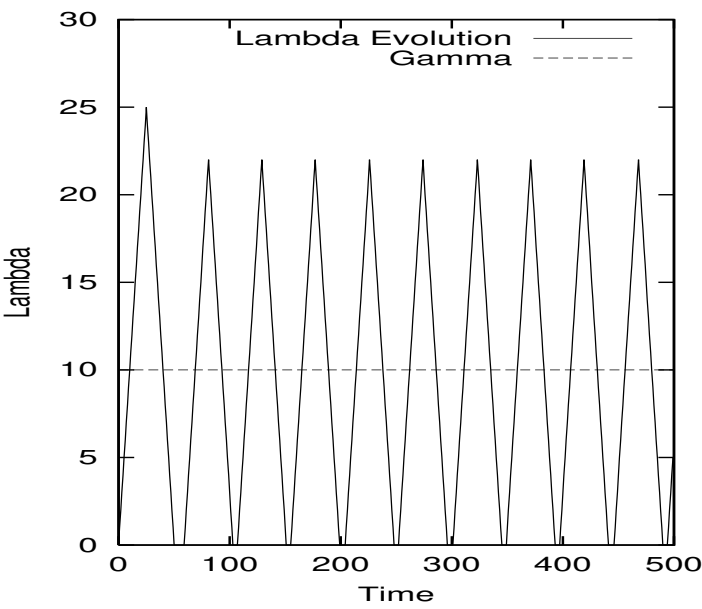
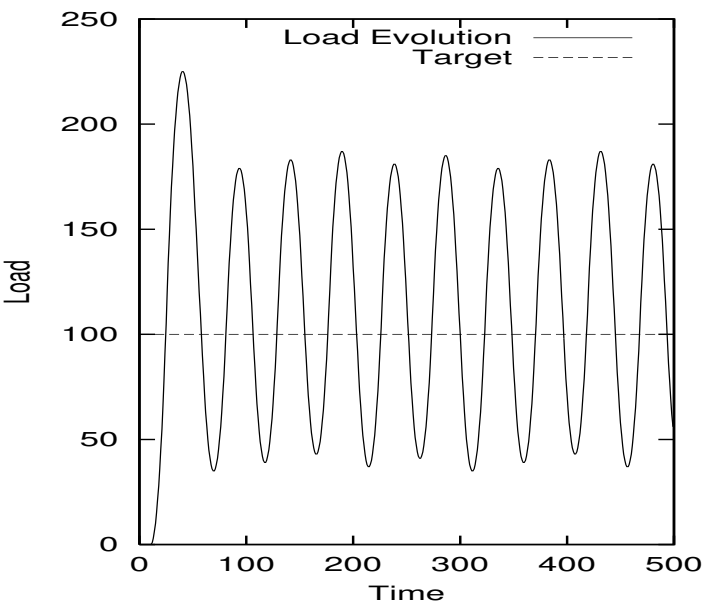
where  $a > 0$  is a fixed parameter

→ called linear increase/linear decrease

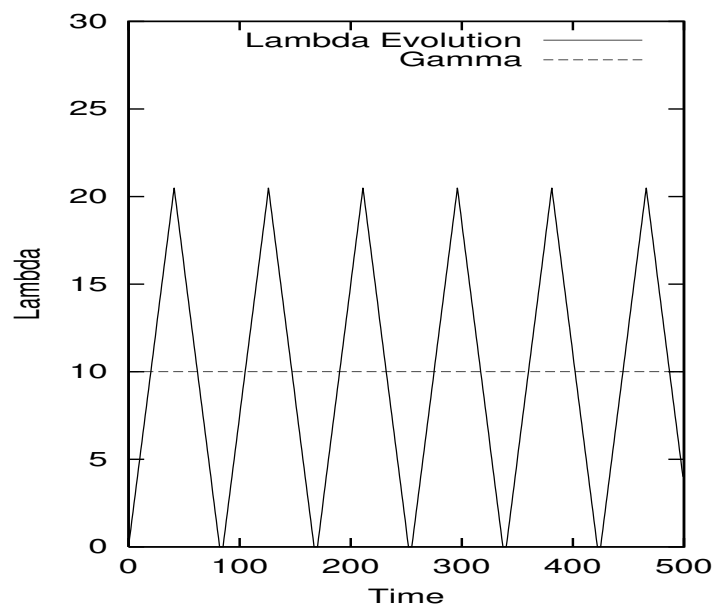
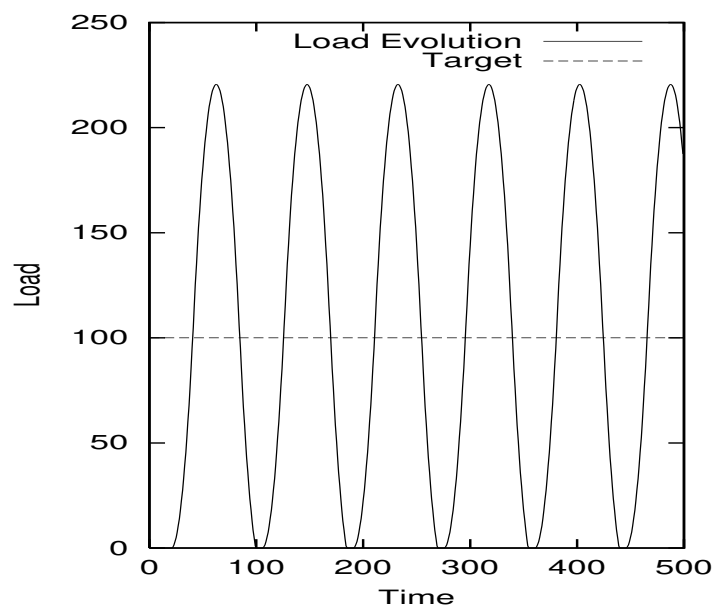
Question: how well does it work?

Example:

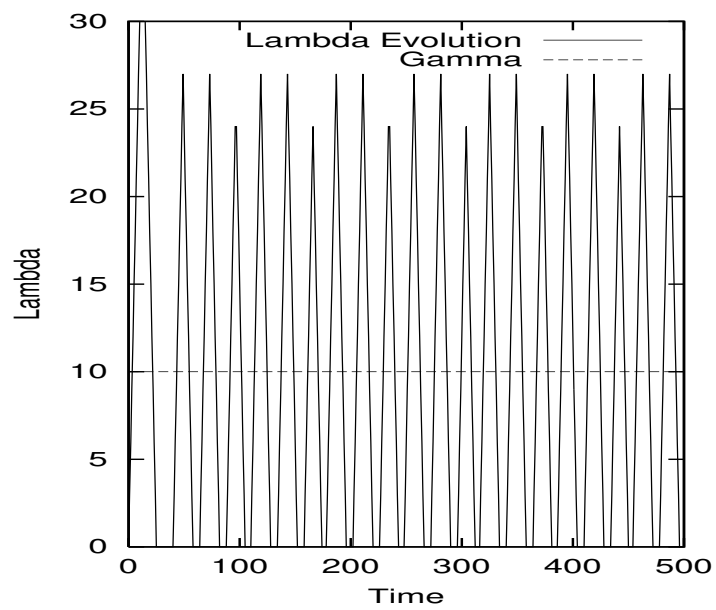
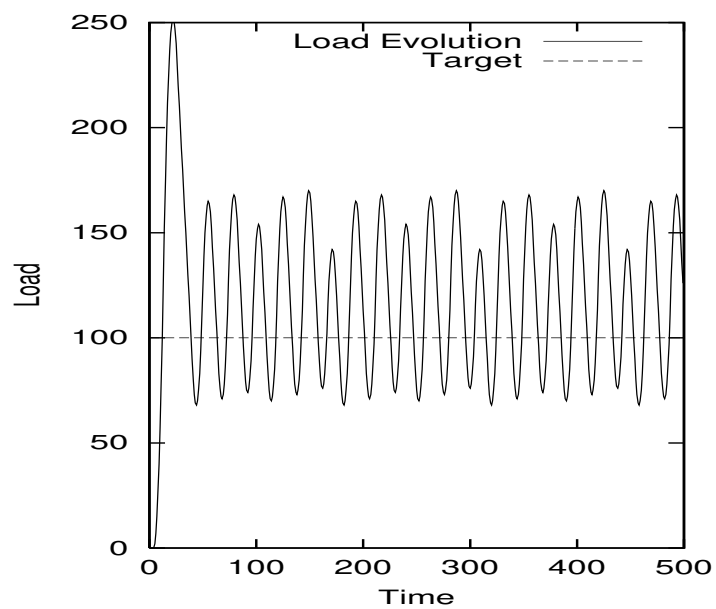
- $Q(0) = 0$
- $\lambda(0) = 0$
- $Q^* = 100$
- $\gamma = 10$
- $a = 1$



With  $a = 0.5$ :



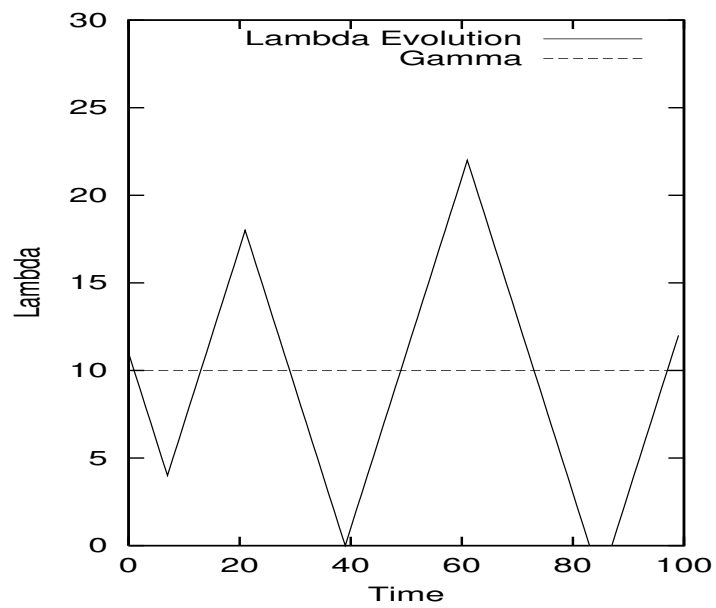
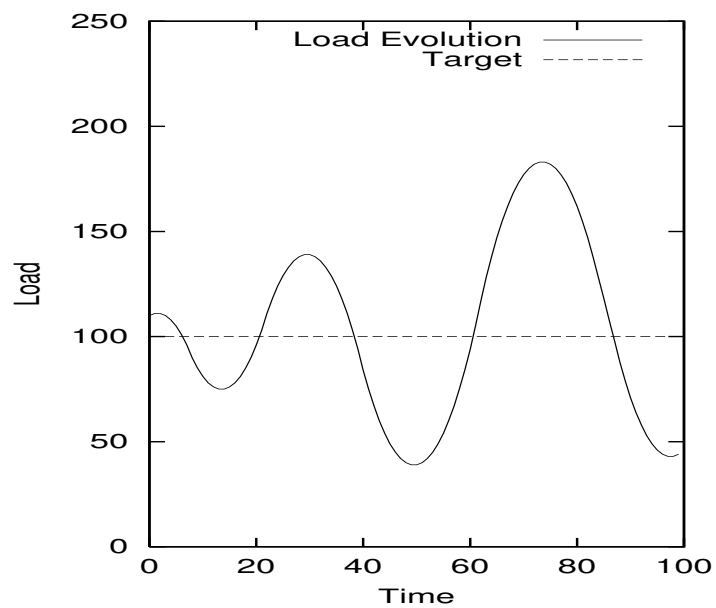
With  $a = 3$ :



Remarks:

- Method A isn't that great no matter what  $a$  value is used
  - keeps oscillating
- Actually: would lead to unbounded oscillation if not for physical restriction  $\lambda(t) \geq 0$  and  $Q(t) \geq 0$ 
  - i.e., bottoms out
  - easily seen: start from non-zero buffer
  - e.g.,  $Q(0) = 110$

With  $a = 1$ ,  $Q(0) = 110$ ,  $\lambda(0) = 11$ :



Method B:

- if  $Q(t) = Q^*$  then  $\lambda(t+1) \leftarrow \lambda(t)$
- if  $Q(t) < Q^*$  then  $\lambda(t+1) \leftarrow \lambda(t) + a$
- if  $Q(t) > Q^*$  then  $\lambda(t+1) \leftarrow \delta \lambda(t)$

where  $a > 0$  and  $0 < \delta < 1$  are fixed parameters

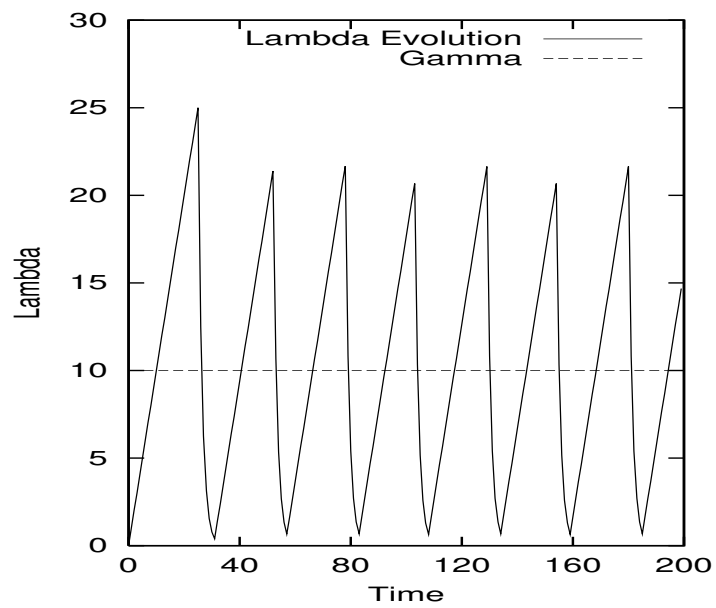
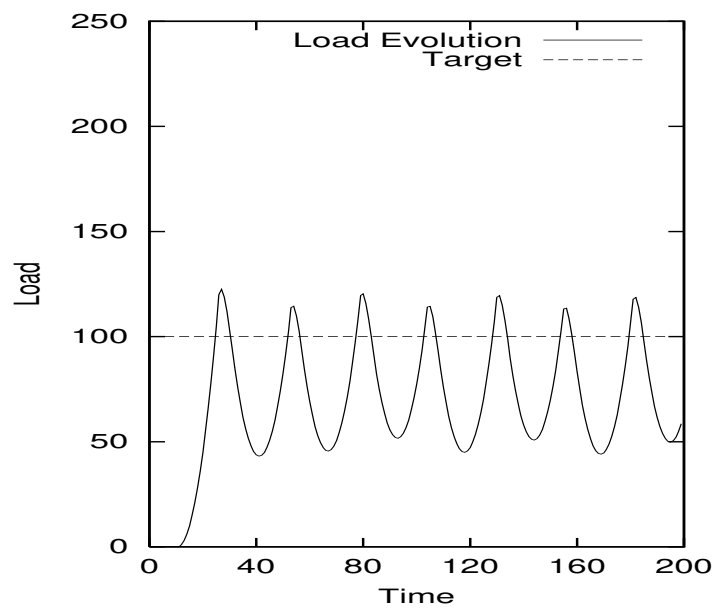
Note: only decrease part differs from **Method A**.

- linear increase with slope  $a$
- exponential decrease with backoff factor  $\delta$
- e.g., binary backoff in case  $\delta = 1/2$

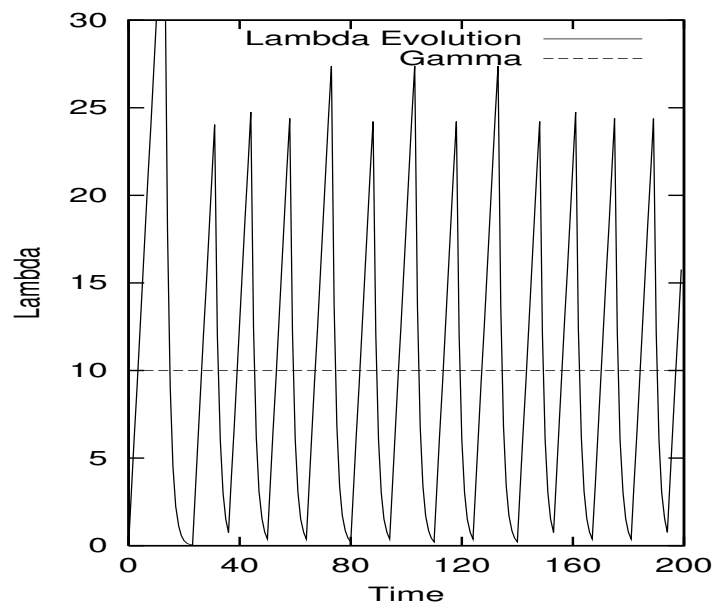
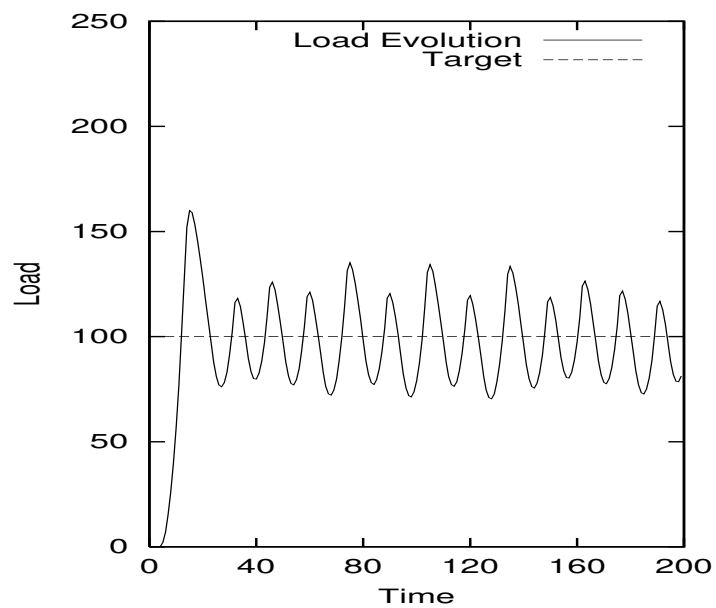
Similar to Ethernet and WLAN backoff

- question: does it work?

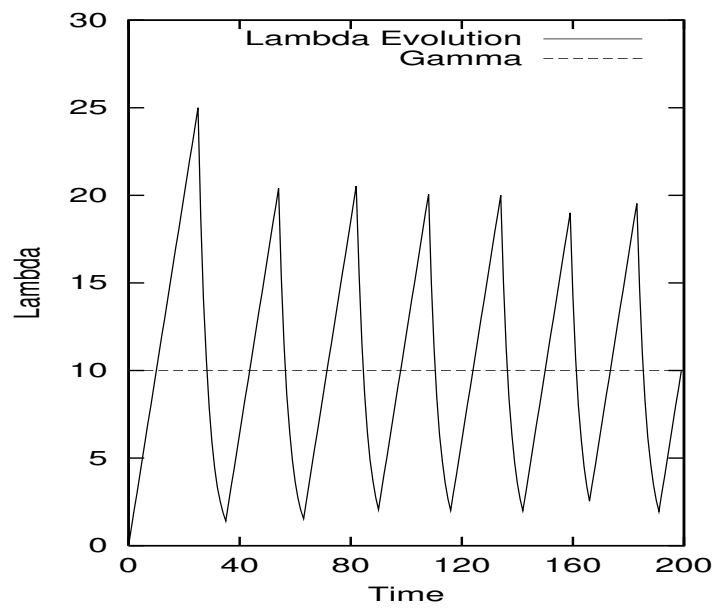
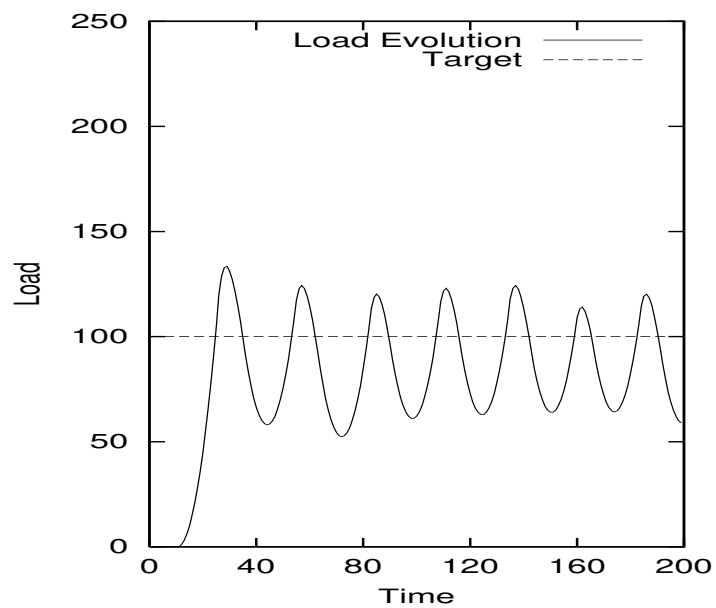
With  $a = 1$ ,  $\delta = 1/2$ :



With  $a = 3$ ,  $\delta = 1/2$ :



With  $a = 1$ ,  $\delta = 3/4$ :



Note:

- Method B oscillates around target
  - does not converge
- Superior to Method A: unbounded oscillation
  - doesn't hit “rock bottom”
  - due to asymmetry in increase vs. decrease policy
  - we observe “sawtooth” pattern
- Method B is used by TCP
  - linear increase/exponential decrease
  - additive increase/multiplicative decrease (AIMD)
  - will discuss specifics separately

Question: can we do better?

→ what information have we not made use of?

Method C:

$$\lambda(t+1) \leftarrow \lambda(t) + \varepsilon(Q^* - Q(t))$$

where  $\varepsilon > 0$  is a fixed parameter

Tries to adjust magnitude of change as a function of the gap  $Q^* - Q(t)$

→ if gap is big, change by a lot

→ if gap is small, change by a little

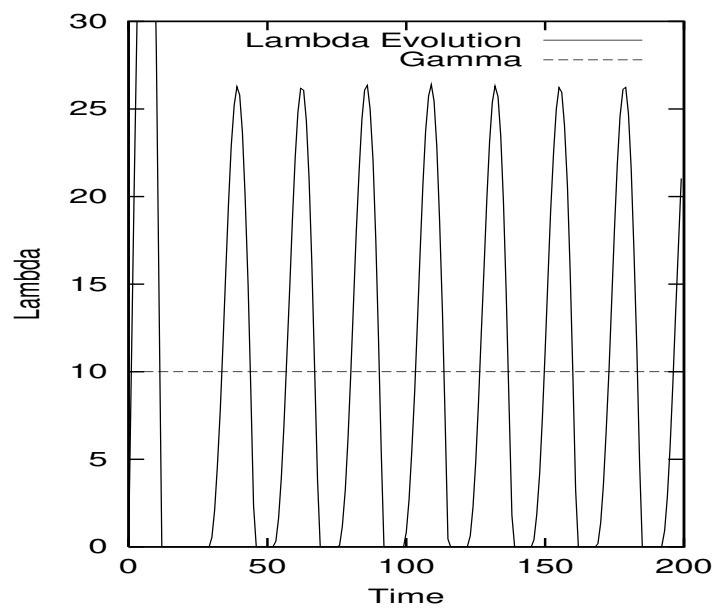
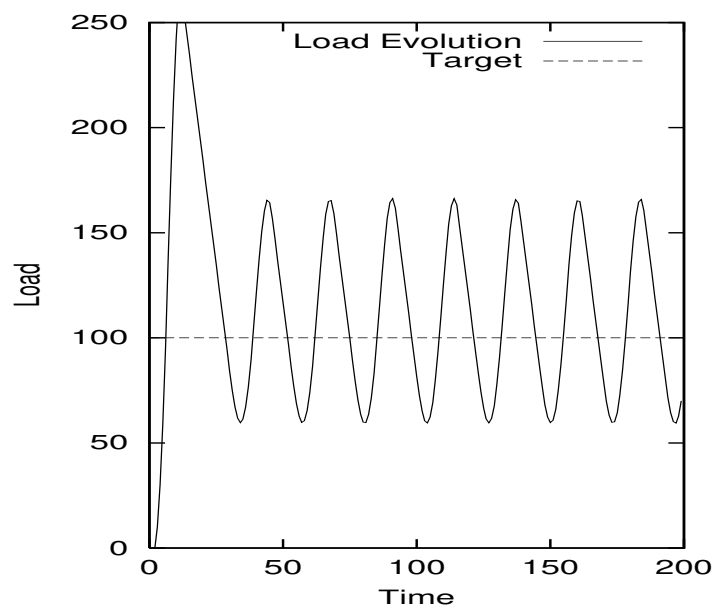
Thus:

- if  $Q^* - Q(t) > 0$ , increase  $\lambda(t)$  proportional to gap
- if  $Q^* - Q(t) < 0$ , decrease  $\lambda(t)$  proportional to gap

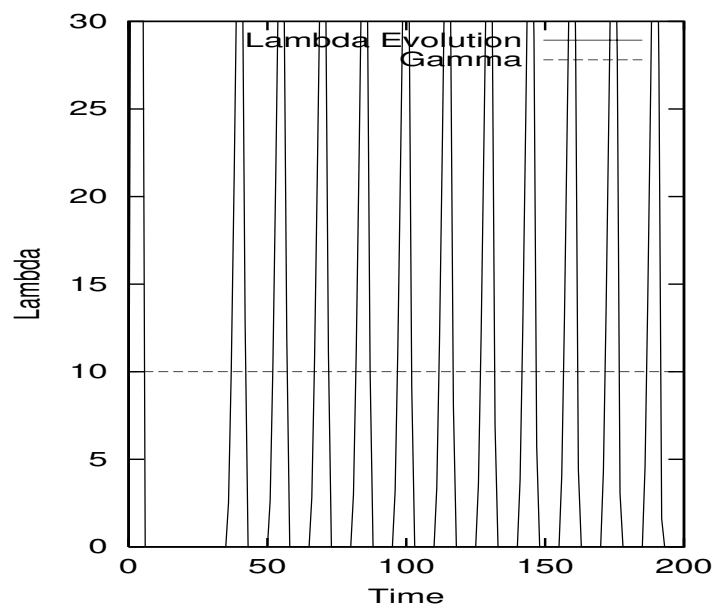
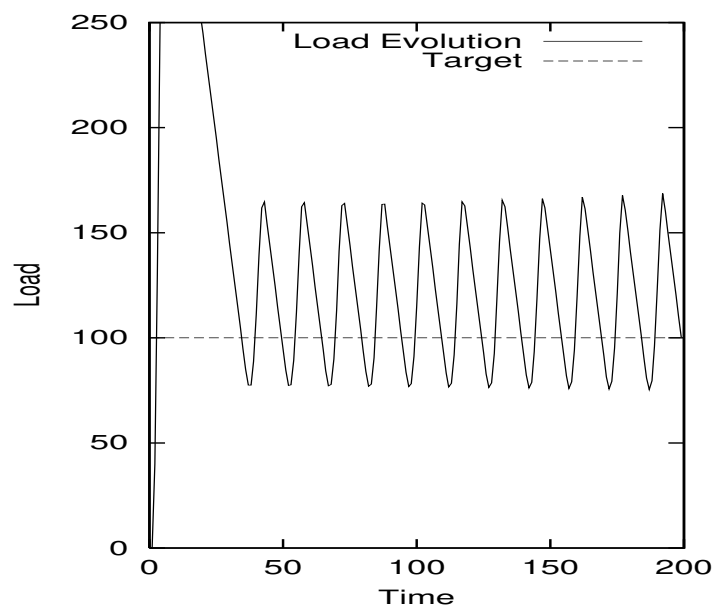
Trying to be more clever...

→ bottom line: is it any good?

With  $\varepsilon = 0.1$ :



With  $\varepsilon = 0.5$ :



Answer: no

→ control law looks good on the surface

→ but looks can be deceiving

Time to try something new

→ any (crazy) ideas?

Method D:

$$\lambda(t+1) \leftarrow \lambda(t) + \varepsilon(Q^* - Q(t)) + \beta(\gamma - \lambda(t))$$

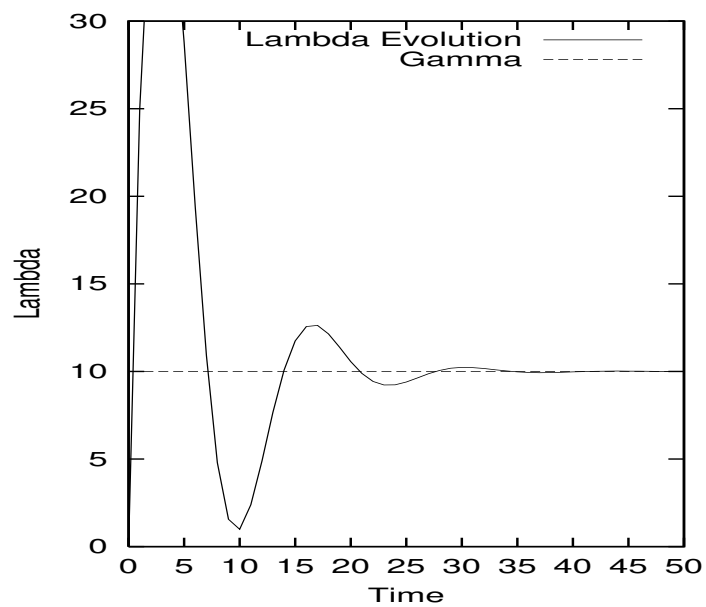
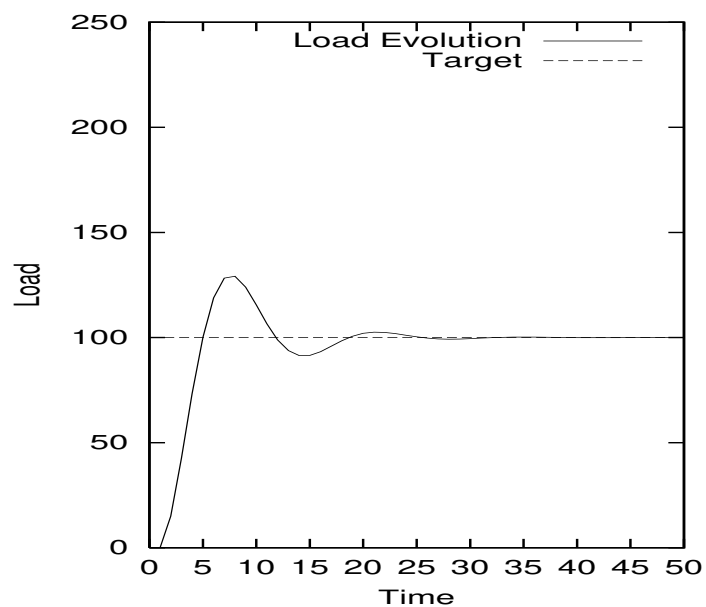
where  $\varepsilon > 0$  and  $\beta > 0$  are fixed parameters

→ additional term  $\beta(\gamma - \lambda(t))$

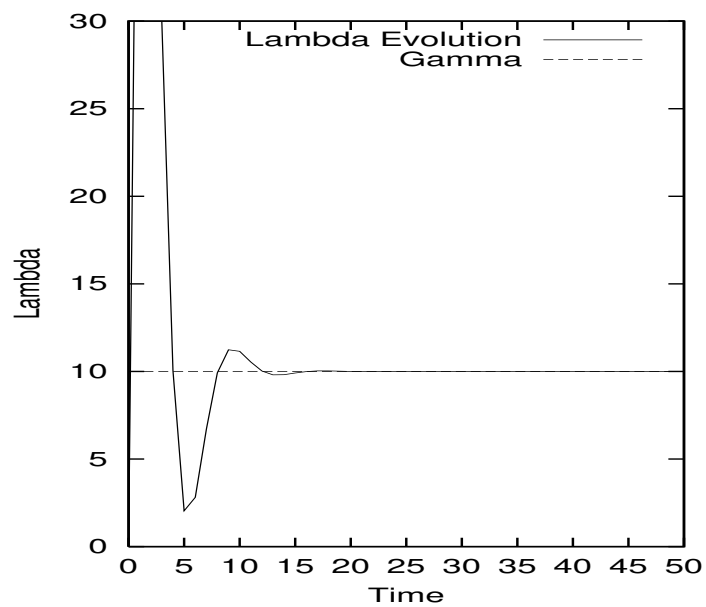
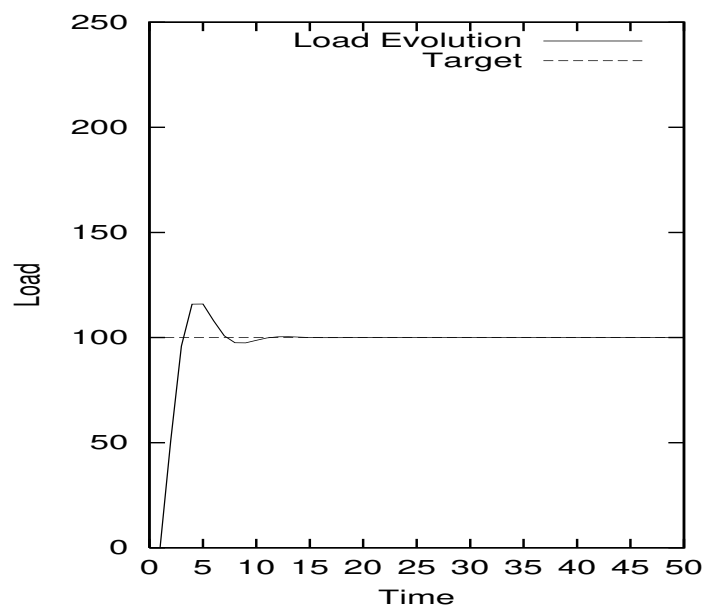
→ what's going on?

→ does it work?

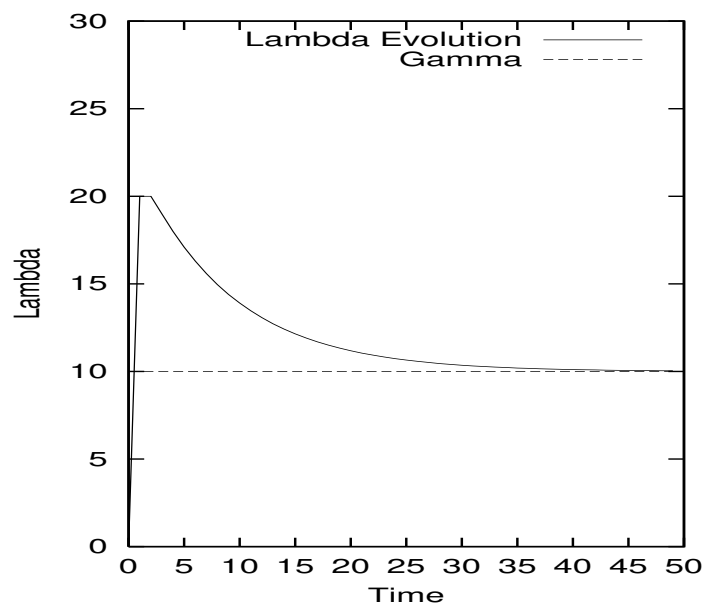
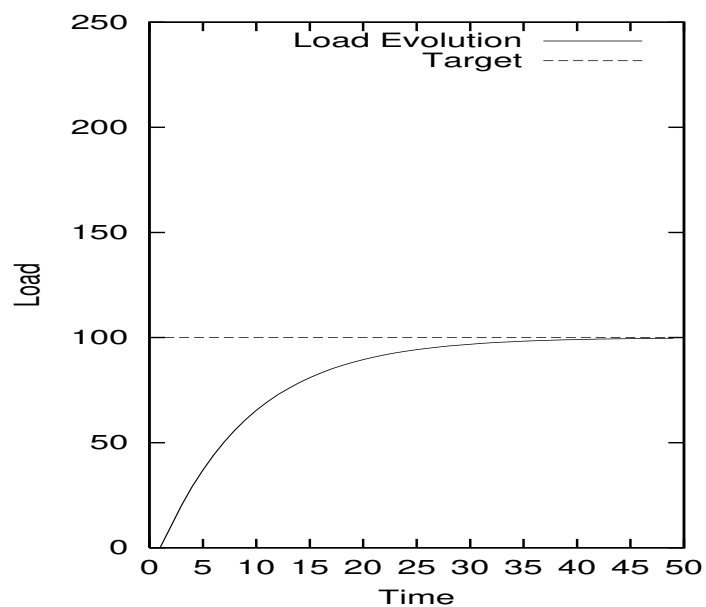
With  $\varepsilon = 0.2$  and  $\beta = 0.5$ :



With  $\varepsilon = 0.5$  and  $\beta = 1.1$ :



With  $\varepsilon = 0.1$  and  $\beta = 1.0$ :



Remarks:

- Method D has desired behavior
- Superior to Methods A, B, and C,
- No unbounded oscillation
- Convergence to desired state
  - target operating point  $(Q^*, \gamma)$
  - asymptotically stable