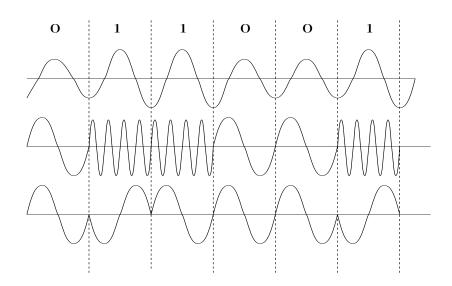
Additional modulation variations:

• Amplitude modulation (AM): encode bits using amplitude levels

 $\rightarrow$  use multiple magnitude levels

 $\rightarrow 8$  levels: 3 bits per clock tick (called baud)

- Frequency modulation (FM): encode bits using frequency changes
- Phase modulation (PM): encode bits using phase shifts



Park

Terminology: AM, FM, PM are also called amplitude, frequence, phase shift keying (ASK, FSK, PSK)

- $\rightarrow$  e.g., BPSK: binary PSK; QPSK (4 phases)
- $\rightarrow$  or their combination: amplitude and phase
- $\rightarrow$  QAM (quadrature amplitude modulation): amplitude and phase
- $\rightarrow$  e.g., 16-QAM: 4 amplitudes, 4 phases; 64-QAM
- $\rightarrow$  e.g., WiFi, DVB

But ASK and PSK can increase bit rate only so much.

Same with increasing frequency.

 $\rightarrow$  esp. wireless due to LOS constraint above 10 GHz

What's left?

Back to 100 MHz–102 MHz example.

- $\rightarrow$  bandwidth: 2 MHz
- $\rightarrow$  how many carrier frequencies can we squeeze in?
- $\rightarrow$  recall: with 100.0, 100.1, 100.2, ..., 101.8, 101.9, 102.0 MHz could support 31 simultaneous users
- $\rightarrow$  what about: 100.00, 100.01, 100.02, . . ., 101.98, 101.99, 102.00 MHz
- $\rightarrow$  how many parallel bit streams possible?

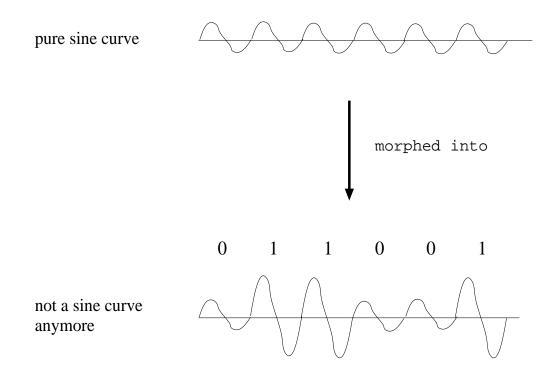
There must be a catch.

 $\rightarrow$  what is it?

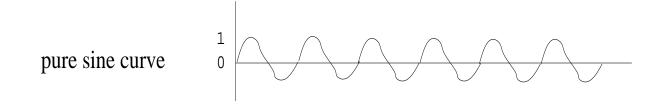
Bits on one carrier frequency may interfere with bits on another carrier frequency.

- $\rightarrow$  e.g., bits carried on 100 MHz frequency distort bits carried on 101 MHz frequency
- $\rightarrow$  and vice versa
- $\rightarrow$  called inter-channel interference (ICI)
- $\rightarrow$  why does this happen?

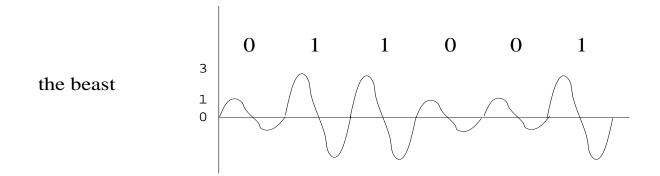
 $\rightarrow$  e.g., frequency f = 100 MHz



To carry bits, it gets morphed by AM into something else.  $\rightarrow$  a beast! (think of movie "The Fly")  $\rightarrow$  a good beast First, what's the "DNA" of pure sine curve?



"DNA" of good beast carrying bits 0 1 1 0 0 1



- $\rightarrow$  DNA from parent: pure sine curve (100 MHz)
- $\rightarrow$  but will also carry mutant DNA: from 101 MHz, 102 MHz
- $\rightarrow$  also how much of each mutant DNA (i.e., magnitude)
- $\rightarrow$  ex.: magnitude 1 from 100 MHz, 2 from 101 MHz, 0.03 from 102 MHz

How to create beast from parent and mutant DNAs:

 $\rightarrow$  just add

 $\rightarrow$  beast = 1 × sine(100 MHz) + 2 × sine(101 MHz) + 0.03 × sine(102 MHz)

Will adding the three sine curves above create the morphed curve carrying bits 0 1 1 0 0 1 ?

For any morphed curve (aka "signal") carrying bits, it is difficult to find by visual inspection what the component DNAs (i.e., pure sine curves) are.

 $\rightarrow$  also how do we know that adding sine curves will give us the beast?

First, why do we care?

- $\rightarrow$  recall motivation: inter-channel interference
- $\rightarrow$  bits carried on frequency 100 MHz distorts bits carried on 101 MHz

 $\rightarrow$  how?

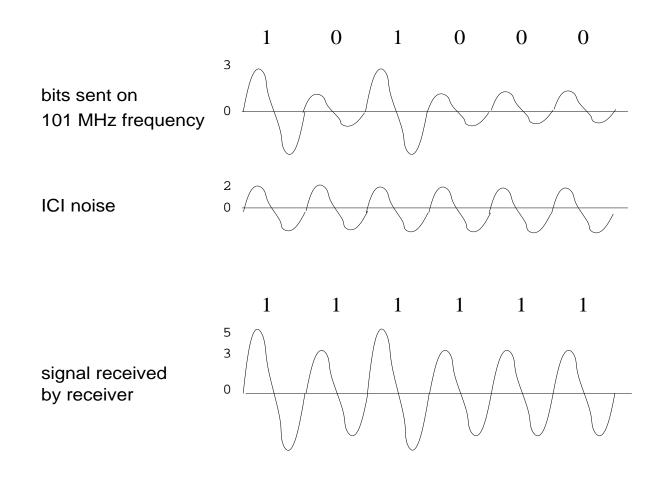
Intuition: performing AM modulation on pure sine curve 100 MHz to ship bits 0 1 1 0 0 1 has a side effect

 $\rightarrow$  creates mutant DNA: 101 MHz sine curve of amplitude 2

When a receiver wants to know what bits are carried on frequency 101 MHz, it "tunes into" frequency 101 MHz and checks how the amplitude varies every clock tick

- $\rightarrow$  say bits 1 0 1 0 0 0 were sent on frequency 101 MHz
- $\rightarrow$  but noise on 101 MHz with amplitude 2 mixes with the original signal

What bits will be receiver think have been transmitted?



Key observations:

1. Sending parallel bit streams using multiple carrier frequencies only works if we can keep inter-channel interference (ICI) under control.

 $\rightarrow$  else receiver gets corrupted bits

2. How do we know that a morphed sine curve carrying bits is just the sum of sine curves with different amplitudes?

 $\rightarrow$  not obvious: J. F. made important contribution during Napoleon's time

3. How do we know what sine curves to add and what amplitude each should get to create beast?

 $\rightarrow$  J. F. gives a simple formula