



**PURDUE**  
UNIVERSITY

CS52600:  
Information Security

*Information Flow*  
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What is the point?  
*Information Flow*

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- Policy governs flow of information
  - *How do we ensure information flows only through governed channels?*
- State transition attempts to capture this
  - We may return to this later
- Next: How do we measure/capture flow?
  - Entropy-based analysis
    - Change in entropy  $\Rightarrow$  flow
  - Confinement
    - “Cells” where information does not leave
  - Language/compiler based mechanisms?
    - Type-based tracking of flow
  - Guards



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## Information Flow



- Information Flow: Where information can move in the system
- How does this relate to confidentiality policy?
  - Confidentiality: What subjects can see what objects
  - Flow: Controls what subjects actually see
- Variable  $x$  holds information classified  $S$ 
  - $\underline{x}$ , information flow class of  $x$ , is  $S$
- Confidentiality specifies what is allowed
- Information flow describes how this is enforced

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## Formal Definition



- Problem: capturing *all* information flow
  - Files
  - Memory
  - Page faults
  - CPU use
  - ?
- Definition: Based on *entropy*
  - Flow from  $x$  to  $y$  (times  $s$  to  $t$ ) if  $H(x_s | y_t) < H(x_s | y_s)$

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## What is Entropy?



- Idea: Entropy captures *uncertainty*
  - $H(X) = -\sum_j P(X=x_j) \lg P(X=x_j)$
- Entropy of a coin flip
  - $H(X) = -\sum_{j=\text{heads,tails}} P(X=x_j) \lg P(X=x_j)$
  - $= -(P(\text{heads}) \lg P(\text{heads}) + P(\text{tails}) \lg P(\text{tails}))$
  - $= -(.5 \lg .5 + .5 \lg .5) = -(.5 * -1 + .5 * -1) = 1$
  - Complete uncertainty!*
- Conditional Entropy:
  - $H(X|Y) = -\sum_j P(Y=y_j) [\sum_i P(X=x_i|Y=y_j) \lg P(X=x_i|Y=y_j)]$

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## Formal Definition



- Flow from  $x$  to  $y$  if  $H(x_s | y_t) < H(x_s | y_s)$ 
  - $-\sum_i P(y_t=y_j) [\sum_i P(x_s=x_i | y_t=y_j) \lg P(x_s=x_i | y_t=y_j)] <$   
 $-\sum_j P(y_s=y_j) [\sum_i P(x_s=x_i | y_s=y_j) \lg P(x_s=x_i | y_s=y_j)]$
- Has the uncertainty of  $x_s$  gone down from knowing  $y_t$ ?
- Examples showing possible flow from  $x$  to  $y$ :
  - $y := x$ 
    - No uncertainty –  $H(x|y) = 0$
  - $y := x / z$ 
    - Greater uncertainty (we only know  $x$  for some values of  $y$ )
  - Why *possible*?
  - Does information flow from  $y$  to  $x$ ?
- What if  $y_s$  not defined?
  - Flow if  $H(x_s | y_t) < H(x_s)$

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## Implicit flow



- Implicit flow: flow of information without assignment
- Example:
  - if  $(x = 1)$  then  $y := 0$  else  $y := 1$
- *This is why the entropy definition is necessary!*

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## How do we Manage Information Flow?



- Information flow policy
  - Captures security levels
  - Often based on *confinement*
  - Principles: Reflexivity, transitivity
- Compiler-based mechanisms
  - Track potential flow
  - Enforce legality of flows
- Execution-based mechanisms
  - Track flow at runtime
  - Validate correct

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## Confinement Flow Model



- $(I, O, \text{confine}, \rightarrow)$ 
  - $I = (SC_I, \leq_I, \text{join}_I)$ : Lattice-based policy
  - $O$ : set of entities
  - $\rightarrow$ :  $O \times O$  indicates possible flows
  - $\text{confine}(o)$ :  $SC_I \times SC_I$  is allowed flow levels
- Security requirement
  - $\forall a, b \in O: a \rightarrow b \Rightarrow a_L \leq_I b_U$
- Similar definitions possible for more general levels
  - non-lattice
  - non-transitive

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## Compiler Mechanisms



- Declaration approach
  - $x$ : *integer class*  $\{ A, B \}$
  - Specifies what security classes of information are allowed in  $x$
- Function parameter: *class* = argument
- Function result: *class* =  $\cup$  parameter classes
  - Unless function verified stricter
- Rules for statements
  - Assignment: LHS must be able to receive all classes in RHS
  - Conditional/iterator: then/else must be able to contain if part
  - Composition
- *Verifying a program is secure becomes type checking!*

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## Execution Mechanisms



- Problem with compiler-based mechanisms
  - *May be too strict*
  - Valid executions not allowed
- Solution: run-time checking
- Difficulty: *implicit* flows
  - **if**  $x=1$  **then**  $y:=0$ ;
  - When  $x:=2$ , does information flow to  $y$ ?
- Solution: Data mark machine
  - Tag variables
  - *Tag Program Counter*
  - Any branching statement affects PC security level
    - Affect ends when “non-branched” execution resumes

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## Data Mark: Example



- Statement involving only variables  $x$ 
  - If  $\underline{PC} \leq x$  then *statement*
- Conditional involving  $x$ :
  - Push  $\underline{PC}$ ,  $\underline{PC} = \text{lub}(\underline{PC}, x)$ , execute inside
  - When done with conditional statement, Pop  $\underline{PC}$
- Call: Push  $\underline{PC}$
- Return: Pop  $\underline{PC}$
- Halt
  - if *stack empty* then *halt execution*

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## Flow Control: Specialized Processor

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- Security Pipeline Interface
  - Independent entity that checks flow
  - Could this manage confidentiality?
  - *Useful for integrity!*

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## Confinement

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- Confinement Problem
  - Prevent a server from leaking confidential information
- Covert Channel
  - Path of communication not designed as communication path
- Transitive Confinement
  - If a confined process invokes a second process, invokee must be as confined as invoker

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## Isolation



- Virtual machine
  - Simulates hardware of an (abstract?) machine
  - Process confined to virtual machine
    - Simulator ensures confinement to VM
  - Real example: IBM VM/SP
    - Each user gets “their own” IBM 370
- Sandbox
  - Environment where actions restricted to those allowed by policy

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## Covert Channels



- Storage channel
  - Uses attribute of shared resource
- Timing channel
  - Uses temporal/ordering relationship of access to shared resource
- Noise in covert channel
  - Noiseless: Resource only available to sender/receiver
  - Noisy: Other subjects can affect resource

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## Modeling Covert Channels



- Noninterference
  - Bell-LaPadula approach
  - All shared resources modeled as subjects/objects
  - Let  $\sigma \in \Sigma$  be states. Noninterference secure if  $\forall s$  at level  $l(s) \exists \equiv: \Sigma \times \Sigma$  such that
    - $\sigma_1 \equiv \sigma_2 \Rightarrow \text{view}(\sigma_1) = \text{view}(\sigma_2)$
    - $\sigma_1 \equiv \sigma_2 \Rightarrow \text{execution}(i, \sigma_1) \equiv \text{execution}(i, \sigma_2)$
    - if  $i$  only contains instructions from subjects dominating  $s$ ,  $\text{view}(\text{execution}(i, \sigma)) = \text{view}(\sigma)$
- Information Flow analysis
  - Again model all shared resources

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## Covert Channel Mitigation



- Can covert channels be eliminated?
  - Eliminate shared resource?
- **Severely** limit flexibility in using resource
  - Otherwise we get the halting problem
  - Example: Assign fixed time for use of resource
    - *Closes timing channel*
- Not always realistic
  - *Do we really need to close every channel?*

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## Covert Channel Analysis

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- Solution: Accept covert channel
  - But analyze the capacity
    - *How many bits/second can be “leaked”*
- Allows cost/benefit tradeoff
  - Risk exists
  - Limits known
- Example: Assume data time-critical
  - Ship location classified until next commercial satellite flies overhead
  - Can covert channel transmit location before this?

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## Example: Covert Channel Analysis

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