## Index

for dissections in *Ernest Irving Freese's Geometric Transformations*. A book page number such as 38 appears as itself, and a manuscript plate number such as Plate 6 is referenced as M6. Let  $\{n\}$  denote a regular polygon of n sides. Let  $\{p/q\}$  denote a star with p points, where each point is connected to its q-th nearest point in a clockwise direction. Let  $\{\tilde{3}\}$  denote a triangle that is not equilateral.

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