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- . Maintain only one array $\mathsf{M}[\mathsf{v}]$ = shortest $\mathsf{v}\text{-t}$ path that we have found so far.
- No need to check edges of the form (v, w) unless M[w] changed in previous iteration.

Theorem. Throughout the algorithm, M[v] is length of some v-t path, and after i rounds of updates, the value $M[\nu]$ is no larger than the length of shortest v-t path using \leq i edges.

Overall impact.

- Memory: O(m + n).
- Running time: O(mn) worst case, but substantially faster in practice.





Distance Vector Protocol

Communication network.

- Node ≈ router.
- Edge \approx direct communication link.
- Cost of edge ≈ delay on link. ← naturally nonnegative, but Bellman-Ford used anyway!

Dijkstra's algorithm. Requires global information of network.

Bellman-Ford. Uses only local knowledge of neighboring nodes.

Synchronization. We don't expect routers to run in lockstep. The order in which each foreach loop executes in not important. Moreover, algorithm still converges even if updates are asynchronous.

 Distance vector protocol. Each router maintains a vector of shortest path lengths to every other node (distances) and the first hop on each path (directions). Algorithm: each router performs n separate computations, one for each potential destination node. "Routing by rumor." 	
Ex. RIP, Xerox XNS RIP, Novell'S IPX RIP, Cisco'S IGRP, DEC'S DNA Phase IV, AppleTalk'S RTMP.	
Caveat. Edge costs may change during algorithm (or fail completely).	
$ \underbrace{ \begin{bmatrix} 1 & & \\ & 1 & \\ & 2 & \\ & 1 & \\ & $	

Distance Vector Protocol

Path Vector Protocols

Link state routing.

- Based on Dijkstra's algorithm. . Avoids "counting-to-infinity" problem and related difficulties.
- Requires significantly more storage.

Ex. Border Gateway Protocol (BGP), Open Shortest Path First (OSPF).









- Bellman-Ford. O(mn) time, O(m + n) space.
- Run Bellman-Ford for n iterations (instead of n-1).
- Upon termination, Bellman-Ford successor variables trace a negative cycle if one exists.
- . See p. 304 for improved version and early termination rule.