

Code Division Multiplexing

Direct sequence:

1) To send bit sequence $x = x_1x_2 \dots x_n$, use pseudorandom bit sequence $y = y_1y_2 \dots y_n$ to compute

$$\begin{aligned} z &= z_1z_2 \dots z_n \\ &= (x_1 \oplus y_1)(x_2 \oplus y_2) \dots (x_n \oplus y_n) \end{aligned}$$

2) Transmit z

3) To decode bit sequence $z = z_1z_2 \dots z_n$, compute

$$x = z \oplus y$$

Ex.: $x = 10010$, $y = 01011$

$$\longrightarrow z = x \oplus y = 10010 \oplus 01011 = 11001$$

$$\longrightarrow z \oplus y = 11001 \oplus 01011 = 10010$$

Pseudo-random y is called chipping code or pseudo-noise (PN) sequence.

In practice, single data bit encoded using $r > 1$ code bits.

Ex.: Suppose $r = 3$. To send single bit, say $x = 1$, “expand” x to $\tilde{x} = 111$ (r -fold duplication). If $y = 010$ then:

$$\longrightarrow z = \tilde{x} \oplus y = 111 \oplus 010 = 101$$

$$\longrightarrow z \oplus y = 101 \oplus 010 = 111$$

→ what next?

→ why use r -fold duplication?

Data rate usually slower than code rate

$$\rightarrow |y| = r \cdot |x|$$

→ more frequent changes: “spreading”

Previous scheme works for single user

- DSSS (direct sequence spread spectrum)
- networking: support multiple users
- how to do it?

Suppose N users, each sending a single bit: x^1, x^2, \dots, x^N .
Assume code rate r .

- user i 's expanded vector: $\tilde{x}^i = (x^i, x^i, x^i)$

Supposing N random chipping codes (one per user)

$$\{y^1, y^2, \dots, y^N\}$$

will the encoding

$$z = \tilde{x}^1 \oplus y^1 + \tilde{x}^2 \oplus y^2 + \dots + \tilde{x}^N \oplus y^N$$

work if user i decodes by EXOR'ing z with y^i ?

- i.e., what is $z \oplus y^i$?
- does it equal \tilde{x}^i ?

A different twist:

- represent bits as 1, -1 (not 1, 0)
 - $x^i \in \{1, -1\}$
- assume chipping codes $\{y^1, y^2, \dots, y^N\}$ are orthonormal
 - i.e., $y^i \circ y^j = 0$ ($i \neq j$) and $y^i \circ y^i = 1$
 - “ \circ ” is the dot product

Encoding (combined signal):

$$z = x^1 y^1 + x^2 y^2 + \dots + x^N y^N$$

→ note: x^i is a scalar, y^i is a vector

Decoding (for user i):

$$\begin{aligned} y^i \circ z &= x^1 y^i \circ y^1 + \dots + x^i y^i \circ y^i + \dots + x^N y^i \circ y^N \\ &= x^i \end{aligned}$$

→ exact recovery

→ CDMA (code division multiple access)

Ex.: $N = 4$, $r = 4$, and chipping code y^i 's are

$(1, 1, 1, 1)$, $(-1, -1, 1, 1)$, $(-1, 1, -1, 1)$, $(-1, 1, 1, -1)$

→ note: orthogonal but not orthonormal

→ $y^i \circ y^i = 4 (= r)$

→ hence, $y^i \circ z = 4 x^i$

→ r is also called “gain”

→ why useful?

Frequency hopping:

Use pseudorandom number sequence as key to index a set of carrier frequencies f_1, f_2, \dots, f_m .

→ frequency spreading

Receiver with access to pseudorandom sequence can decode transmitted signal.

→ receiver's tuner must jump around

→ code narrowband input as broadband output

→ frequency spreading

→ FHSS (frequency hopping spread spectrum)

DSSS vs. FHSS?

Benefits of CDMA:

- more secure against eavesdropping
 - confidentiality
- resistant to jamming
 - must jam a wider spectrum: more difficult
 - first introduced in the military context
- noise resistance
 - code rate r
- graceful degradation
 - compared to TDM

Deployment and usage:

- wireless LAN (WLAN): DSSS and FHSS
- cellular (e.g., Sprint PCS, Verizon): CDMA

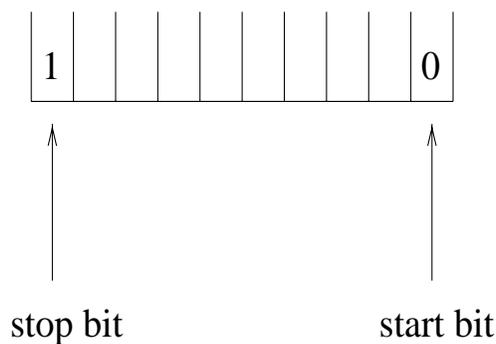
Competing with CDMA cellular: the rest!

- majority
- AT&T Wireless, Cingular, etc.
- dominant standard: GSM
- uses TDMA (time division multiple access)
- TDMA: FDM + TDM

Framing

- packet layout
- variety of framing conventions

Asynchronous: e.g., ASCII character transmission between dumb terminal and host computer.



- each character is an independent unit
 - “asynchronous”
- receiver needs to know bit duration
 - bit rate assumed known between sender/receiver

Overhead problem; assuming 1 start bit, 1 stop bit, 8 data bits, only 80% efficiency.

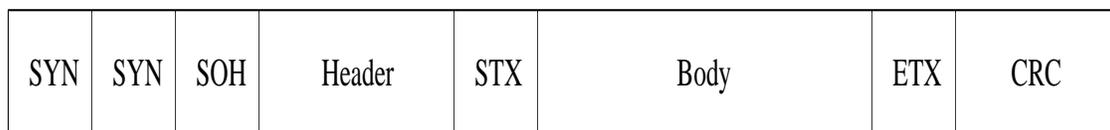
→ inefficient for long messages

iPod & radio example:

→ coding used asynchronous?

→ clock needed?

Synchronous: “Byte-oriented”; e.g., PPP, BISYNC



- SYN, SOH, STX, ETX, DLE: sentinels
- variable body size

Two problems:

- How to maintain synchronization if $|\text{Body}|$ is large?
- Control characters within body of message.
 - inefficient for short messages
 - efficiency approaches 1 as $|\text{Body}| \rightarrow \infty$

“Bit-oriented”; e.g., HDLC

→ bit is the unit

Use fixed *preamble* and *postamble*; simply a bit pattern.

→ 01111110

How to avoid confusing 01111110 in the data part?

→ bit stuffing

→ for data: stuff 0 after 5 consecutive 1's

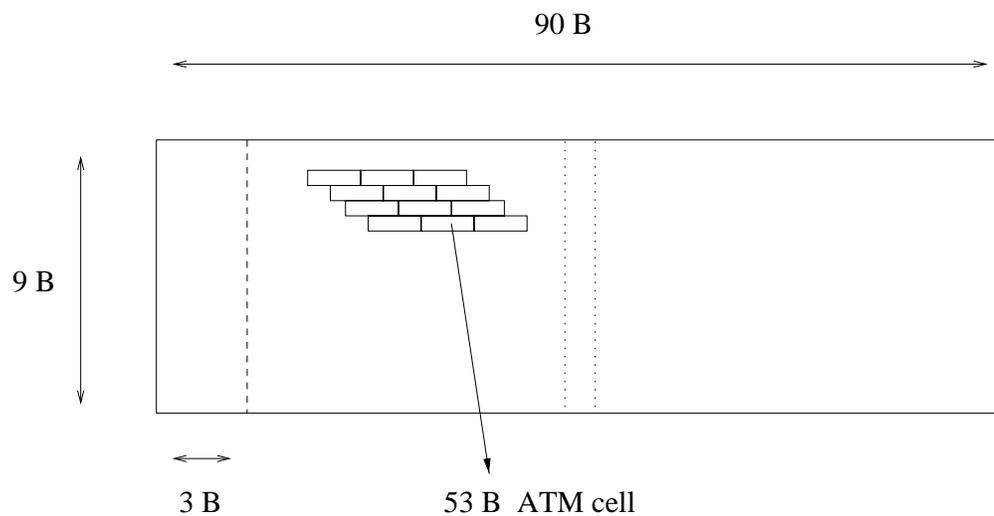
SONET (Synchronous Optical Network)

→ framing standard for optical fiber

Rates: OC-1 (51.84 Mbps), OC-3 (155.25 Mbps), OC-3c, OC-12 (622.08 Mbps), OC-24 (1.24416 Gbps), OC-48, etc.

→ formally: STS- n

OC-1 frame:



Features:

- 125 μ sec frame duration (for all OC- n)
- 51.84 Mbps = $810 \cdot 8 \cdot 8000$
- 3 + 1 columns of overhead
- overhead includes synchronization, pointer fields
- overhead encoded using NRZ
- payload scrambled (XOR'ed) to achieve approximate self-clocking