

Homework 2 Statistics

Minimum Value	40.00
Maximum Value	100.00
Range	60.00
Average	83.79
Median	85.00
Standard Deviation	15.93



Midterm Exam

- Thursday, October 5th at 9 AM (in class)
 - Multiple Choice, True/False, Fill-in-the-Blank
 - 75 minutes
- You may bring one (double sided) index card with notes
- No electronic devices/calculators
- May Incorporate Content from Today's Lecture or Katz and Lindell Chapters 1--6

Final Exam

- **Time:** Tuesday, December 12th at 1PM (Tentative Subject to Change)
- **Location:** LWSN 1106

Recap

- Random Oracle Model
 - Pros (Easier Proofs/More Efficient Protocols/Solid Evidence for Security in Practice)
 - Cons (Strong Assumption)
- Hashing Applications
- Building Stream Ciphers
 - Linear Feedback Shift Registers (+ Attacks)
 - RC4 (+ Attacks)
 - Trivium
- Block Ciphers

Cryptography

CS 555

Week 7:

- Block Ciphers
- Feistel Networks
- DES, 3DES, AES

Readings: Katz and Lindell Chapter 6

CS 555: Week 7: Topic 1

Block Ciphers (Continued)

Review Pseudorandom Permutation

A keyed function $F: \{0,1\}^n \times \{0,1\}^n \rightarrow \{0,1\}^n$, which is invertible and “looks random” without the secret key k .

- Similar to a PRF, but
- Computing $F_k(x)$ and $F_k^{-1}(x)$ is efficient (polynomial-time)

Definition 3.28: A keyed function $F: \{0,1\}^n \times \{0,1\}^n \rightarrow \{0,1\}^n$ is a **strong pseudorandom permutation** if for all PPT distinguishers D there is a negligible function μ s.t.

$$\left| \Pr \left[D^{F_k(\cdot), F_k^{-1}(\cdot)}(1^n) \right] - \Pr \left[D^{f(\cdot), f^{-1}(\cdot)}(1^n) \right] \right| \leq \mu(n)$$

Pseudorandom Permutation

Definition 3.28: A keyed function $F: \{0,1\}^n \times \{0,1\}^n \rightarrow \{0,1\}^n$ is a **strong pseudorandom permutation** if for all PPT distinguishers D there is a negligible function μ s.t.

$$\left| \Pr \left[D^{F_k(\cdot), F_k^{-1}(\cdot)}(1^n) \right] - \Pr \left[D^{f(\cdot), f^{-1}(\cdot)}(1^n) \right] \right| \leq \mu(n)$$

Notes:

- the first probability is taken over the uniform choice of $k \in \{0,1\}^n$ as well as the randomness of D .
- the second probability is taken over uniform choice of $f \in \mathbf{Perm}_n$ as well as the randomness of D .
- D is *never* given the secret k
- However, D is given oracle access to keyed permutation and inverse

How many permutations?

- $|\text{Perm}_n| = ?$
- **Answer:** $2^n!$
- How many bits to store $f \in \text{Perm}_n$?

- **Answer:**

$$\begin{aligned} \log(2^n!) &= \sum_{i=1}^{2^n} \log(i) \\ &\geq \sum_{i=2^{n-1}}^{2^n} (n-1) \geq (n-1) \times 2^{n-1} \end{aligned}$$

How many bits to store permutations?

$$\begin{aligned}\log(2^n!) &= \sum_{i=1}^{2^n} \log(i) \\ &\geq \sum_{i=2^{n-1}}^{2^n} n - 1 \geq (n - 1) \times 2^{n-1}\end{aligned}$$

Example: Storing $f \in \mathbf{Perm}_{50}$ requires over 6.8 petabytes (10^{15})

Example 2: Storing $f \in \mathbf{Perm}_{100}$ requires about 12 yottabytes (10^{24})

Example 3: Storing $f \in \mathbf{Perm}_8$ requires about 211 bytes

Attempt 1: Pseudorandom Permutation

- Select 16 random permutations on 8-bits $f_1, \dots, f_{16} \in \mathbf{Perm}_8$.
- **Secret key:** $k = f_1, \dots, f_{16}$ (about 3 KB)
- **Input:** $x = x_1, \dots, x_{16}$ (16 bytes)

$$F_k(x) = f_1(x_1) \parallel f_2(x_2) \parallel \dots \parallel f_{16}(x_{16})$$

- Any concerns?

Attempt 1: Pseudorandom Permutation

- Select 16 random permutations on 8-bits $f_1, \dots, f_{16} \in \mathbf{Perm}_8$.

$$F_k(x) = f_1(x_1) \parallel f_2(x_2) \parallel \dots \parallel f_{16}(x_{16})$$

- Any concerns?

$$F_k(x_1 \parallel x_2 \parallel \dots \parallel x_{16}) = f_1(x_1) \parallel f_2(x_2) \parallel \dots \parallel f_{16}(x_{16})$$

$$F_k(\mathbf{0} \parallel x_2 \parallel \dots \parallel x_{16}) = \mathbf{f}_1(\mathbf{0}) \parallel f_2(x_2) \parallel \dots \parallel f_{16}(x_{16})$$

- Changing a bit of input produces insubstantial changes in the output.
- A truly random permutation $F \in \mathbf{Perm}_{128}$ would not behave this way!

Pseudorandom Permutation Requirements

- Consider a truly random permutation $F \in \mathbf{Perm}_{128}$
- Let inputs x and x' differ on a single bit
- We expect outputs $F(x)$ and $F(x')$ to differ on approximately half of their bits
 - $F(x)$ and $F(x')$ should be (essentially) independent.
- A pseudorandom permutation must exhibit the same behavior!

Confusion-Diffusion Paradigm

- Our previous construction was not pseudorandom, but apply the permutations do accomplish something
 - They introduce confusion into F
 - Attacker cannot invert (after seeing a few outputs)
- Approach:
 - **Confuse**: Apply random permutations f_1, \dots , to each block of input to obtain y_1, \dots ,
 - **Diffuse**: Mix the bytes y_1, \dots , to obtain bytes z_1, \dots ,
 - **Confuse**: Apply random permutations f_1, \dots , with inputs z_1, \dots ,
 - Repeat as necessary

Confusion-Diffusion Paradigm

Example:

- Select 8 random permutations on 8-bits $f_1, \dots, f_{16} \in \mathbf{Perm}_8$
- Select 8 extra random permutations on 8-bits $g_1, \dots, g_8 \in \mathbf{Perm}_8$

$F_K(x_1 \parallel x_2 \parallel \dots \parallel x_8) =$

1. $y_1 \parallel \dots \parallel y_8 := f_1(x_1) \parallel f_2(x_2) \parallel \dots \parallel f_8(x_8)$

2. $z_1 \parallel \dots \parallel z_8 := \mathbf{Mix}(y_1 \parallel \dots \parallel y_8)$

3. **Output:** $f_1(z_1) \parallel f_2(z_2) \parallel \dots \parallel f_8(z_8)$

Example Mixing Function

Mix($y_1 \parallel \dots \parallel y_8$) =

1. For $i=1$ to 8
2. $z_i := y_1[i] \parallel \dots \parallel y_8[i]$
3. End For
4. **Output:** $g_1(z_1) \parallel g_2(z_2) \parallel \dots \parallel g_8(z_8)$

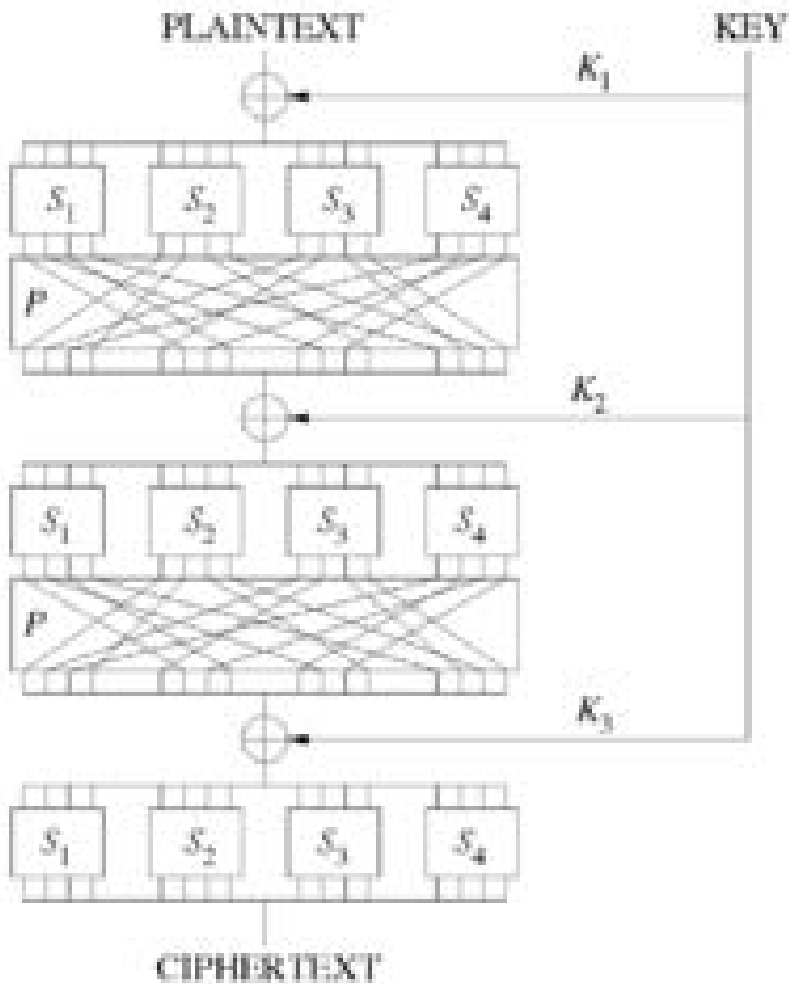
$$y_1 = \left[\begin{array}{c} z_1 \\ y_1[1] \\ \vdots \\ y_8[1] \end{array} \right] \cdots \left[\begin{array}{c} z_8 \\ y_1[8] \\ \vdots \\ y_8[8] \end{array} \right]$$

Substitution Permutation Networks

- S-box a public “substitution function” (e.g. $S \in \mathbf{Perm}_8$).
- S is not part of a secret key, but can be used with one
$$f(x) = S(x \oplus k)$$
- Input to round: x , k (k is subkey for current round)
- **Key Mixing:** Set $x := x \oplus k$
- **Substitution:** $x := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
- **Bit Mixing Permutation:** permute the bits of x to obtain the round output

Note: there are only $n!$ possible bit mixing permutations of $[n]$ as opposed to $2^n!$ Permutations of $\{0,1\}^n$

Substitution Permutation Networks



- **Proposition 6.3:** Let F be a keyed function defined by a Substitution Permutation Network. Then for any keys/number of rounds F_k is a permutation.
- Why? Composing permutations f, g results in another permutation $h(x)=g(f(x))$.

Remarks

- Want to achieve “avalanche effect” (one bit change should “affect” every output bit)
- Should a S-box be a random byte permutation?
- Better to ensure that $S(x)$ differs from x on at least 2-bits (for all x)
 - Helps to maximize “avalanche effect”
- Mixing Permutation should ensure that output bits of any given S-box are used as input to multiple S-boxes in the next round

Remarks

- How many rounds?
- **Informal Argument:** If we ensure that $S(x)$ differs from $S(x')$ on at least 2-bits (for all x, x' differing on at least 1 bit) then every input bit affects
 - 2 bits of round 1 output
 - 4 bits of round 2 output
 - 8 bits of round 3 output
 -
 - 128 bits of round 4 output
- Need at least 7 rounds (minimum) to ensure that every input bit affects every output bit

Attacking Lower Round SPNs

- Trivial Case: One full round with no final key mixing step
- **Key Mixing:** Set $x := x \oplus k$
- **Substitution:** $y := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
- **Bit Mixing Permutation:** P permute the bits of y to obtain the round output

- Given input/output $(x, F_k(x))$
 - Permutations P and S_i are public and can be run in reverse
 - $P^{-1}(F_k(x)) = S_1(x_1 \oplus k_1) \parallel S_2(x_2 \oplus k_2) \parallel \dots \parallel S_8(x_8 \oplus k_8)$
 - $x_i \oplus k_i = S_i^{-1}(S_i(x_i \oplus k_i))$
 - Attacker knows x_i and can thus obtain k_i

Attacking Lower Round SPNs

- Easy Case: One full round with final key mixing step
- **Key Mixing:** Set $x := x \otimes k_1$
- **Substitution:** $y := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
- **Bit Mixing Permutation:** $z_1 \parallel \dots \parallel z_8 = P(y)$
- **Final Key Mixing:** Output $z \oplus k_2$

- Given input/output $(x, F_k(x))$
 - Permutations P and S_i are public and can be run in reverse once k_2 is known
 - Immediately yields attack in 2^{64} time (k_1, k_2 are each 64 bit keys) which narrows down key-space to 2^{64} but we can do much better!

Attacking Lower Round SPNs

- Easy Case: One full round with final key mixing step
- **Key Mixing:** Set $x := x \oplus k_1$
- **Substitution:** $y := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
- **Bit Mixing Permutation:** $z_1 \parallel \dots \parallel z_8 = P(y)$
- **Final Key Mixing:** Output $z \oplus k_2$

- Given input/output $(x, F_k(x))$
 - Permutations P and S_i are public and can be run in reverse once k_2 is known
 - Guessing 8 specific bits of k_2 (which bits depends on P) we can obtain one value $y_i = S_i(x_i \otimes k_i)$
 - Attacker knows x_i and can thus obtain k_i by inverting S_i and using XOR
 - Narrows down key-space to 2^{64} , but in time 8×2^8

Attacking Lower Round SPNs

- Easy Case: One full round with final key mixing step
- **Key Mixing:** Set $x := x \oplus k_1$
- **Substitution:** $y := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
- **Bit Mixing Permutation:** $z_1 \parallel \dots \parallel z_8 = P(y)$
- **Final Key Mixing:** Output $z \oplus k_2$

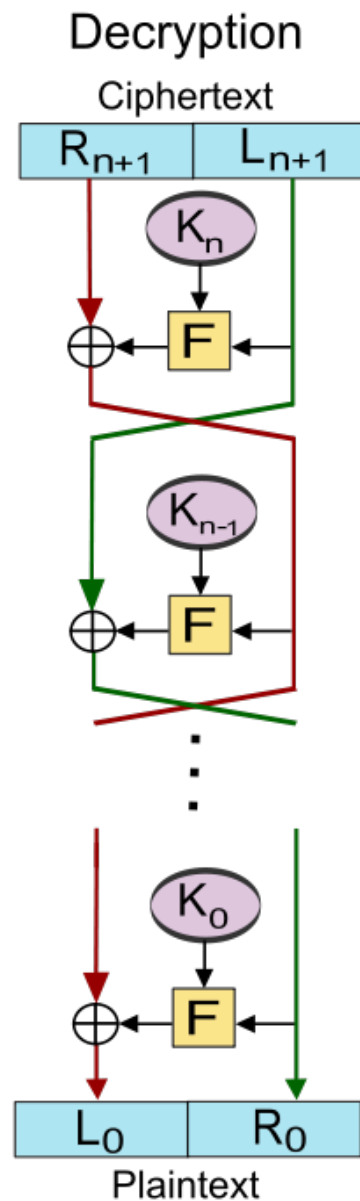
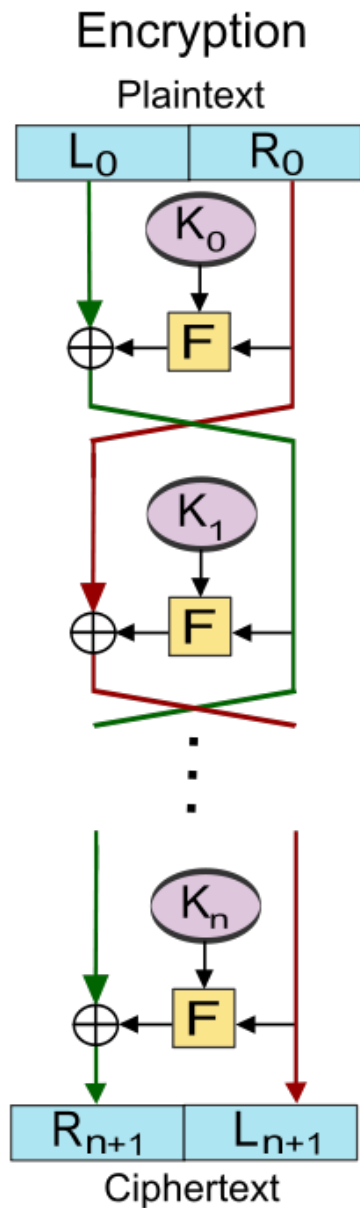
- Given several input/output pairs $(x_j, F_k(x_j))$
 - Can quickly recover k_1 and k_2

Attacking Lower Round SPNs

- Harder Case: Two round SPN
- Exercise 😊

Feistel Networks

- Alternative to Substitution Permutation Networks
- **Advantage:** underlying functions need not be invertible, but the result is still a permutation



- $R_{i-1} = L_i$
- $L_{i-1} := R_i \oplus F_{k_i}(R_{i-1})$

Proposition: the function is invertible.

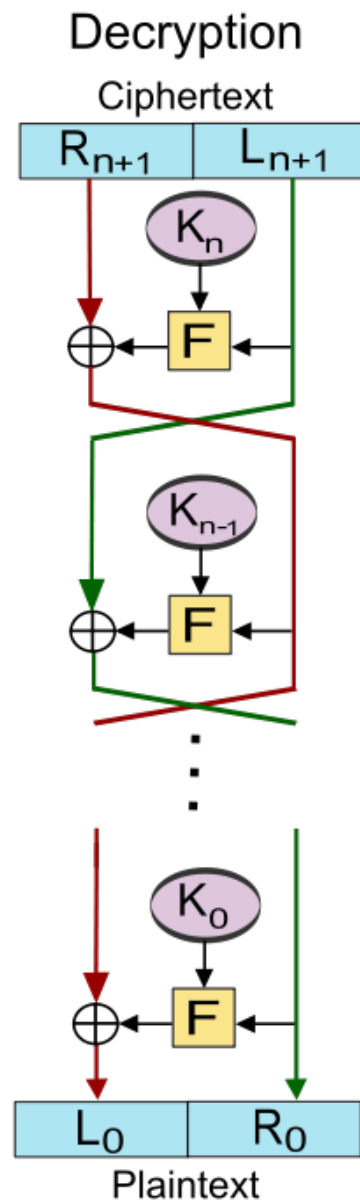
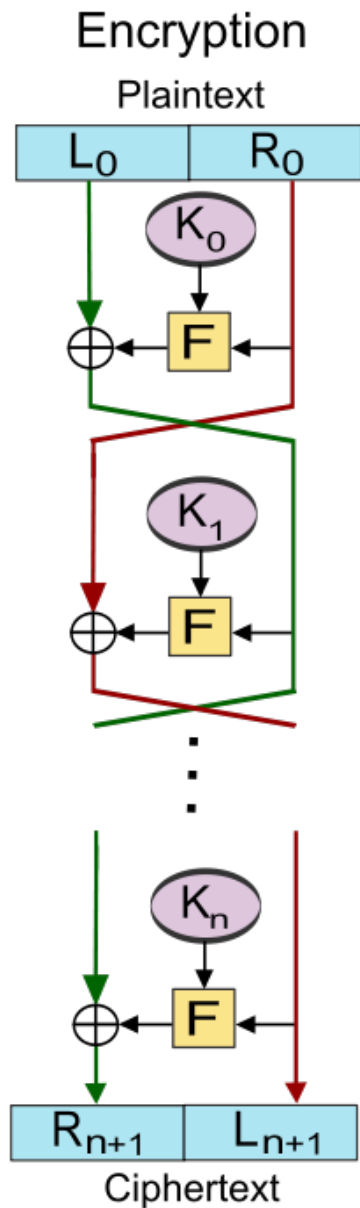
Digital Encryption Standard (DES): 16-round Feistel Network.

CS 555: Week 7: Topic 2

DES, 3DES, AES

Feistel Networks

- Alternative to Substitution Permutation Networks
- **Advantage:** underlying functions need not be invertible, but the result is still a permutation



- $L_{i+1} = R_i$
- $R_{i+1} := L_i \oplus F_{K_i}(R_i)$

Proposition: the function is invertible.

Data Encryption Standard

- Developed in 1970s by IBM (with help from NSA)
- Adopted in 1977 as Federal Information Processing Standard (US)
- Data Encryption Standard (DES): 16-round Feistel Network.
- Key Length: 56 bits
 - Vulnerable to brute-force attacks in modern times
 - 1.5 hours at 14 trillion keys/second (e.g., Antminer S9)

DES Round

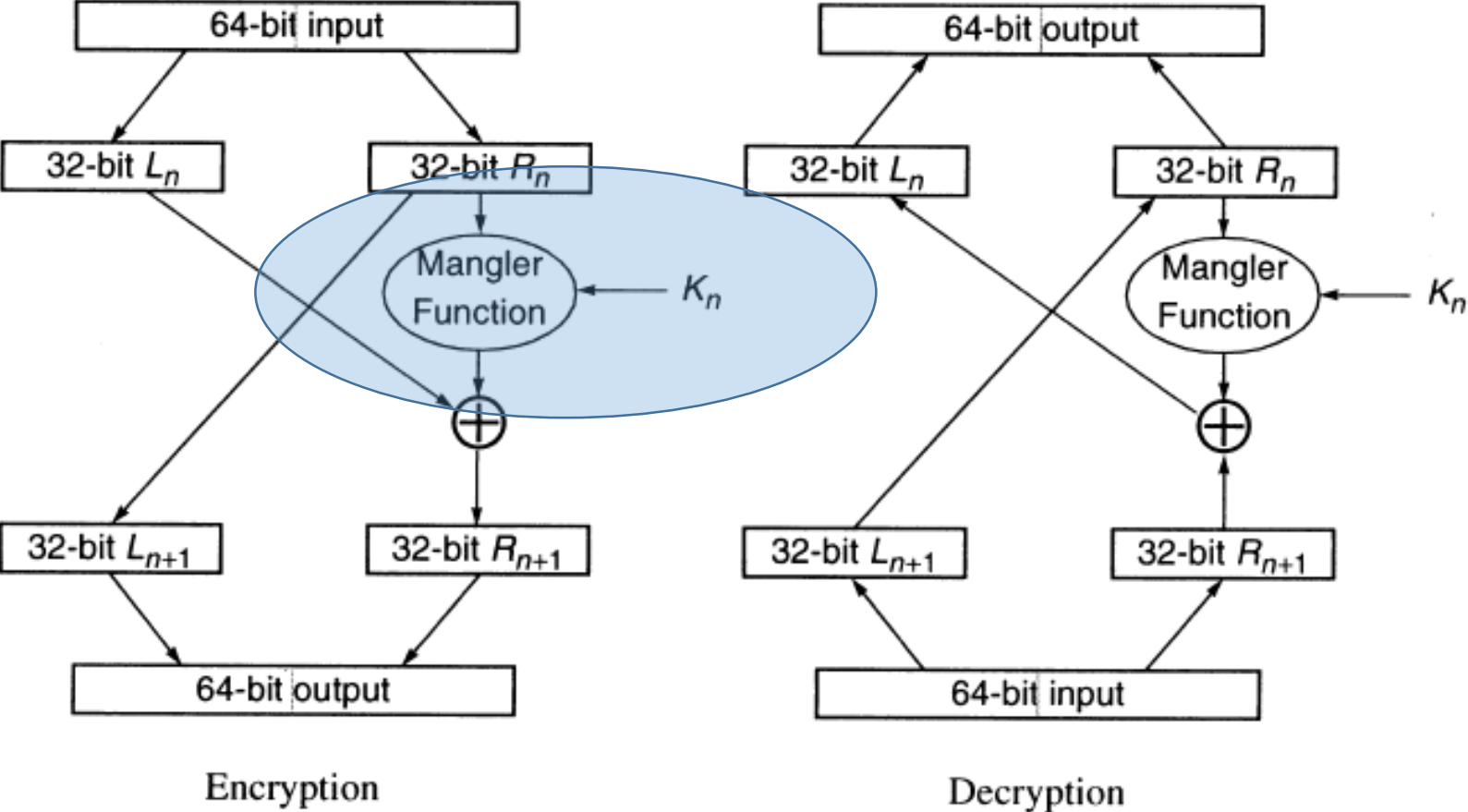
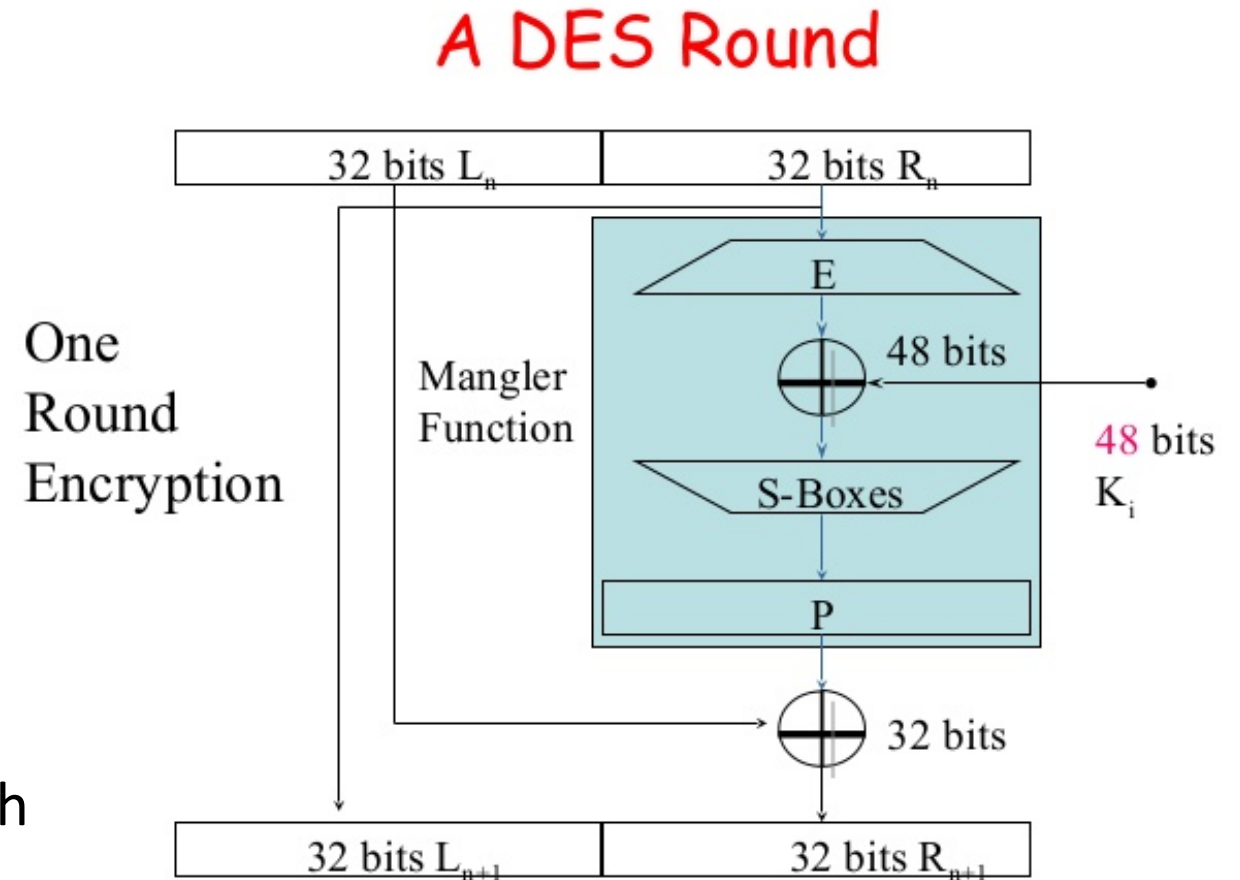


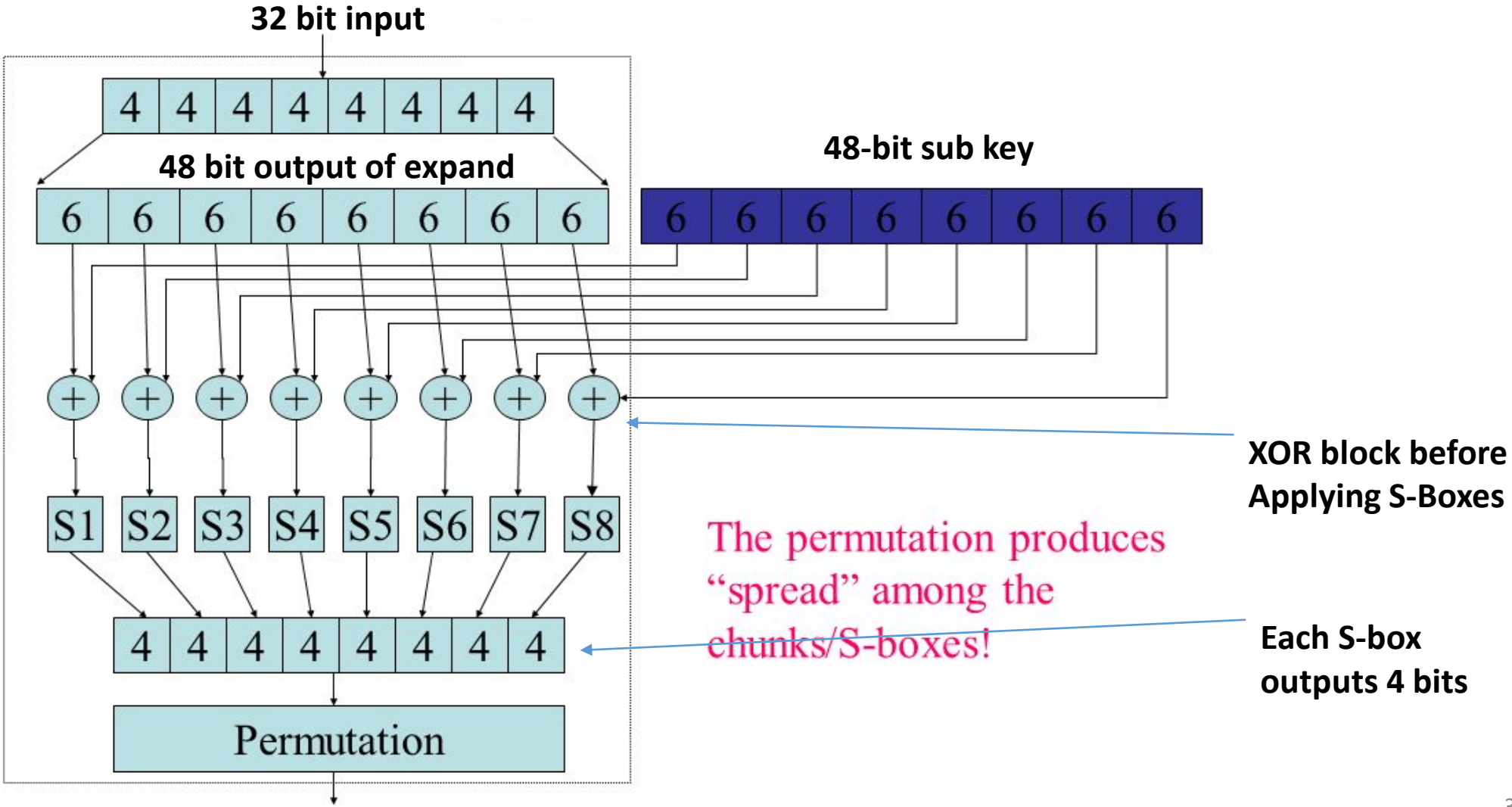
Figure 3-6. DES Round

DES Mangle Function

- Expand E: 32-bit input \rightarrow 48-bit output (duplicates 16 bits)
- S-boxes: S_1, \dots, S_8
 - Input: 6-bits
 - Output: 4 bits
 - Not a permutation!
- 4-to-1 function
 - Exactly four inputs mapped to each possible output



Mangle Function



S-Box Representation as Table

4 columns (2 bits)

16 columns (4 bits)

	00	01	10	11
0000				
0001				
0010				
0011				
0100				
0101				
0110				S(x)=1101
...
1111				

$x = 101101$

$S(x) = \text{Table}[0110, 11]$

S-Box Representation

Each column is permutation

4 columns (2 bits)

16 columns (4 bits)

	00	01	10	11
0000				
0001				
0010				
0011				
0100				
0101				
0110				S(x)=1101
...
1111				

$$x = 101101$$

$$S(x) = T[0110, 11]$$

Pseudorandom Permutation Requirements

- Consider a truly random permutation $F \in \mathbf{Perm}_{128}$
- Let inputs x and x' differ on a single bit
- We expect outputs $F(x)$ and $F(x')$ to differ on approximately half of their bits
 - $F(x)$ and $F(x')$ should be (essentially) independent.
- A pseudorandom permutation must exhibit the same behavior!
- **Requirement:** DES Avalanche Effect!

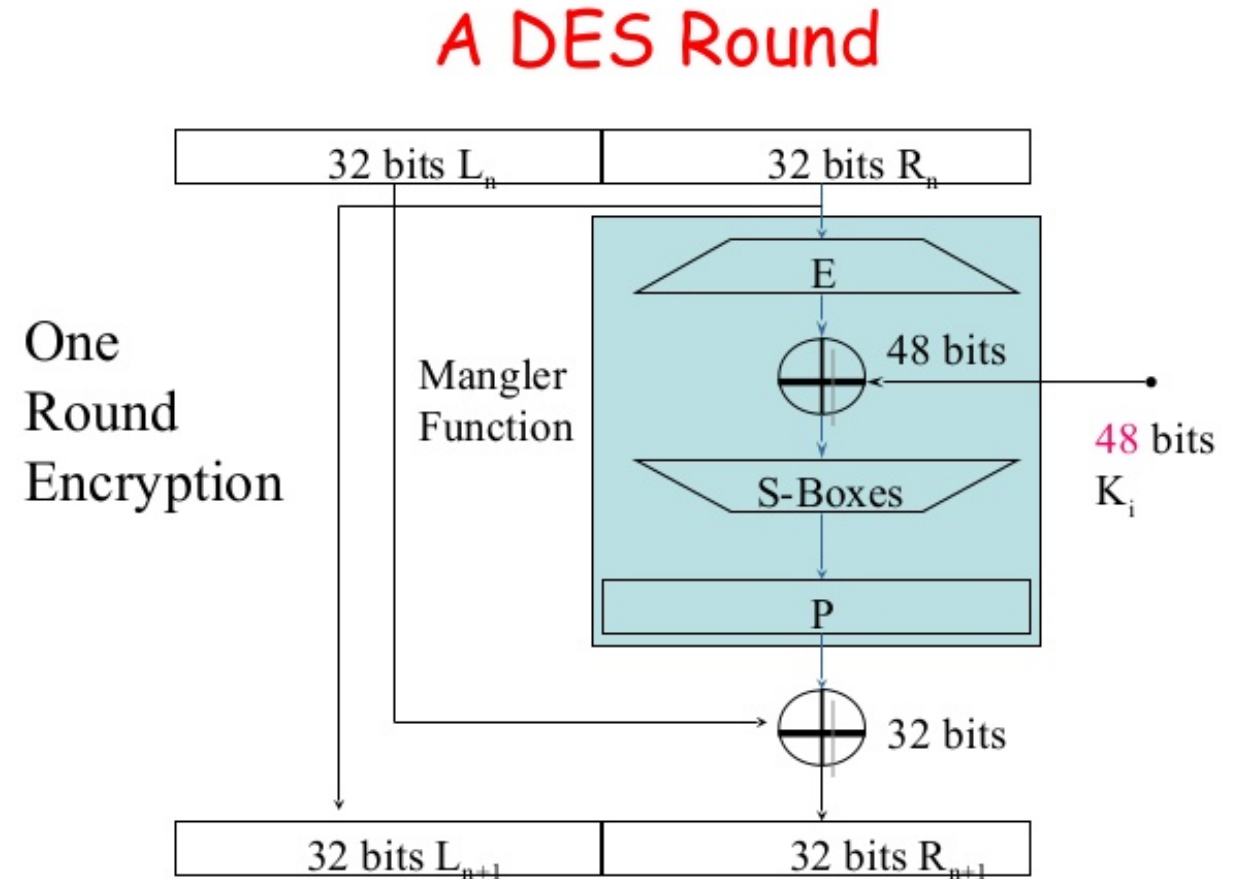
DES Avalanche Effect

- Permutation the end of the mangle function helps to mix bits
- Special S-box property #1

Let x and x' differ on one bit then $S_i(x)$ differs from $S_i(x')$ on two bits.

Avalanche Effect Example

- Consider two 64 bit inputs
 - (L_n, R_n) and $(L'_n, R'_n = R_n)$
 - L_n and L'_n differ on one bit
- This is worst case example
 - $L_{n+1} = L'_{n+1} = R_n$
 - But now R'_{n+1} and R_{n+1} differ on one bit
- Even if we are unlucky $E(R'_{n+1})$ and $E(R_{n+1})$ differ on 1 bit
- $\rightarrow R_{n+2}$ and R'_{n+2} differ on two bits
- $\rightarrow L_{n+2} = R'_{n+1}$ and $L'_{n+2} = R'_{n+1}$ differ in one bit



Avalanche Effect Example

- R_{n+2} and R'_{n+2} differ on two bits
- $L_{n+2} = R_{n+1}$ and $L_{n+2}' = R'_{n+1}$ differ in one bit

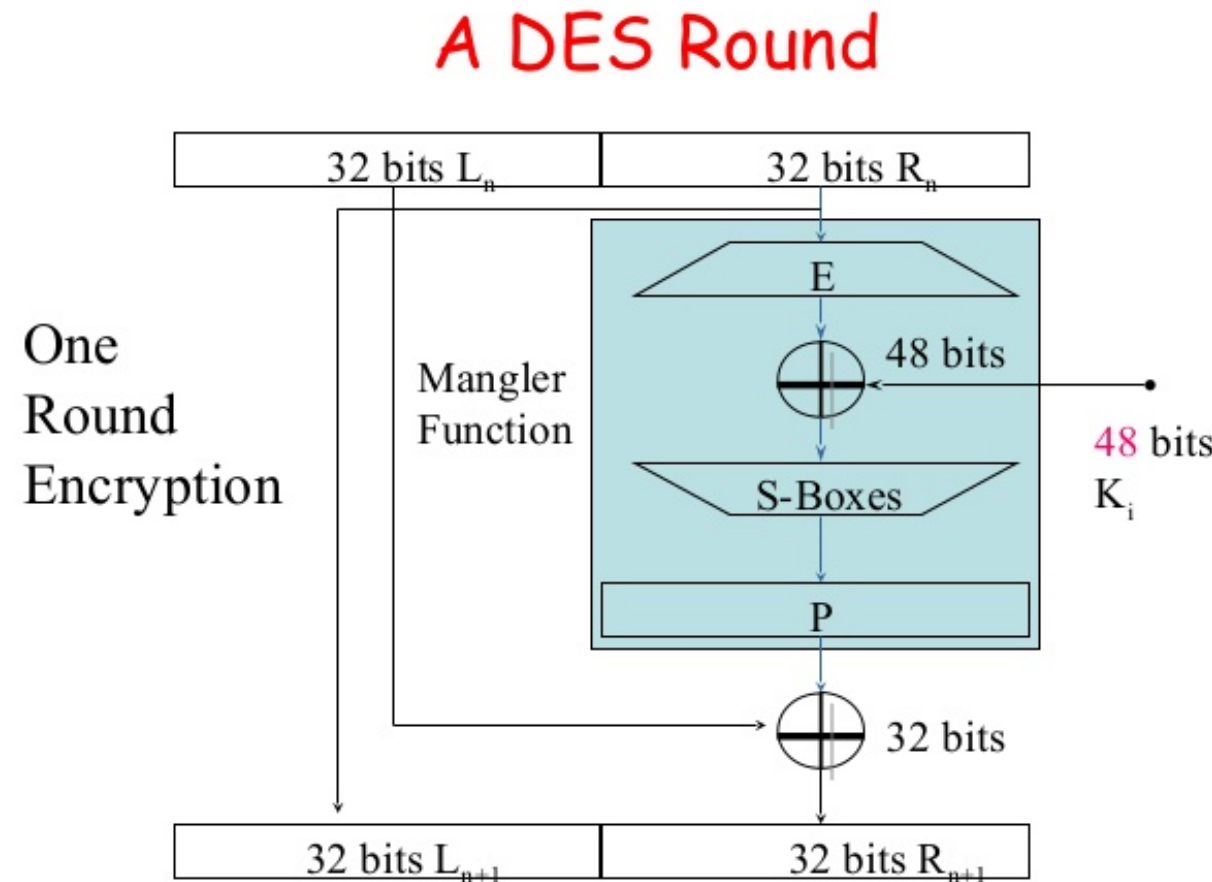
→ R_{n+3} and R'_{n+3} differ on four bits since we have different inputs to two of the S-boxes

→ $L_{n+3} = R'_{n+2}$ and $L_{n+2}' = R'_{n+2}$ now differ on two bits

- Seven rounds we expect all 32 bits in right half to be “affected” by input change

...

DES has sixteen rounds



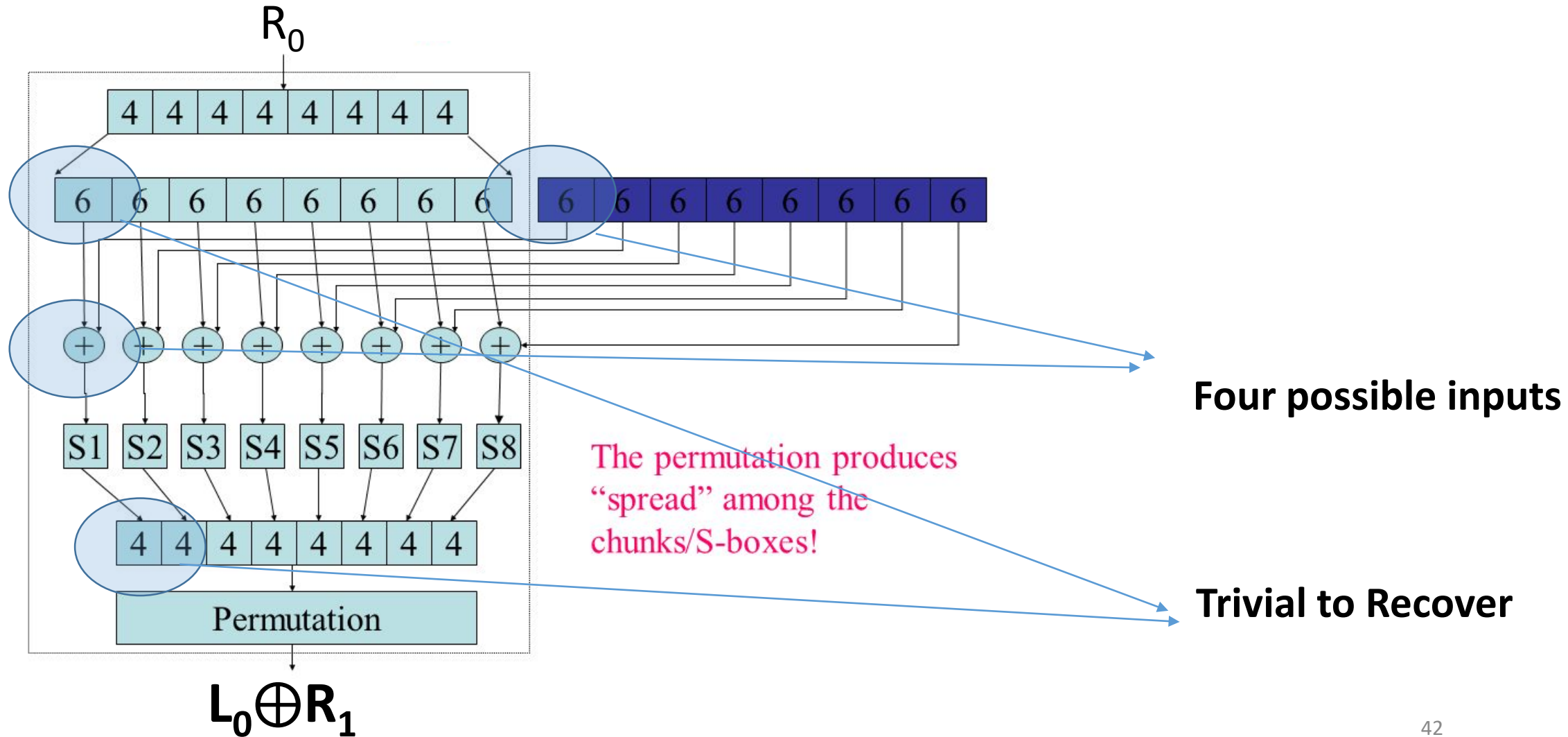
Attack on One-Round DES

- Given input/output pair (x,y)
 - **Output:** $y=(L_1,R_1)$
 - **Input:** $X=(L_0,R_0)$
- Note: $R_0=L_1$
- Note: $R_1=L_0 \oplus f_1(R_0)$ where f is the Mangling Function with key k_1

Conclusion:

$$f_1(R_0)=L_0 \oplus R_1$$

Attack on One-Round DES



Attack on Two-Round DES

- Output $y = (L_2, R_2)$
- Note: $R_1 = L_0 \oplus f_1(R_0)$
 - Also, $R_1 = L_2$
 - Thus, $f_1(R_0) = L_2 \oplus L_0$
- So we can still attack the first round key k_1 as before as R_0 and $L_2 \oplus L_0$ are known
- Note: $R_2 = L_1 \oplus f_2(R_1)$
 - Also, $L_1 = R_0$ and $R_1 = L_2$
 - Thus, $f_2(L_2) = R_2 \oplus R_0$
- So we can attack the second round key k_2 as before as L_2 and $R_2 \oplus R_0$ are known

Attack on Three-Round DES

$$\begin{aligned} f_1(\mathbf{R}_0) \oplus f_3(\mathbf{R}_2) &= (L_0 \oplus L_2) \oplus (L_2 \oplus R_3) \\ &= L_0 \oplus R_3 \end{aligned}$$

We know all of the values L_0, R_0, R_3 and $L_3 = R_2$.

Leads to attack in time $\approx 2^{n/2}$

(See details in textbook)

Remember that DES is 16 rounds

DES Security

- Best Known attack is brute-force 2^{56}
 - Except under unrealistic conditions (e.g., 2^{43} known plaintexts)
- Brute force is not too difficult on modern hardware
- Attack can be accelerated further after precomputation
 - Output is a few terabytes
 - Subsequently keys are cracked in 2^{38} DES evaluations (minutes)
- Precomputation costs amortize over number of DES keys cracked

- Even in 1970 there were objections to the short key length for DES

Double DES

- Let $F_k(x)$ denote the DES block cipher
- A new block cipher F' with a key $k = (k_1, k_2)$ of length $2n$ can be defined by

$$F'_k(x) = F_{k_2}(F_{k_1}(x))$$

- Can you think of an attack better than brute-force?

Meet in the Middle Attack

$$F'_k(x) = F_{k_2} \left(F_{k_1}(x) \right)$$

Goal: Given $(x, c = F'_k(x))$ try to find secret key k in time and space $O(n2^n)$.

- **Solution?**

- **Key Observation**

$$F_{k_1}(x) = F_K^{-1}(c)$$

- **Compute $F_K^{-1}(c)$ and $F_K(x)$ for each potential key K and store $(K, F_K^{-1}(c))$ and $(K, F_K(x))$**
 - **Sort each list of pairs (by $F_K^{-1}(c)$ or $F_K(x)$) to find K_1 and K_2 .**

Triple DES Variant 1

- Let $F_k(x)$ denote the DES block cipher
- A new block cipher F' with a key $k = (k_1, k_2, k_3)$ of length $2n$ can be defined by

$$F'_k(x) = F_{k_3} \left(F_{k_2}^{-1} \left(F_{k_1}(x) \right) \right)$$

- Meet-in-the-Middle Attack Requires time $\Omega(2^{2n})$ and space $\Omega(2^{2n})$

Triple DES Variant 1

Allows backward compatibility with DES by setting $k_1=k_2=k_3$

- Let $F_k(x)$ denote the DES block cipher
- A new block cipher F' with a key $k = (k_1, k_2, k_3)$ of length $2n$ can be defined by

$$F'_k(x) = F_{k_3} \left(F_{k_2}^{-1} \left(F_{k_1}(x) \right) \right)$$

- Meet-in-the-Middle Attack Requires time $\Omega(2^{2n})$ and space $\Omega(2^{2n})$

Triple DES Variant 2

Just two keys!



- Let $F_k(x)$ denote the DES block cipher
- A new block cipher F' with a key $k = (k_1, k_2)$ of length $2n$ can be defined by

$$F'_k(x) = F_{k_1} \left(F_{k_2}^{-1} \left(F_{k_1}(x) \right) \right)$$

- Meet-in-the-Middle Attack still requires time $\Omega(2^{2n})$ and space $\Omega(2^{2n})$
- Key length is still just 112 bits (128 bits is recommended)

Triple DES Variant 1

$$F'_k(x) = F_{k_3} \left(F_{k_2}^{-1} \left(F_{k_1}(x) \right) \right)$$

- Standardized in 1999
- Still widely used, but it is relatively slow (three block cipher operations)
 - Now viewed as “weak cipher” by OpenSSL
- Current gold standard: AES

Advanced Encryption Standard (AES)

- (1997) US National Institute of Standards and Technology (NIST) announces competition for new block cipher to replace DES
- Fifteen algorithms were submitted from all over the world
 - Analyzed by NIST
- Contestants given a chance to break competitors schemes
- October, 2000 NIST announces a winner Rijndael
 - Vincent Rijmen and Joan Daemen
 - No serious vulnerabilities found in four other finalists
 - Rijndael was selected for efficiency, hardware performance, flexibility etc...

Advanced Encryption Standard

- **Block Size:** 128 bits (viewed as 4x4 byte array)
- **Key Size:** 128, 192 or 256
- Essentially a Substitution Permutation Network
 - **AddRoundKey:** Generate 128-bit sub-key from master key XOR with current state
 - **SubBytes:** Each byte of state array (16 bytes) is replaced by another byte according a a single S-box (lookup table)
 - **ShiftRows** – shift ith row by i bytes
 - **MixColumns** – permute the bits in each column

Substitution Permutation Networks

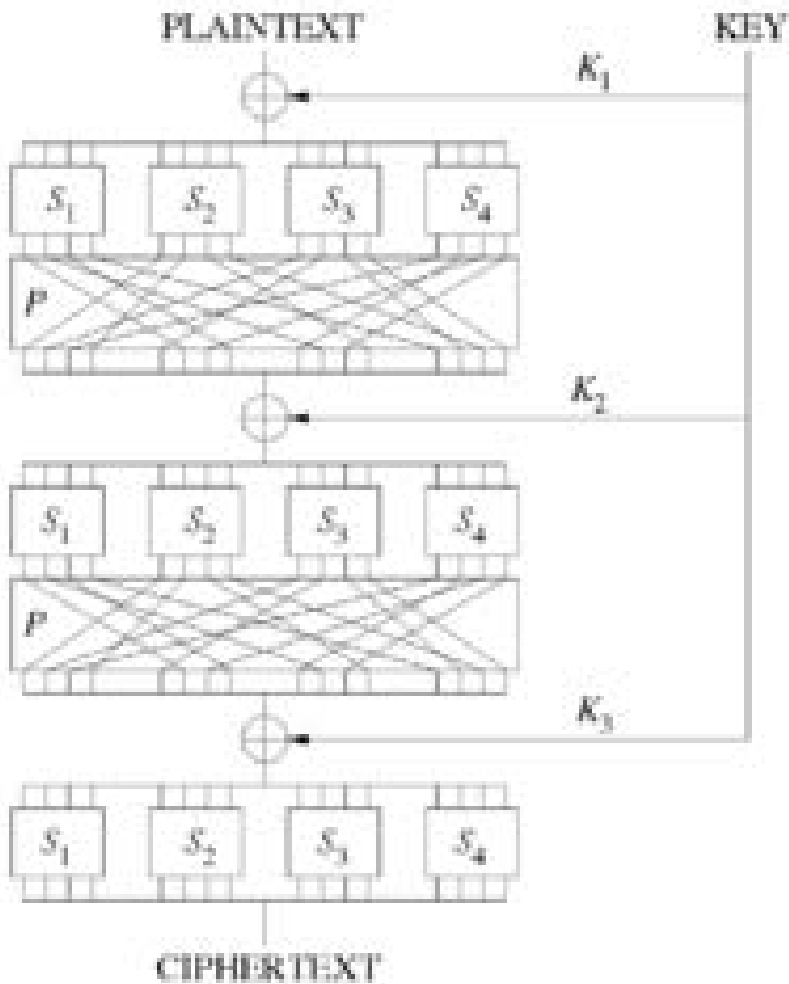
- S-box a public “substitution function” (e.g. $S \in \mathbf{Perm}_8$).
- S is not part of a secret key, but can be used with one
$$f(x) = S(x \oplus k)$$

Input to round: x , k (k is subkey for current round)

1. **Key Mixing:** Set $x := x \oplus k$
2. **Substitution:** $x := S_1(x_1) \parallel S_2(x_2) \parallel \dots \parallel S_8(x_8)$
3. **Bit Mixing Permutation:** permute the bits of x to obtain the round output

Note: there are only $n!$ possible bit mixing permutations of $[n]$ as opposed to $2^n!$ Permutations of $\{0,1\}^n$

Substitution Permutation Networks



- **Proposition 6.3:** Let F be a keyed function defined by a Substitution Permutation Network. Then for any keys/number of rounds F_k is a permutation.
- Why? Composing permutations f, g results in another permutation $h(x)=g(f(x))$.

Advanced Encryption Standard

- Block Size: 128 bits
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 - **ShiftRows**
 - **MixColumns**
- Key Mixing**
- Permutation**
- Substitution**
-

AddRoundKey:



Round Key (16 Bytes)

00001111			
10100011	...		
11001100		...	
01111111			...



State

11110000			
01100010	...		
00110000		...	
11111111			...

=

11111111			
11000001	...		
11111100		...	
10000000			...

AddRoundKey:



Round Key (16 Bytes)

10100011	...		
		...	
			...

State

11111111			
11000001	...		
11111100		...	
10000000			...

SubBytes (Apply S-box)

S(11111111)			
S(11000001)	S(...)		
S(11111100)		S(...)	
S(10000000)			S(...)

AddRoundKey:



Round Key (16 Bytes)

10100011	...		
		...	
			...

State

S(11111111)			
S(11000001)	S(...)		
S(11111100)		S(...)	
S(10000000)			S(...)

Shift Rows

S(11111111)			
	S(11000001)	S(...)	
S(...)		S(11111100)	
		S(...)	S(10000000)

AddRoundKey:



Round Key (16 Bytes)

10100011	...		
		...	
			...

State

S(11111111)			
	S(11000001)	S(...)	
S(...)		S(11111100)	
		S(...)	S(10000000)

Mix Columns

Invertible (linear) transformation.

Key property: if inputs differ in $b > 0$ bytes then output differs in $5 \cdot b$ bytes (minimum)

AES

- We just described one round of the SPN
- AES uses
 - 10 rounds (with 128 bit key)
 - 12 rounds (with 192 bit key)
 - 14 rounds (with 256 bit key)



AES Attacks?

- Side channel attacks affect a few specific implementations
 - But, this is not a weakness of AES itself
 - Timing attack on OpenSSL's implementation AES encryption (2005, Bernstein)
- (2009) Attack on 11 round version of AES
 - recovers 256-bit key in time 2^{70}
 - But AES is 14 round (with 256 bit key) so the attack doesn't apply in practice
- (2009) Attack on 192-bit and 256 bit version of AES
 - recovers 256-bit key in time $2^{99.5}$.
- First public cipher approved by NSA for Top Secret information