Route or path: criteria of goodness

- Hop count
- Delay
- Bandwidth
- Loss rate

Composition of goodness metric:
$\longrightarrow$ quality of end-to-end path

- Additive: hop count, delay
- Min: bandwidth
- Multiplicative: loss rate

Goodness of routing:
$\longrightarrow$ assume $N$ users or sessions
$\longrightarrow \quad$ suppose path metric is delay

Two approaches:

- system optimal routing
$\rightarrow$ choose paths to minimize $\frac{1}{N} \sum_{i=1}^{N} D_{i}$
$\rightarrow$ good for the system as a whole
- user optimal routing
$\rightarrow$ each user $i$ chooses path to minimize $D_{i}$
$\rightarrow$ selfish route selections by each user
$\rightarrow$ end result may not be good for system as a whole

Pros/cons:

- system optimal routing:
- good: minimizes delay for the system as a whole
- bad: complex and difficult to scale up
- user optimal routing:
- good: simple
- bad: may not make efficient use of resources
$\rightarrow$ low utilization
$\rightarrow$ recall "tragedy of commons" in congestion control

Two pitfalls of user optimal routing:

- fluttering or ping pong effect
- Braess paradox
$\rightarrow$ adding more resources can make things worse


## Algorithms

Find short, in particular, shortest paths from source to destination.

Key observation on shortest paths:

- Assume $p$ is a shortest path from $S$ to $D$
$\rightarrow S \xrightarrow{p} D$
- Pick any intermediate node $X$ on the path
- Consider the two segments $p_{1}$ and $p_{2}$
$\rightarrow S \xrightarrow{p_{1}} X \xrightarrow{p_{2}} D$
- The path $p_{1}$ from $S$ to $X$ is a shortest path, and so is the path $p_{2}$ from $X$ to $D$
$\longrightarrow$ leads to Dijkstra's algorithm


## Illustration:


$\rightarrow$ suggests algorithm for finding shortest path

Leads to Dijkstra's shortest-path algorithm:
$\rightarrow$ single-source all-destination

## Features:

- nunning time: $O\left(n^{2}\right)$ time complexity
$\rightarrow n$ : number of nodes
- if heap is used: $O(|E| \log |V|)$
$\rightarrow O(n \log n)$ if $|E|=O(n)$
- can also be run "backwards"
$\rightarrow$ start from destination $D$ and go to all sources
$\rightarrow$ a variant used in inter-domain routing
$\rightarrow$ forward version: used in intra-domain routing
- source $S$ requires global link distance knowledge
$\rightarrow$ centralized algorithm (center: source $S$ )
$\rightarrow$ every router runs Dijkstra with itself as source
$\rightarrow$ lots of broadcast management packets
- Internet protocol implementation
$\rightarrow$ OSPF (Open Shortest Path First)
$\rightarrow$ also called link state algorithm
$\rightarrow$ broadcast protocol
- builds minimum spanning tree rooted at $S$ :
$\rightarrow$ to all destinations
$\rightarrow$ if select destination: called multicasting
$\rightarrow$ multicast group
$\rightarrow$ standardized feature of IETF but not actively utilized on Internet
$\rightarrow$ complexity including group membership management


# Distributed/decentralized shortest path algorithm: 

$\longrightarrow$ Bellman-Ford algorithm
$\longrightarrow$ based on shortest path decomposition property

Key procedure:

- Each node $X$ maintains current shortest distance to all other nodes
$\rightarrow$ a distance vector
- Each node advertises to neighbors its current best distance estimates
$\rightarrow$ i.e., neighbors exchange distance vectors
- Each node updates shortest paths based on neighbors' advertised information
$\rightarrow$ same update criterion as Dijkstra's algorithm


## Features:

- running time: $O\left(n^{3}\right)$
- each source or router only talks to neighbors
$\rightarrow$ local interaction
$\rightarrow$ no need to send update if no change
$\rightarrow$ if change, entire distance vector must be sent
- knows shortest distance, but not path
$\rightarrow$ just the next hop is known
- elegant but additional issues compared to Dijkstra's algorithm
$\rightarrow$ e.g., stability
- Internet protocol implementation
$\rightarrow$ RIP (Routing Information Protocol)


## QoS routing:

Given two or more performance metrics e.g., delay and bandwidth - find path with delay less than target delay $D$ (e.g., 100 ms ) and bandwidth greater than target bandwidth $B$ (e.g., 1.5 Mbps$)$
$\longrightarrow$ from shortest path to best QoS path
$\longrightarrow$ multi-dimensional QoS metric
$\longrightarrow$ other: jitter, hop count, etc.

How to find best QoS path that satisfies all requirements?
Brute-force

- enumerate all possible paths
- rank them

How many paths are there:

- If there are $n$ nodes, there can be up to

$$
\frac{n(n-1)}{2}
$$

undirected links

- Hence, from source $S$ there can be up to

$$
(n-1)(n-2) \cdots 321=(n-1)!
$$

paths

- By Stirling's formula

$$
n!\approx \sqrt{2 \pi n}\left(\frac{n}{e}\right)^{n}
$$

$\rightarrow$ superexponential
$\rightarrow$ too many for brute-force

Is there a more clever or better algorithm?
$\longrightarrow$ as of Apr. 25, 2011: unknown
$\longrightarrow$ specifically: QoS routing is NP-hard
$\longrightarrow$ strong evidence there may not exist good algorithm

In networking: several problems turn out to be NP-complete
$\longrightarrow$ e.g., scheduling, control, crypto, ...
$\longrightarrow$ "P $=$ NP" problem
$\longrightarrow$ one of the hardest problems in science
In practice: doesn't matter too much for QoS routing
$\longrightarrow$ little demand for very good algorithm
$\longrightarrow$ roughly OK is fine
$\longrightarrow$ intra-domain: short paths
$\longrightarrow$ inter-domain: shortness plus other factors
$\longrightarrow$ policy routing

## Policy routing:

$\longrightarrow$ meaning of "policy" is not precisely defined
$\longrightarrow$ almost anything goes

Criteria include:

- Performance
$\rightarrow$ e.g., short paths
- Trust
$\rightarrow$ what is "trust"?
- Economics
$\rightarrow$ pricing
- Politics, etc.


## Implementation

Major Internet routing protocols:

- RIP (v1 and v2): intra-domain, Bellman-Ford
$\rightarrow$ also called distance vector routing
$\rightarrow$ metric: hop count
$\rightarrow$ UDP
$\rightarrow$ nearest neighbor advertisement
$\rightarrow$ popular in small intra-domain networks
- OSPF (v1 and v2): intra-domain, Dijkstra
$\rightarrow$ also called link state
$\rightarrow$ metric: average delay
$\rightarrow$ directly over IP: protocol number 89
$\rightarrow$ broadcasting via flooding
$\rightarrow$ popular in larger intra-domain networks
- IS-IS: intra-domain, Dijkstra
$\rightarrow$ directly over link layer (e.g., Ethernet)
$\rightarrow$ also available over IP (more recent)
$\rightarrow$ flooding
$\rightarrow$ popular in larger intra-domain networks

BGP (Border Gateway Protocol):
$\longrightarrow$ inter-domain routing
Autonomous System A
Autonomous System B


Border Routers
$\longrightarrow$ "peering" between two domains
$\longrightarrow$ typical: customer-provider relationship
$\longrightarrow$ in some cases: equals (true peers)
$\longrightarrow$ Internet exchanges: multiple domains meet up

- CIDR addressing
$\rightarrow$ i.e., a.b.c.d/x
$\rightarrow$ Purdue: 128.10.0.0/16, 128.210.0.0/16, 204.52.32.0/20
$\rightarrow$ check at www. iana.org (e.g., ARIN for US)
- Metric: policy
$\rightarrow$ e.g., shortest-path, trust, pricing
$\rightarrow$ meaning of "shortest": delay, router hop, AS hop
$\rightarrow$ mechanism: path vector routing
$\rightarrow$ BPG update message

BGP route update:
$\longrightarrow$ BGP update message propagation
BGP update message format:

$$
\operatorname{ASN} A_{k} \rightarrow \cdots \rightarrow \mathrm{ASN} A_{2} \rightarrow \operatorname{ASN} A_{1} ; \text { a.b.c.d/x }
$$

Meaning: ASN $A_{1}$ (with CIDR address a.b.c.d/x) can be reached through indicated path
$\longrightarrow$ called path vector
$\longrightarrow$ also AS-PATH
Some AS numbers:

- Purdue: 17
- BBN: 1
- UUNET: 701
- Level3: 3356
- Abilene (aka "Internet2"): 11537
- AT\&T: 7018


## Policy:

- if multiple AS-PATHs to target AS are known, choose one based on policy
$\rightarrow$ e.g., shortest AS path length, cheapest, least worrisome
- advertise to neighbors target AS's reachability
$\rightarrow$ also subject to policy
$\rightarrow$ no obligation to advertise!
$\rightarrow$ specifics depend on bilateral contract (SLA)

SLA (service level agreement):
$\longrightarrow$ bandwidth (e.g., 1 Gbps)
$\longrightarrow$ delay (e.g., avrg. 25ms US), loss (e.g., 0.05\%)
$\longrightarrow$ also peak vs. average
$\longrightarrow$ pricing (e.g., 1 Mbps: below $\$ 100$ )
$\longrightarrow$ availability, etc.

Example:


## Performance

Route update frequency:
$\longrightarrow$ routing table stability vs. responsiveness
$\longrightarrow$ rule: not too frequently
$\longrightarrow 30$ seconds
$\longrightarrow$ stability wins
$\longrightarrow$ hard lesson learned from the past (sub-second)
$\longrightarrow$ legacy: TTL

Other factors for route instability:
$\longrightarrow$ selfishness (e.g., fluttering)
$\longrightarrow$ BGP's vector path routing: inherently unstable
$\longrightarrow$ more common: slow convergence
$\longrightarrow$ target of denial-of-service (DoS) attack

Route amplification:
$\longrightarrow$ shortest AS path $\neq$ shortest router path
$\longrightarrow$ e.g., may be several router hops longer
$\longrightarrow$ AS graph vs. router graph
$\longrightarrow$ policy: company in Denmark

Route asymmetry:
$\longrightarrow$ routes are not symmetric
$\longrightarrow$ estimate: $>50 \%$
$\longrightarrow$ mainly artifact of inter-domain policy routing
$\longrightarrow$ various performance implications
$\longrightarrow$ source traceback

Black holes:
$\longrightarrow$ persistent unreachable destination prefixes
$\longrightarrow$ BGP routing problems
$\longrightarrow$ further aggrevated by DNS

