

CS590U

# **Access Control: Theory and Practice**

Lecture 12 (February 17)

Constraints in Role Based Access  
Control



# SoD

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- If a sensitive task comprises two steps, then two different users should perform each step.
- E.g. the same user cannot order goods, and authorize payment for those goods.
- Is a security principle that is generally considered to be useful.



# SoD (contd.)

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- More elaborate example:
  - (a) Order goods and record details of order
  - (b) Receive invoice and check against order
  - (c) Receive goods and check against invoice
  - (d) Authorize payment against invoice
  
- A set of SoD requirements:
  - (1) No user performs (a) and (d).
  - (2) At least 3 users to perform all 4 steps.

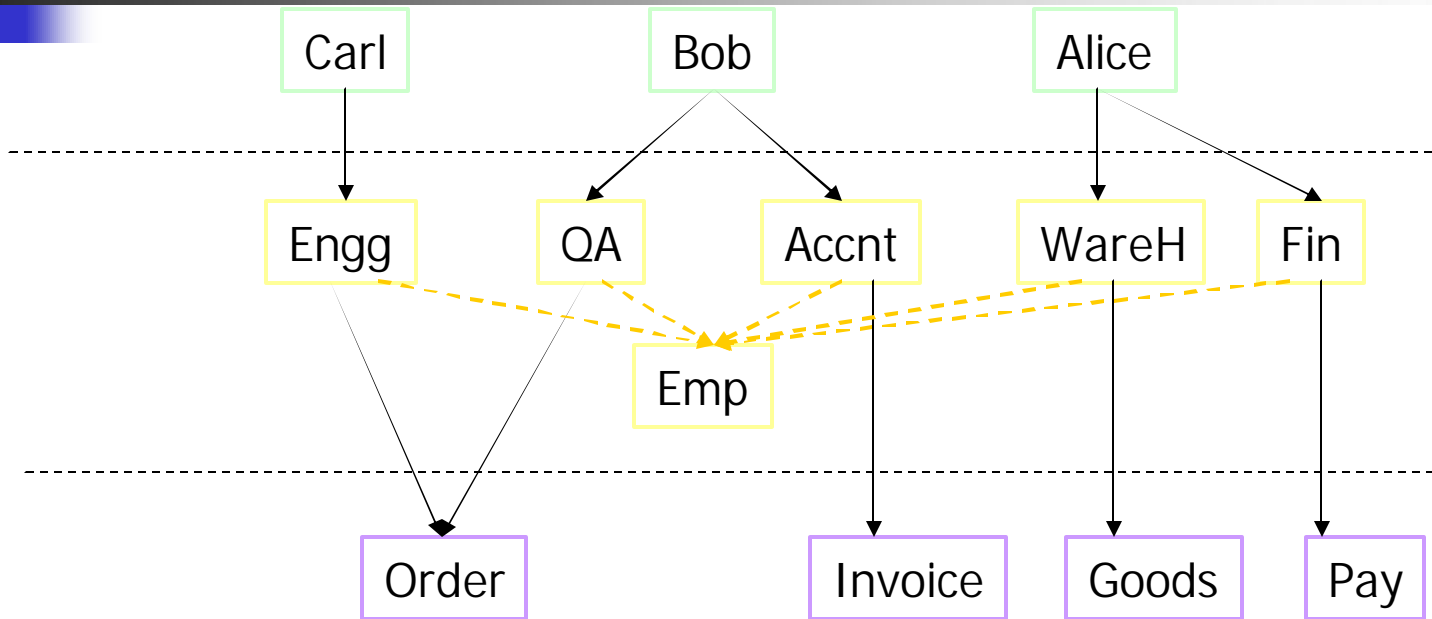


# Enforcement of SoD

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- Static enforcement
  - the permissions to perform two steps are not assigned to a single user
- Dynamic enforcement
  - remember which user performed each step, and don't allow a user to perform the next step if violating SoD policy

# SoD and RBAC



- Static SoD policy:  $ssod(\{ p_1, \dots, p_n \}, k)$ 
  - $e_1 = ssod(\{order, pay\}, 2)$
  - $e_2 = ssod(\{order, invoice, goods, pay\}, 3)$



# SSoD Safety

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- An RBAC state is given by  $\langle UA, PA, RH \rangle$
- **Definition:** An RBAC state  $\gamma$  is safe wrt.  $ssod(\{p_1, \dots, p_n\}, k)$  iff. in  $\gamma$  no  $k-1$  users together have all permissions in  $\{p_1, \dots, p_n\}$ .
- **Definition:** An RBAC state  $\gamma$  is safe wrt. a set  $E$  of SSoD policies iff  $\gamma$  is safe wrt. each  $e$  in  $E$ .
- **Definition:** The SCSSoD problem is to determine whether an RBAC state is safe wrt. a set  $E$  of SSoD policies.



# SCSSOD is coNP-complete

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Proof: Show that determining whether  $\gamma$  is not safe wrt.  $E$  is NP-complete.

**In NP:** if unsafe, then  $\exists$  ssod( $\{p_1, \dots, p_n\}, k$ ) in  $E$ , and  $k-1$  users such that the permissions they have contains  $\{p_1, \dots, p_n\}$ . After guessing  $e$ , and  $k-1$  users, can be verified in polynomial time.

**NP-hard:** The set covering problem: Given a finite set  $S$ ,  $F = \{S_1, \dots, S_m\}$  (where  $S_j \subseteq S$ ),  $B$ , determine whether exist  $B$  members of  $F$  such that their union is  $S$ .

Reduction: each element in  $S$  maps to a permission, each  $S_j$  maps to a user



# SMER Constraints

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- Statically mutually-exclusive role (SMER) constraints:  $\text{smer}(\{r_1, \dots, r_m\}, t)$ 
  - means that no user can be a member of  $t$  roles from  $\{r_1, \dots, r_m\}$
  - $\text{smer}(\{r_1, r_2\}, 2)$  means that  $r_1$  and  $r_2$  are mutually exclusive, i.e., no user can be a member of both roles
- Example:
  - $C = \{c_1, c_2, c_2\}$ , where<sup>8</sup>





# Terminology Confusion in Literature

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- SMER constraints are called SSoD constraints in the literature
  - possible reason: given  $\text{ssod}(\{p_1, p_2\}, 2)$ , if only  $r_1$  has  $p_1$  and only  $r_2$  has  $p_2$ , then making  $r_1$  and  $r_2$  mutually exclusive enforces  $\text{ssod}(\{p_1, p_2\}, 2)$
- Why this is bad?
  - confusing objective with mechanism
  - suppose that one makes  $r_1$  and  $r_2$  exclusive and permission assignment changes, then it may not enforce the SSoD policy anymore



# Even more Terminology Confusion

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- DMER constraints, which require that certain roles cannot be activated in the same session, are called DSoD constraints in the literature
  - because they are dynamic version of “SSoD constraints”
- However, DMER constraints have nothing to do with Separation of Duty; they are motivated by the Least Privilege Principle.



# SMER Constraints and SSoD Policies

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- How effective is it to use SMER constraints to enforce SSoD policies?



# SC-SMER

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- **Definition:** An RBAC state  $\gamma$  satisfies an SMER constraint  $\text{smer}(\{r_1, \dots, r_m\}, t)$  iff. no user is a member of at least  $t$  roles in  $\{r_1, \dots, r_m\}$
- Firstly: can we check whether an RBAC state satisfies an SMER constraint efficiently?
- Yes: for each user
  - compute set of roles of which she is a member
  - intersect with set of roles from constraint
  - check if size  $< t$



# SSoD and SMER

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- Enforcement Verification (EV) problem:  
whether a set  $C$  of SMER constraints enforces  
a set  $E$  of SSoD policies under a given PA and  
RH
  - for all possible user-role assignments, does  
 $\text{satisfies}_C(s) \Rightarrow \text{safe}_E(s)$  ?



# CEV

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- CEV problem: similar to EV, except with
  - Singleton set of SSoD policies
  - Set of canonical SMER constraints
- EV and CEV are coNP-complete
  - Monotone-3-2-SAT reduces to CEV with only 2-2 SMER constraints
  - EV is in coNP

# Monotone 3-2-SAT is NP-complete

- CNF-SAT is to determine whether a list of disjunctive clauses can be satisfied at the same time
  - e.g.,  $(p_1 \vee \neg p_2 \vee \neg p_3) \wedge (p_2 \vee \neg p_3 \vee p_4) \wedge$
- In a monotone 3-2-SAT instance, each clause either consists of 3 positive literals, or 2 negative literals
- Every 3-SAT instance can be transformed to an equivalent 3-2-SAT instance.



# A Special Case of CEV is NP-complete

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- Determining whether a set of 2-2 smer constraints does not enforce a 2-n SSoD policy is NP-complete
- Given a monotone 3-2-SAT instance,
  - for each clause, creates a permission,
  - for each role creates a propositional variable,
  - each positive clause is translated into permission-role assignments
  - each negative clause is translated into a 2-2 smer





# The case in favor of SMER

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- EV needs to be performed only when role-role or permission-role relationships change. These are infrequent.
- When  $(u,r)$  is added to UA, only SC-SMER needs to be checked.
- Complement of CEV reduces to SAT.



# Generation of SMER

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- How did SMER constraints get there in the first place (for us to consider EV)?
- Alternate approach: start with set E of SSoD policies, then generate SMER constraints. Then, EV is inconsequential.
- Naïve approach: make each role mutually exclusive from every other role. But this is too restrictive.

# First Step: From SSoD to RSSoD



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- SSoD policies are about permissions
- SMER constraints are about role memberships
- Need to translate requirements on permissions to those on roles
  - $ssod(\{p_1, \dots, p_n\}, k)$  no  $k-1$  users have all permissions
  - $rssod(\{r_1, \dots, r_n\}, k)$  no  $k-1$  users have all roles
  - $smer(\{r_1, \dots, r_m\}, t)$  no single user has  $t$  or more roles



# A Generation Algorithm

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Input:  $\text{rssod}(R, k)$

Output: SMER constraints

- 1 Let  $n = |R|$ ,  $S = \text{emptyset}$
- 2 If  $k = 2$  output  $\text{smer}(R, n)$
- 3 Else
- 4     for all  $j$  from 2 to  $\text{floor}((n-1)/(k-1)) + 1$
- 5         let  $m = (k-1)(j-1) + 1$
- 6         for each size- $m$  subset  $R'$  of  $R$
- 7             output  $\text{smer}(R', j)$



# Output of the Algorithm

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- If  $k = 2$ , output is  $\text{smer}(R, n)$
- If  $k = n$ , output is  $\text{smer}(R, 2)$
- In other cases, we get multiple outputs. *Each* is sufficient to enforce the RSSoD requirement.
  
- How good is the algorithm?



# Precise Enforcement

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- A set  $C$  of SMER constraints precisely enforces a set  $D$  of RSSoD requirements when for every state  $s$ :
  - $\text{satisfies}_C(s) \Rightarrow \text{safe}_D(s)$
  - $\text{safe}_D(s) \text{ and } \text{live}_D(s) \Rightarrow \text{satisfies}_C(s)$
- Only two cases that precise enforcement is possible for  $\text{rssod}(R, k)$ :
  - $k = 2$
  - $k = n = |R|$



# Minimal Enforcement

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- C is minimal if C enforces D and no other constraint that enforces D is less restrictive.
- If C is precise, then C is minimal.
- The algorithm:
  - Each constraint that is generated is minimal.
  - Every singleton set of constraints that is minimal is generated.



# Next Lecture

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- Administration of RBAC