

CS590U

# **Access Control: Theory and Practice**

Lecture 20 (March 24)

Security Analysis in Trust Management



# What is Security Analysis?

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- Inspired by safety analysis, which was initially formalized by Harrison et al.
- An access control policy verification technique
- Studies properties of access control systems whose state may change
- Precisely evaluates which principals/users are trusted for what properties.



# The Abstract Security Analysis Problem

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- Given a start state  $P$ ,
  - a query  $Q$ ,
  - and a rule  $R$  that determines how states can change (defines reachability among states);
- Ask
  - Is  $Q$  possible? (existential)
    - whether  $\exists$  reachable  $P'$  s.t.  $Q$  is true in  $P'$
  - Is  $Q$  necessary? (universal)
    - whether  $\forall$  reachable  $P'$ ,  $Q$  is true in  $P'$



# How to Use Security Analysis

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- Guarantee safety and availability properties of an AC system:
  - Properties one wants to guarantee are encoded in a set of queries
  - R identifies trusted principals
    - assumes that parts under these principals' control do not change
  - Trusted principals perform security analysis before making changes

# Security Analysis in RBAC

N. Li & M. Tripunitara  
SACMAT 2004



# Security Analysis in RBAC

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- RBAC state is  $\langle UA, PA, RH \rangle$
- State change rules: admin model, e.g. ARBAC97 [Sandhu et al., TISSEC'99]
- Queries:
  - Have the form "userSet<sub>1</sub> ? userSet<sub>2</sub> ?"
    - e.g. "is  $r_1 \cap r_2$  ? {u1,u2}?"
  - Called semi-static if either userSet<sub>1</sub> or userSet<sub>2</sub> can be evaluated independent of the state



# Admin Models: AATU and AAR

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- $AATU = \langle can\_assign, T \rangle$ 
  - $can\_assign \subseteq R \times C \times 2^R$ 
    - $\langle manager, employee \ ? \ engineer, \{projLead\} \rangle$
  - T: a set of trusted users
- $AAR = \langle can\_assign, can\_revoke \rangle$ 
  - $can\_revoke \subseteq R \times 2^R$ 
    - $\langle manager, \{projLead\} \rangle$



# Results - AATU

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- For semi-static queries, security analysis is efficient (polynomial time)
- For other types of queries, security analysis is decidable, but intractable (coNP-hard)





# Results - AAR

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- For semi-static queries, security analysis is efficient.
- For other queries, security analysis is decidable, but intractable (coNP-complete)



# How We Showed This

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- We present a reduction from our security analysis instances to instances in RT
- Mapping:
  - Input: RBAC  $\langle \text{state}, \text{query}, \text{state-change rule} \rangle$
  - Output: RT  $\langle \text{state}, \text{query}, \text{state-change rule} \rangle$

# Beyond Proof-of-Compliance: Security Analysis in Trust Management

N. Li, J.C. Mitchell & W.H. Winsborough.

To Appear in JACM.

Conference version in IEEE S&P 2003.



# Motivation for Security Analysis in TM?

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- Delegation is used extensively in TM
- Control may be delegated to partially trusted principals
- What if one delegates to the wrong principal?
- How to ensure that desirable security properties are maintained with delegation?

# The TM Language

$$RT[\Leftarrow, \cap] = RT_0$$

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- Basic concepts in  $RT[\Leftarrow, \cap]$ :
  - Principals:  $K, K_1, K_2$
  - Role names:  $r, r_1, r_2$
  - Roles:  $K.r$  (K's r role)
    - each role has a member set



# Statements in $RT[\Leftarrow, \cap]$

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- Type-1:  $K.r \leftarrow K_1$ 
  - $\text{mem}[K.r] \hat{E} \{K_1\}$
  - $K_{\text{HR}}.\text{manager} \leftarrow K_{\text{Alice}}$
  
- Type-2:  $K.r \leftarrow K_1.r_1$ 
  - $\text{mem}[K.r] \hat{E} \text{mem}[K_1.r_1]$
  - $K_{\text{SSO}}.\text{admin} \leftarrow K_{\text{HR}}.\text{manager}$

# Statements in $RT[\Leftarrow, \cap]$

- Type-3:  $K.r \leftarrow K.r_1.r_2$

- Let  $\text{mem}[K.r_1]$  be  $\{K_1, K_2, \dots, K_n\}$        $\text{mem}[K.r] \hat{=} \bigcap_{i=1}^n \text{mem}[K_i.r_2]$
- $K_{SSO}.\text{delegAccess} \leftarrow K_{SSO}.\text{admin.access}$

- Type-4:  $K.r \leftarrow K_1.r_1 \underset{\zeta}{\cap} K_2.r_2$

- $\text{mem}[K.r] \hat{=} \text{mem}[K_1.r_2] \underset{\zeta}{\cap} \text{mem}[K_2.r_2]$
- $K_{SSO}.\text{access} \leftarrow K_{SSO}.\text{delegAccess} \underset{\zeta}{\cap} K_{HR}.\text{employee}$



# The Query Q

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- Form-1:  $\text{mem}[K.r] \hat{E} \{K_1, \dots, K_n\} ?$
- Form-2:  $\{K_1, \dots, K_n\} \hat{E} \text{mem}[K.r] ?$
- Form-3:  $\text{mem}[K_1.r_1] \hat{E} \text{mem}[K.r] ?$





# The Semantic Relation

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- A statement  $\Rightarrow$  a Datalog rule
  - $K.r \leftarrow K_2 \quad \Rightarrow \quad m(K, r, K_2)$
  - $K.r \leftarrow K_1.r_1 \quad \Rightarrow \quad m(K, r, z) :- m(K_1, r_1, z)$
  - ...
- A state  $P \Rightarrow$  a Datalog program  $SP[P]$ 
  - $\text{mem}[K.r] \circ \{ K' \mid m(K, r, K') \text{ is in the minimal Herbrand model of } SP[P] \}$



# Example Queries & Answers

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1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
3.  $K_{HR}.employee \leftarrow K_{HR}.manager$
4.  $K_{HR}.manager \leftarrow K_{Alice}$
5.  $K_{HR}.employee \leftarrow K_{David}$

$mem[K_{SSO}.access] \hat{E} \{K_{David}\}?$  No

$\{K_{Alice}, K_{David}\} \hat{E} mem[K_{SSO}.employee]?$  Yes

$mem[K_{HR}.employee] \hat{E} mem[K_{SSO}.access]?$  Yes



# The State-Change Rule R

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- $R = (G, S)$ 
  - G is a set of growth-restricted roles
    - if  $A.r \in G$ , then cannot add " $A.r \leftarrow \dots$ "
  - S is a set of shrink-restricted roles
    - if  $A.r \in S$ , then cannot remove " $A.r \leftarrow \dots$ "
- Motivation:
  - Definitions of roles that are not under one's control may change



# Sample Analysis Queries

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- Simple safety (existential form-1):
  - Is  $\text{mem}[K.r] \supseteq \{K_1\}$  possible?
- Simple availability (universal form-1):
  - Is  $\text{mem}[K.r] \supseteq \{K_1\}$  necessary?
- Bounded safety (universal form-2):
  - Is  $\{K_1, \dots, K_n\} \supseteq \text{mem}[K.r]$  necessary?
- Containment (universal form-3):
  - Is  $\text{mem}[K_1.r_1] \supseteq \text{mem}[K.r]$  necessary?



# Example

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1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.access \leftarrow K_{SSO}.delegAccess \text{ } \textcircled{C} \text{ } K_{HR}.employee$
3.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
4.  $K_{SSO}.delegAccess \leftarrow K_{SSO}.admin.access$
5.  $K_{HR}.employee \leftarrow K_{HR}.manager$
6.  $K_{HR}.employee \leftarrow K_{HR}.engineer$
7.  $K_{HR}.manager \leftarrow K_{Alice}$
8.  $Alice.access \leftarrow K_{Bob}$

Legend:           fixed  
                  can grow, can shrink



# A Simple Availability Query

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1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.access \leftarrow K_{SSO}.delegAccess \wp K_{HR}.employee$
3.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
4.  $K_{SSO}.delegAccess \leftarrow K_{SSO}.admin.access$
5.  $K_{HR}.employee \leftarrow K_{HR}.manager$
6.  $K_{HR}.employee \leftarrow K_{HR}.engineer$
7.  $K_{HR}.manager \leftarrow K_{Alice}$
8.  $Alice.access \leftarrow K_{Bob}$

Query: Is  $mem[K_{SSO}.access] \hat{E} \{K_{Alice}\}$  necessary?

Answer: Yes. (Available)

Why: Statements 1, 3, and 7 cannot be removed



# A Simple Safety Query

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1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.access \leftarrow K_{SSO}.delegAccess \text{ } \subset K_{HR}.employee$
3.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
4.  $K_{SSO}.delegAccess \leftarrow K_{SSO}.admin.access$
5.  $K_{HR}.employee \leftarrow K_{HR}.manager$
6.  $K_{HR}.manager \leftarrow K_{Alice}$
7.  $K_{HR}.employee \leftarrow K_{HR}.engineer$
8.  $K_{Alice}.access \leftarrow K_{Bob}$

Query: Is  $\text{mem}[K_{SSO}.access] \supseteq \{K_{Eve}\}$  possible?

Answer: Yes. (Unsafe)

Why: Both  $K_{HR}.engineer$  and  $K_{Alice}.access$  may grow.

# A Containment Analysis Query about Safety

1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.access \leftarrow K_{SSO}.delegAccess \text{ } \textcircled{C} \text{ } K_{HR}.employee$
3.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
4.  $K_{SSO}.delegAccess \leftarrow K_{SSO}.admin.access$
5.  $K_{HR}.employee \leftarrow K_{HR}.manager$
6.  $K_{HR}.employee \leftarrow K_{HR}.engineer$
7.  $K_{HR}.manager \leftarrow K_{Alice}$
8.  $K_{Alice}.access \leftarrow K_{Bob}$

Query: Is  $\text{mem}[K_{HR}.employee] \supseteq \text{mem}[K_{SSO}.access]$  necessary?

Answer: Yes. (Safe)

Why:  $K_{SSO}.access$  and  $K_{SSO}.admin$  cannot grow and Statement 5 cannot be removed.



# An Containment Analysis Query about Availability

1.  $K_{SSO}.access \leftarrow K_{SSO}.admin$
2.  $K_{SSO}.access \leftarrow K_{SSO}.delegAccess \wp K_{HR}.employee$
3.  $K_{SSO}.admin \leftarrow K_{HR}.manager$
4.  $K_{SSO}.delegAccess \leftarrow K_{SSO}.admin.access$
5.  $K_{HR}.employee \leftarrow K_{HR}.manager$
6.  $K_{HR}.employee \leftarrow K_{HR}.engineer$
7.  $K_{HR}.manager \leftarrow K_{Alice}$
8.  $Alice.access \leftarrow K_{Bob}$

Query: Is  $mem[K_{SSO}.access] \supseteq mem[K_{HR}.manager]$  necessary?

Answer: Yes. (Available)

Why: Statements 1 and 3 cannot be removed



# Form-1 and Form-2 Queries

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- PTIME

- Form-1 queries are monotonic in P
- Form-2 queries are anti-monotonic in P
- Use the minimal reachable state to answer universal form-1 and existential form-2
- The maximal reachable state answers existential form-1 and universal form-2
  - the state is simulated by a logic program

Reminder: Form-1 query:  $\text{mem}[K.r] \hat{E} \{K_1, \dots, K_n\}$   
Form-2 query:  $\{K_1, \dots, K_n\} \hat{E} \text{mem}[K.r]$

# Universal Form-3 $\equiv$ Containment Analysis

- With just type 1 and 2 statements
  - containment analysis is in PTIME
    - using logic programs with stratified negation
- With type 1, 2, and 4 statements
  - containment analysis is coNP-complete
    - equivalent to determining validity of propositional-logic formulas

Reminder:

Queries:	Form-3:	$\text{mem}[K_1.r_1] \supseteq \text{mem}[K.r]$
Statements:	Type-1:	$K.r \leftarrow K_1$
	Type-2:	$K.r \leftarrow K_1.r_1$
	Type-4:	$K.r \leftarrow K_1.r_1 \cap K_2.r_2$

# Universal Form-3 (Containment Analysis)

- $RT[\Leftarrow]$  (Type 1, 2, and 3 statements)
  - containment analysis is PSPACE-complete
    - $RT[\Leftarrow] \Leftrightarrow$  string-rewriting systems
    - equivalent to determining containment of languages accepted by NFA's
  - remains PSPACE-complete without shrinking
  - coNP-complete without growing

Reminder:

Type-1:	$K.r \leftarrow K_1$
Type-2:	$K.r \leftarrow K_1.r_1$
Type-3:	$K.r \leftarrow K_1.r_1.r_2$

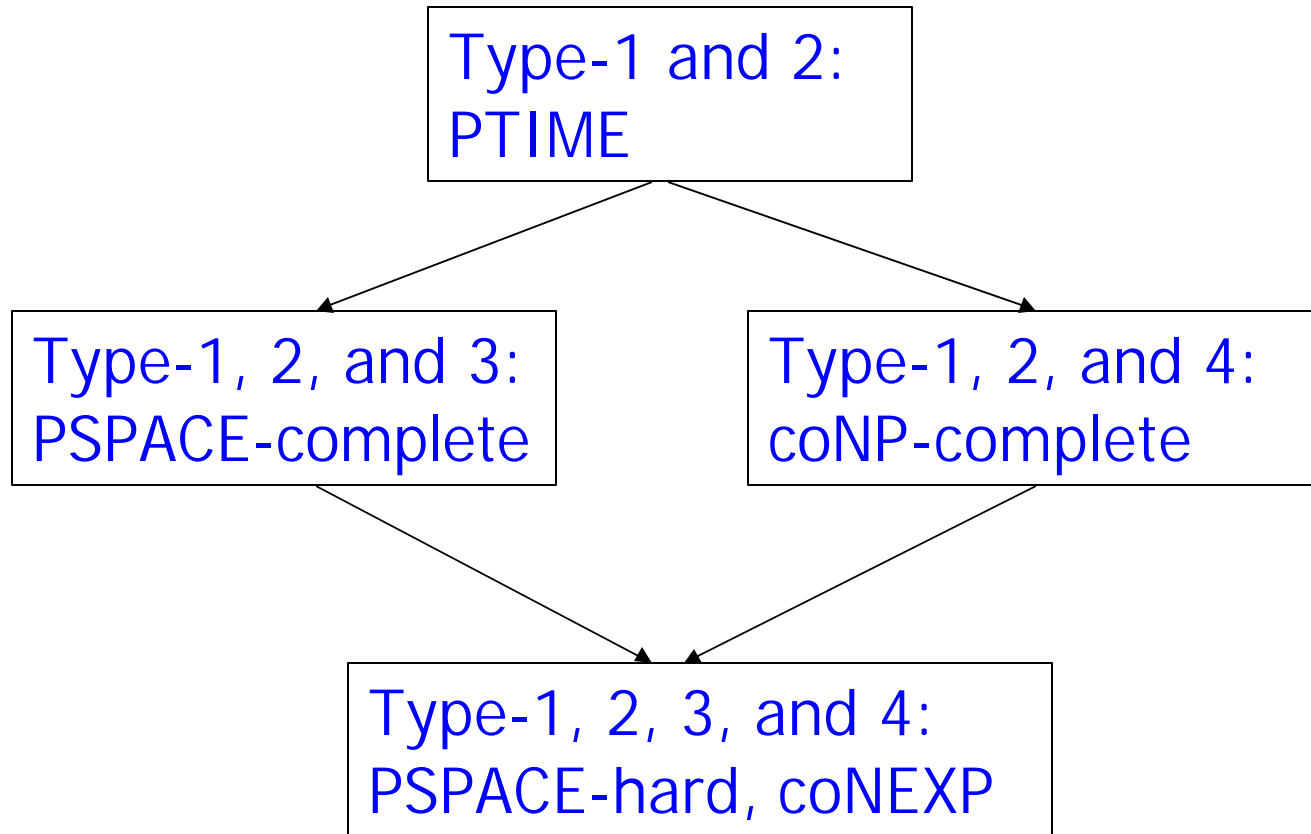


# Universal Form-3 (Containment Analysis)

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- $RT[\Leftarrow, \cap]$  (all four types of statements)
  - in coNEXP
    - although infinitely many new principals and statements may be added, if the containment does not hold, there exists a counter example whose size is at most exponential
  - PSPACE-hard
  - exact complexity still open!
  - coNP-complete without growing

# Summary of Complexities for Containment Analysis





# Summary

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- The analysis problem: Given  $P$ ,  $Q$ , and  $R$ , is  $Q$  possible, is  $Q$  necessary?
- Certain classes of security analysis in RBAC reduce to that in  $RT[\Leftarrow, \cap]$
- Security analysis problems for  $RT[\Leftarrow, \cap]$ 
  - decidable
  - efficiently decidable for most queries
  - for containment analysis, complexity depends on delegation features of the policy language

# Mapping the HRU model to the Abstract Analysis Problem

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- P: an access matrix
- R: the protection system state can change by executing commands
  - e.g.,  $c(x,y,z) \{ \text{if 'own'} \in \text{cell}(x,z) \wedge \text{'controls'} \in \text{cell}(x,y) \text{ then add 'read' to cell}(y,z) \}$
- Q: is  $r \in \text{cell}(s,o)$  possible?
  - simple safety queries only
- Main result in the HRU model
  - simple safety is undecidable





# Relating $RT[\Leftarrow, \cap]$ with HRU

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- Role memberships determined by a  $RT[\Leftarrow, \cap]$  state is an access matrix
  - principals correspond to both subjects and objects
  - $K_1 \hat{I} \text{ mem}[K.r]$   
subject  $K_1$  has right  $r$  over object  $K \Leftrightarrow r \hat{I}$   
cell( $K_1, K$ )
- Adding a type-1 statement  $K.r \leftarrow K_1$ 
  - adding  $r$  into cell( $K_1, K$ )



# Relating $RT[\Leftarrow, \cap]$ with HRU

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- Adding a type-2 statement  $K.r \leftarrow K_1.r_1$ 
  - for every  $K'$  such that  $K' \hat{I} \text{ mem}[K_1.r_1]$  add  $r$  into  $\text{cell}(K', K)$
  - need to run an HRU command for every principal
  - this propagation needs to happen every time the matrix is changed

Access Matrix:

	$K_1$	$K_2$	$K_3$	$K_4$
$K_1$				
$K_2$	$r'$	$r$		
$K_3$	$r'$	$r$		
$K_4$	$r'$	$r$	$r'$	

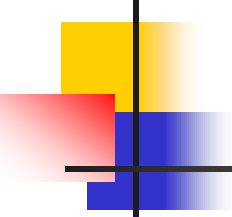
1. Add  $K_2.r \leftarrow K_2$
2. Add  $K_1.r' \leftarrow K_2.r$
3. Add  $K_2.r \leftarrow K_3$
4. Add  $K_2.r \leftarrow K_2.r.r'$
5. Add  $K_3.r' \leftarrow K_4$

Triggers:

2. " $K'$ , execute $rr'(K_1, K_2, K')$
4. " $K', K''$ execute $r'rr(K_2, K', K'')$

$rr'(x, y, z) \{ \text{if } r \hat{I} \text{ cell}(z, y) \text{ then add } r' \text{ to cell}(z, x) \}$

$r'rr(x, y, z) \{ \text{if } r \hat{I} \text{ cell}(z, y) \hat{U} r \hat{I} \text{ cell}(y, x) \text{ then add } r' \text{ to cell}(z, x) \}$



# Can HRU simulate RT? (Probably not!)

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- It seems that HRU cannot simulate RT
  - Adding one statement corresponds to executing multiple HRU commands
  - Seems unable to simulate the effect of propagation
  - Unclear how to simulate removal of statements



# Why Our Problem is Decidable?

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- Note that we consider queries that are more complicated than simple safety
  - e.g., containment analysis
- Some parameters in our analysis problem are simpler
  - no need to consider arbitrary commands
    - only four types of statements
  - restriction rules are static



# Next Lecture

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- Automated Trust Negotiation