## Index

for dissections in Ernest Irving Freese's Geometric Transformations. A book page number such as 38 appears as itself, and a manuscript plate number such as Plate 6 is referenced as M6. Let $\{n\}$ denote a regular polygon of $n$ sides. Let $\{p / q\}$ denote a star with $p$ points, where each point is connected to its $q$-th nearest point in a clockwise direction. Let $\{\tilde{3}\}$ denote a triangle that is not equilateral.
\{3\}
to $\{\tilde{3}\}, \quad 38, \mathrm{M} 3, \mathrm{M} 7$
two to three $\{\tilde{3}\}, \quad$ M7
three to one $\{\tilde{3}\}, \quad$ M7
for $(\sin \pi / 3)^{2}+(\cos \pi / 3)^{2}=1, \quad 40, \mathrm{M} 6$
for $1^{2}+3^{2}+5^{2}+7^{2}=(\sqrt{84})^{2}, \quad 47,48$, M21
for $1^{2}+2^{2}+3^{2}+4^{2}+5^{2}+6^{2}=(\sqrt{91})^{2}, \quad 49, \mathrm{M} 21$
for $2^{2}+5^{2}+8^{2}+11^{2}+14^{2}+17^{2}+20^{2}+23^{2}+26^{2}=48^{2}, \quad \mathrm{M} 22$
two to one, M14
two unequal to one, M6
three to one, M14
four to three, M20
five to one, M15
seven to one, M16, M17
seven to three, M19
nine to four, 43, M9
twelve to one, M19
thirteen to one, M16, M18
sixteen to nine, 44, M10
$\{\tilde{3}\}$
to $\{\tilde{3}\}, \quad \mathrm{M} 3, \mathrm{M} 6$
to two $\{\tilde{3}\} \mathrm{s}, \quad \mathrm{M} 1, \mathrm{M} 2, \mathrm{M} 6$
to ten $\{\tilde{3}\} \mathrm{s}, \quad 184, \mathrm{M} 196$
to ten $\{6\} \mathrm{s}, \mathrm{M} 195$
one to three $\{3\}, \quad \mathrm{M} 7$
two to another, $38, \mathrm{M} 1, \mathrm{M} 2, \mathrm{M} 6$
nine to four, 43
sixteen to nine, 44
\{4\}
to $\{\tilde{3}\}, \quad 41,42,183 \mathrm{M} 8, \mathrm{M} 27, \mathrm{M} 28, \mathrm{M} 193$
one to two $\{\tilde{3}\} \mathrm{s}, \quad \mathrm{M} 27$

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one to \(\{\tilde{3}\}\) and to another \(\{\tilde{3}\}, \quad 54, \mathrm{M} 28\)
to \(\{3\}, \quad 6, \mathrm{M} 8, \mathrm{M} 79\)
one to two \(\{3\}, \quad\) M20
two to one \(\{3\}, 42\), M9
three to one \(\{3\}, \quad\) M10
for \(1^{2}+(\sqrt{3})^{2}+(\sqrt{5})^{2}+(\sqrt{7})^{2}+3^{2}+(\sqrt{11})^{2}=6^{2}, \quad 58\), M40
for \((\sqrt{2})^{2}+(\sqrt{3})^{2}+2^{2}=3^{2}, \quad\) M38
for \(2^{2}+4^{2}+5^{2}+6^{2}=9^{2}, \quad 58\), M39
for \(2^{2}+5^{2}+8^{2}+11^{2}+14^{2}+17^{2}+20^{2}+23^{2}+26^{2}=48^{2}, \quad \mathrm{M} 42\)
for \(7^{2}+15^{2}+23^{2}+31^{2}=42^{2}, \quad 60\)
for \(8^{2}+9^{2}+12^{2}=17^{2}, \quad 58\)
for \(8^{2}+15^{2}=17^{2}, \quad 149\)
for \(9^{2}+12^{2}+20^{2}=25^{2}, \quad\) M39
for \(13^{2}+19^{2}+25^{2}+31^{2}=46^{2}, \quad 59\), M41
for \(4 \times 21^{2}=7^{2}+15^{2}+23^{2}+31^{2}, \quad 60, \mathrm{M} 43\)
one to two unequal, 4, 5, 149, M35, M148
three to one, M36
five to one, M37
five to two, M37
seven to one, M36
eight to one, M37
nine to one and to two, M37
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to \(\{4\}\), M33, M34, M44
to two given squares, M144
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to \(\{4\}, 61,63,64, \mathrm{M} 45\)
to hollow square, M46
3 -square with 1 -square hole
to \(\{4\}, 62\)
to \(\{3\}, \quad\) M47
to \(\{\tilde{3}\}, \quad 39, \mathrm{M} 4\)
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\{5\}
to $\{4\}, \mathrm{M} 48$
two and two $\{3\}$ s to $\{4\}, \quad 178, \mathrm{M} 185$
for $(\sin \pi / 5)^{2}+(\cos \pi / 5)^{2}=1, \quad 72, \mathrm{M} 56$
two to one, 68, M50
two unequal to one, $71, \mathrm{M} 55, \mathrm{M} 56$
four to one, M51
five to one, 9,69 , M51, M52
nine to one, 70, M53
sixteen to one, M54
to $\{\tilde{3}\}$ s of areas 1 and 4 , M5
to pentagram and co-pentagram, M171
two equal to $\{4\}$, M57
to squares of areas $1,2,3$, and $4,75, \mathrm{M} 58$
$\{5 / 2\}$
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five to one, $76, \mathrm{M} 60$
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to five $\{5\} \mathrm{s}, \quad 80,82, \mathrm{M} 62$
\{6\}
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to $\{5\}, \quad \mathrm{M} 49$
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three to one, M69
four to one, M69, M87
four to three, 91, M75
six to one, $89, \mathrm{M} 70$
seven to one, M71
seven to three, M72
nine to one, M76
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twelve to one, M72
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forty-nine to one, M163
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    to two {3}s, M81
    to three {3}s, 95, M81
    to four {3}s, 97, M83
    to five {3}s, 50, M24
    to eight {3}s, M76
    to twelve {3}s, 98, M84
    to fourteen {3}s, M72
    to twenty {3}s, M25
    two to one {3}, 49, M23
    two to three {3}s, M76
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    to hexagram and co-hexagram, M171
    to three rhombuses, M173
    right-angled hexagon to rectangle, M145
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    to {3}, 8, 99, M85
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{7}
    for }(\operatorname{sin}\pi/7\mp@subsup{)}{}{2}+(\operatorname{cos}\pi/7\mp@subsup{)}{}{2}=1,\quad7
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three to one, 108, M94
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\{16\}
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two to one, M137
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$\{20\}$
to $\{4\}, 143, \mathrm{M} 138$
two to one, M139
\{24\}
to $\{4\}, \quad 145, \mathrm{M} 140$
two to one, M141
$\{30\}$
to $\{\tilde{3}\} \mathrm{s}$ of areas $1,4,9$, and $16, \mathrm{M} 5$
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to $\{4\}, \quad \mathrm{M} 157$
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to $\{3\}, 27, \mathrm{M} 19$
to $\{4\}$, M30
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to two $\{4\} \mathrm{s}, \mathrm{M} 30, \mathrm{M} 154$
two to $\{4\}, \mathrm{M} 29$
four to $\{4\}, \mathrm{M} 29$
two to one, M31
four to one, M31
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pendulum
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