



Modeling Plant Life in Computer Graphics

Introduction

Siggraph 2016 Course

Sören Pirk, Bedrich Benes, Takashi Ijiri, Yangyan Li,
Oliver Deussen, Baoquan Chen, Radomír Měch

Course Summary

An introduction to plant modeling

and

recent advances in plant modeling in computer graphics.



Course Motivation

Recent years have seen a lot of progress in vegetation modeling

We focus on the following three areas

- 1) Procedural and biological modeling
- 2) Reconstruction and inverse procedural modeling
- 3) User-assisted models

Requirements

- The course is 1.5 hours long
- No previous knowledge of biology is required
- Requires basics of basic algebra and calculus
- Knowledge about geometric modeling is a plus

Presenters

- Bedrich Benes Purdue University, USA
- Oliver Deussen University of Konstanz, Germany
- Sören Pirk Stanford University, USA
- Baoquan Chen Shandong University, China
- Radomír Měch Adobe Systems, Inc., USA
- Takashi Ijiri Ritsumeikan University, Japan
- Yangyan Li Stanford University, USA



Modeling Plant Life in Computer Graphics

Overview

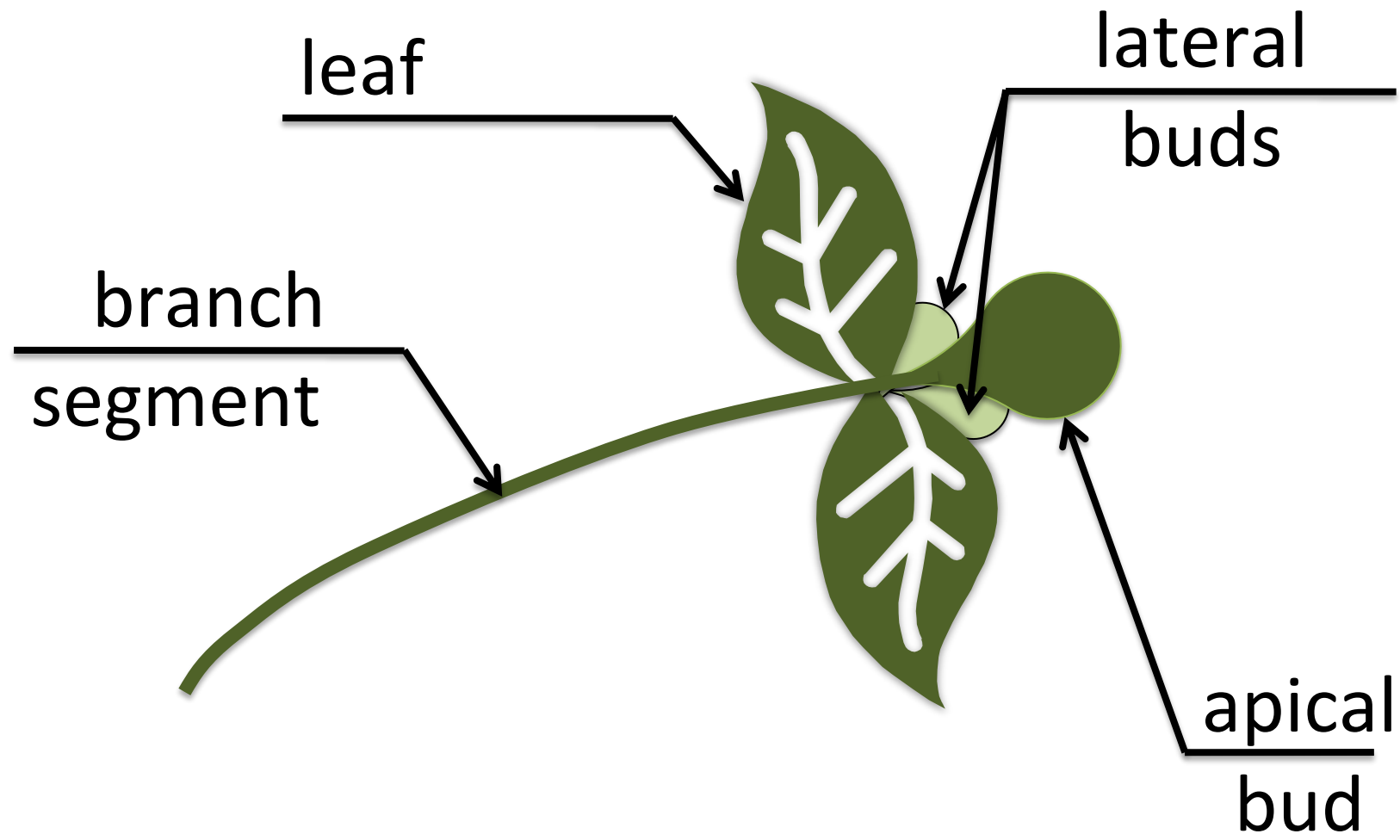
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Plants in Computer Graphics

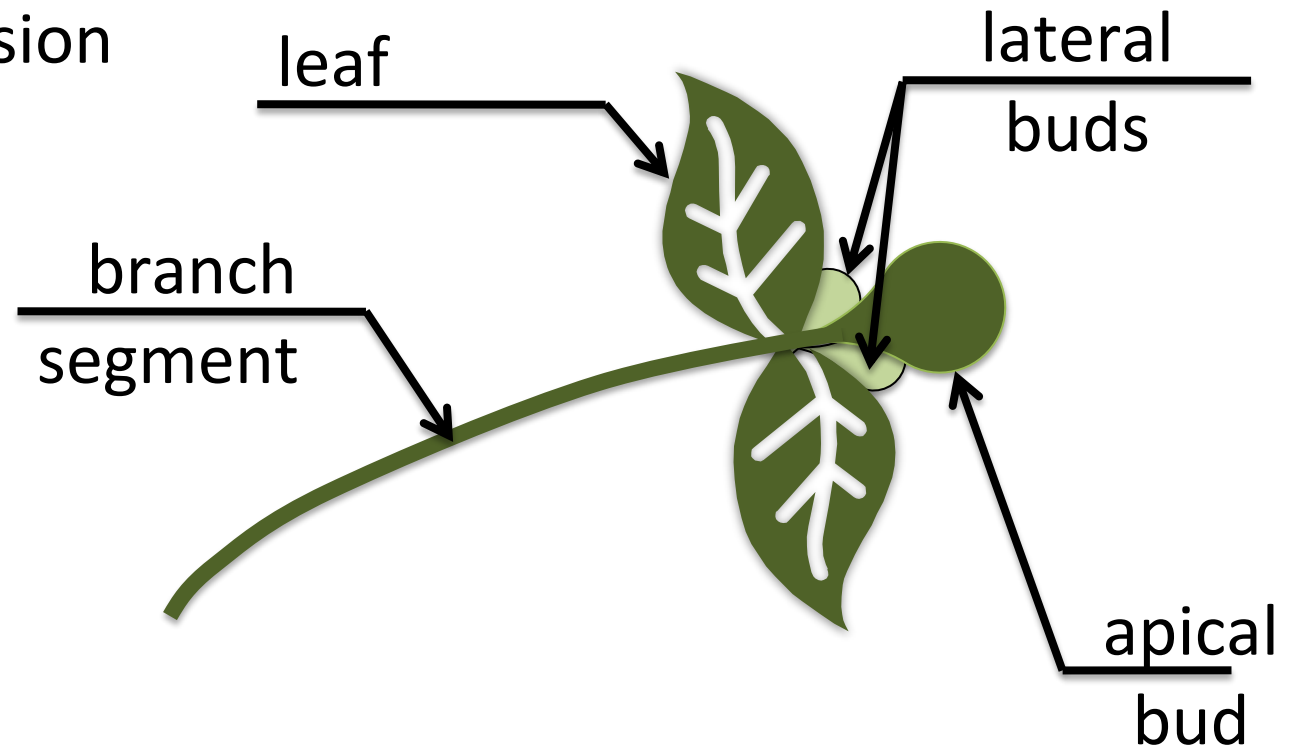
- Biologically-based simulations
- Plant is a modular system – basic elements (leaves, internodes, etc.)
- Ecosystems consider entire plant communities (a plant is a module)
- Plant geometry is the result of **interaction of the modules**

Plant Modules



Plant Growth

- Growth is biologically-based
- Uses plant modules to control the growth
- Primary growth – apex extension
- Apical bud
- Lateral buds
 - Initially dormant
 - Activated after some time



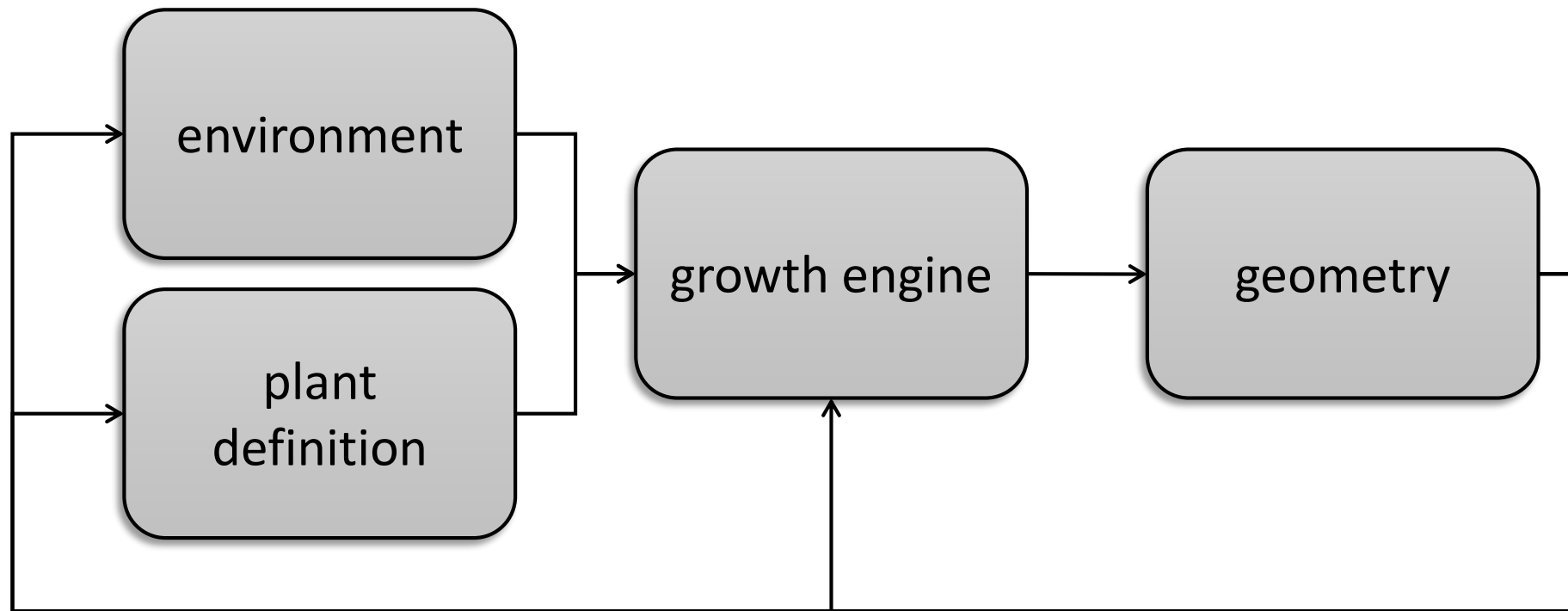


Plant Growth

- Secondary growth (cambial growth)
- Branch is getting thicker
- Annual rings formation



Generic Plant Modeling System

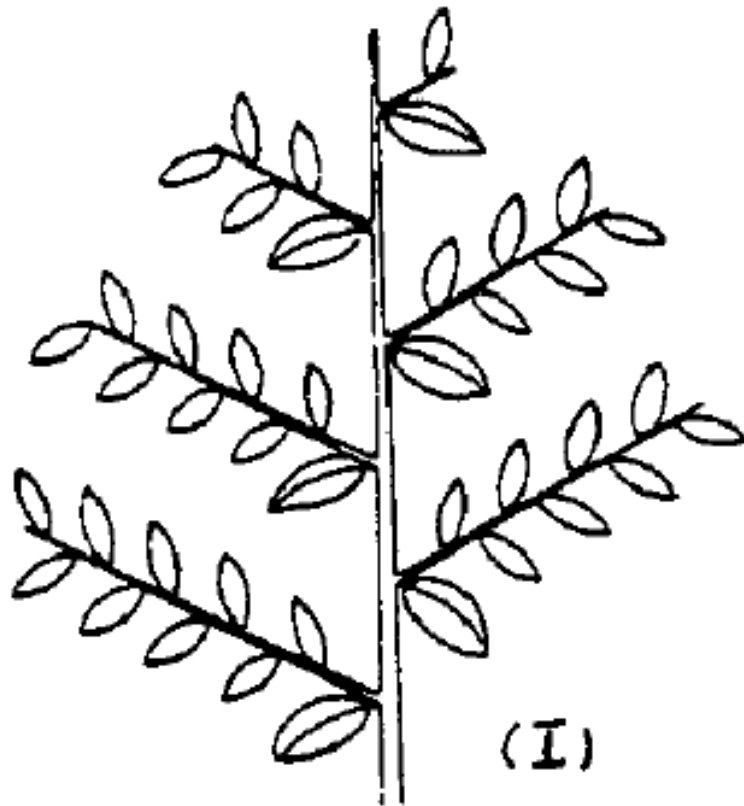




Plant Definition

- Ramification (branching)
- Biological model
- Bud lifespan
- Plant sensitivity to external impetus

Ramification



Continuous

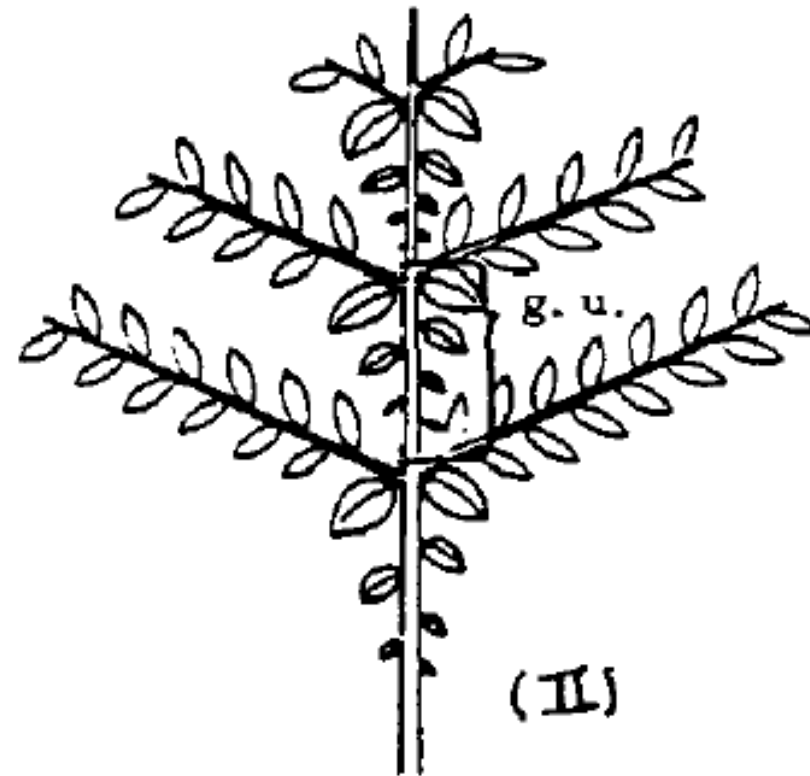


Image from (de Reffye et al 1988)
Rhythmic

Axis (branch) order

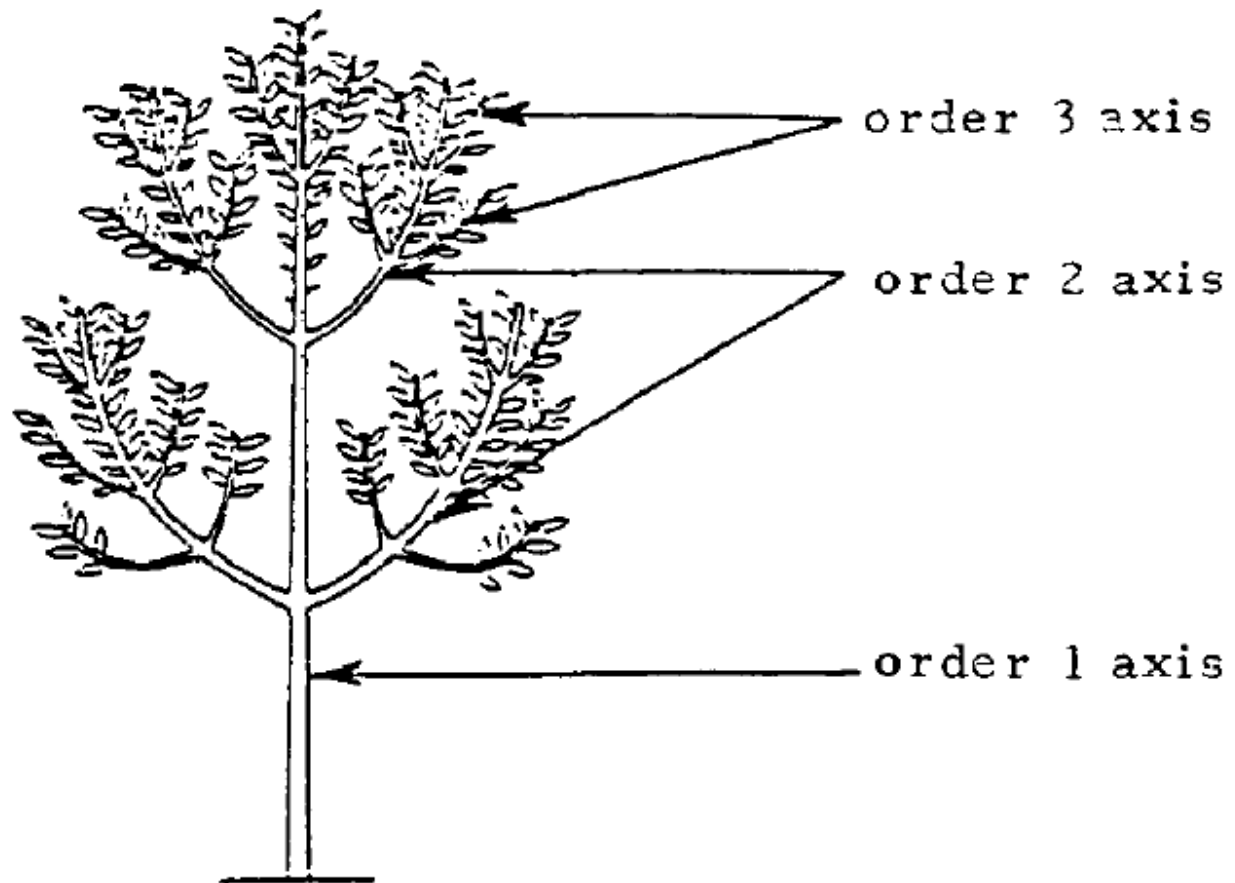
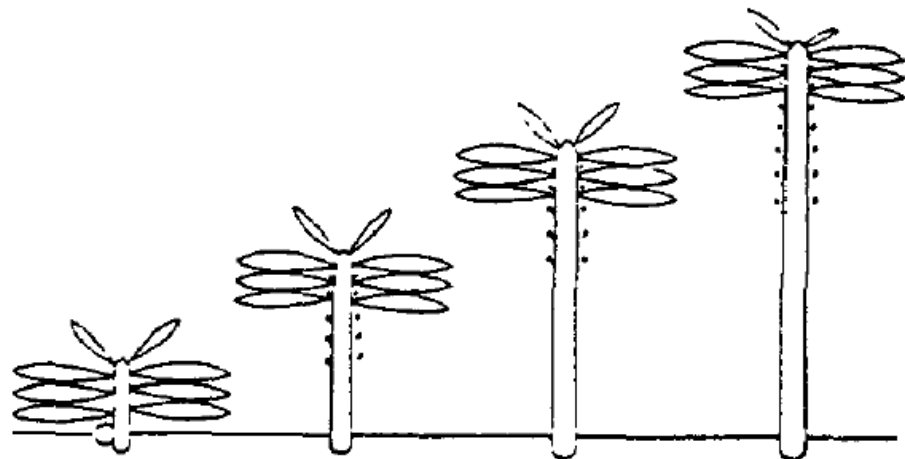
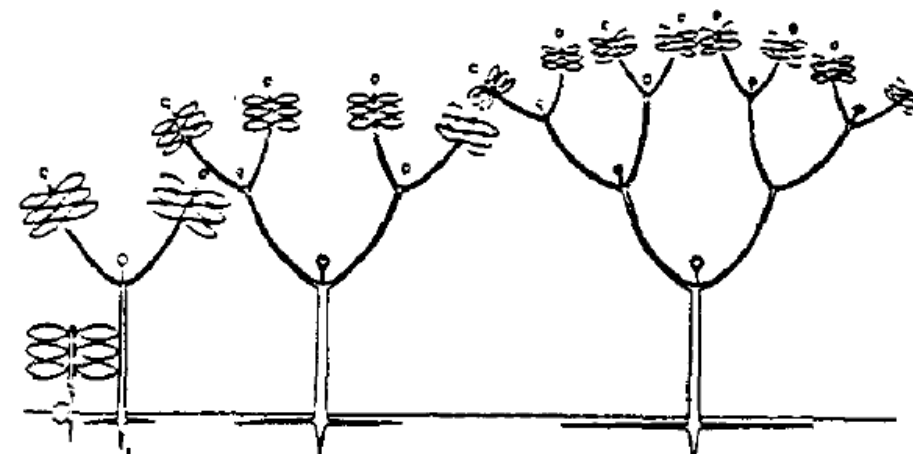


Image from (de Reffye et al 1988)

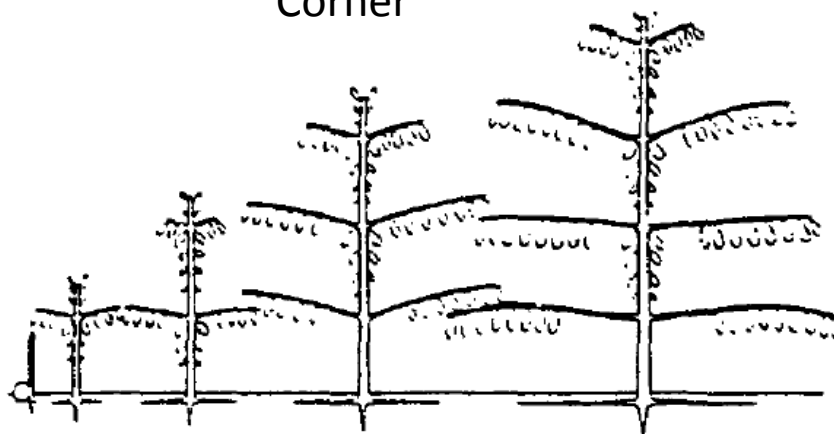
Biological Model



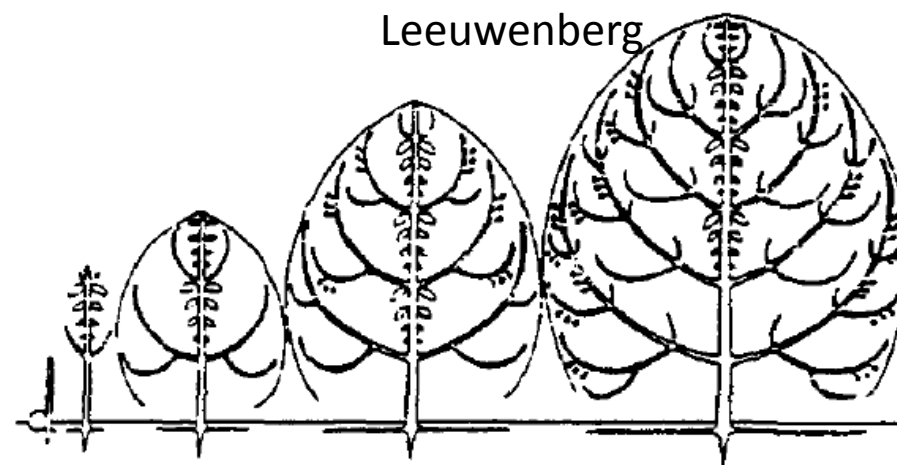
Corner



Leeuwenberg



Massart



Rauh



Light and Phototropism

- plant growth is driven by buds (“plant engines”)
- each bud evaluates its illumination
- determines the brightest spot (bending)
- % of illuminated buds on a branch determines its fate

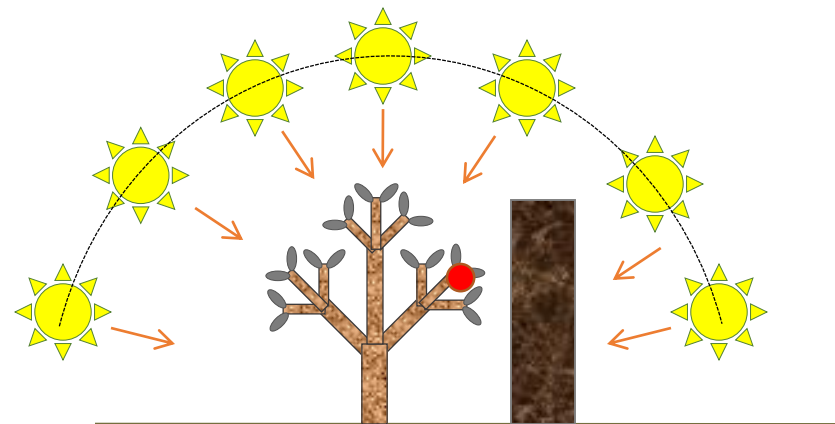
Illumination

- Phototropism

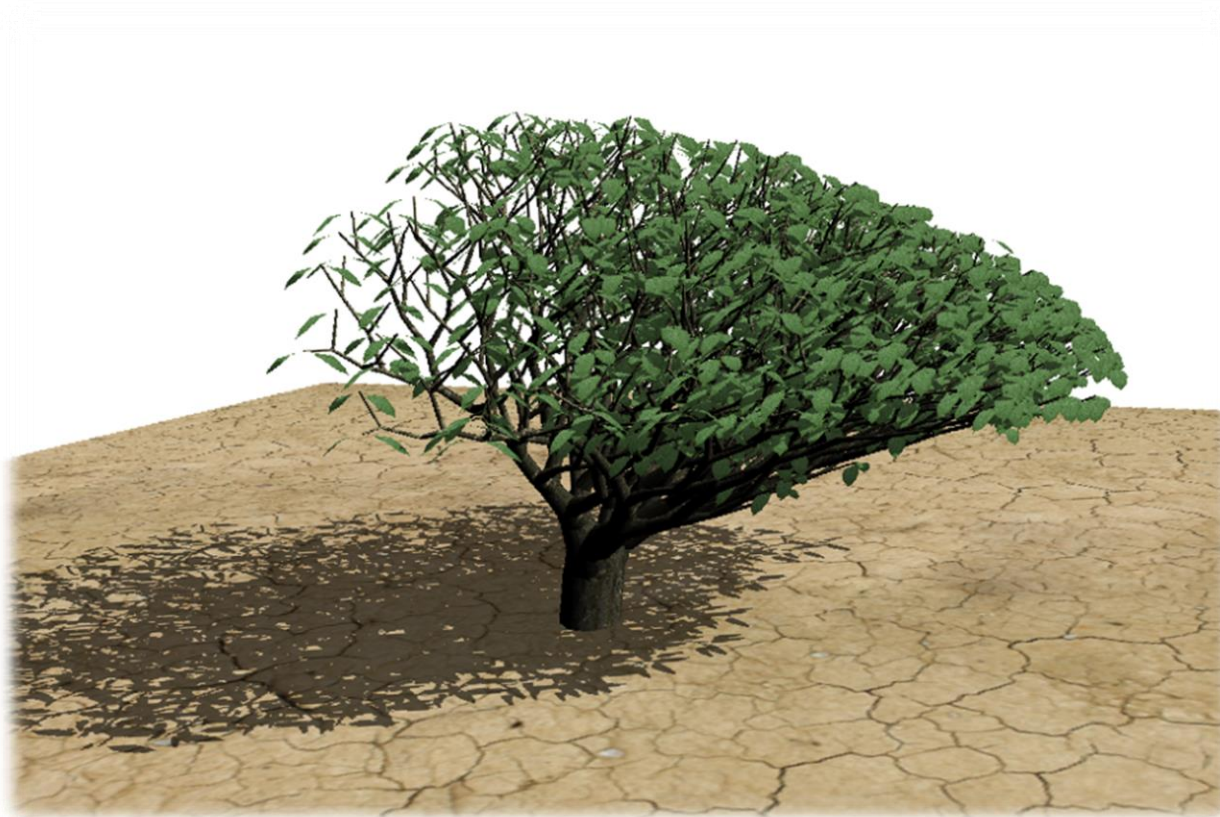
- Branches tend to grow toward the light
- Calculate the total illumination on a bud i

$$E_i = n_i / m$$

- n_i – no. of positive samples
- m – no. of all samples
- Find the brightest spot
 - Bend the direction

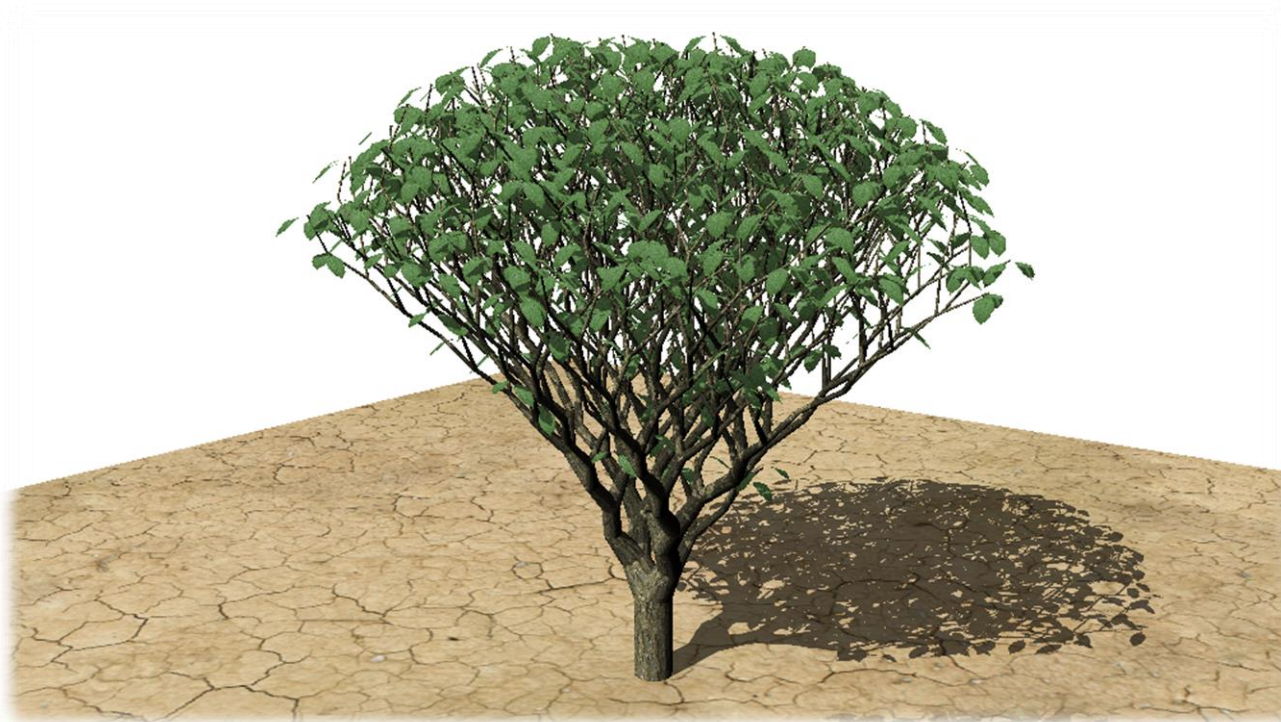


Light and Phototropism



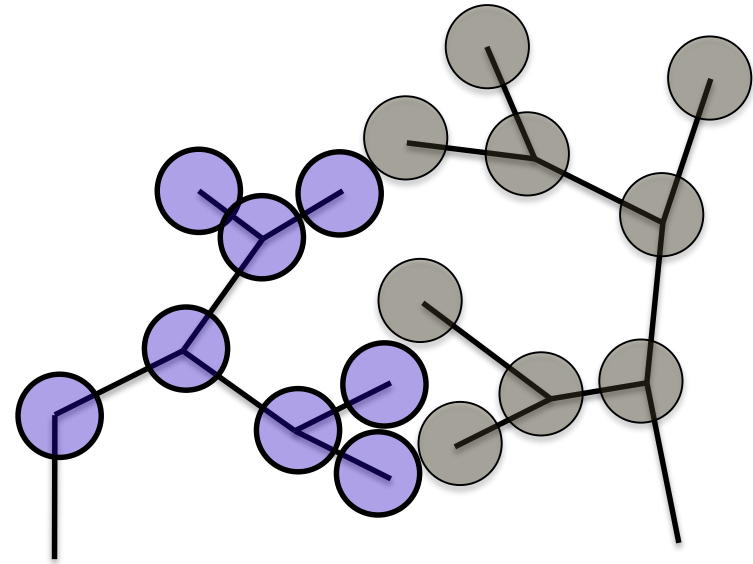
Gravity

- Gravitropism
 - Branches tend to grow against gravity



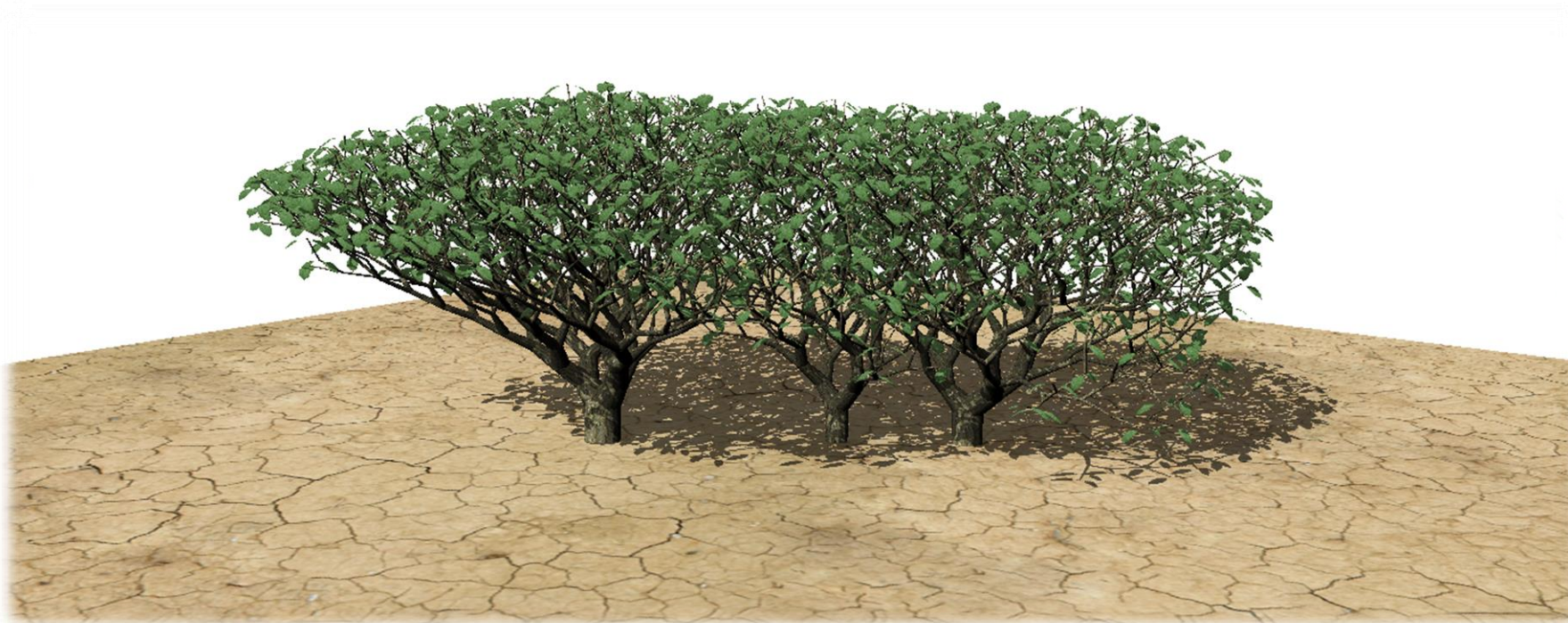
Competition for Resources

- Branches tend to avoid each other
- Honda model [Honda67]
 - A buds has a sphere of interest
 - Two spheres cannot overlap
 - If two spheres collide – do something



Competition for Resources

- a small ecosystem fighting for space on bud level

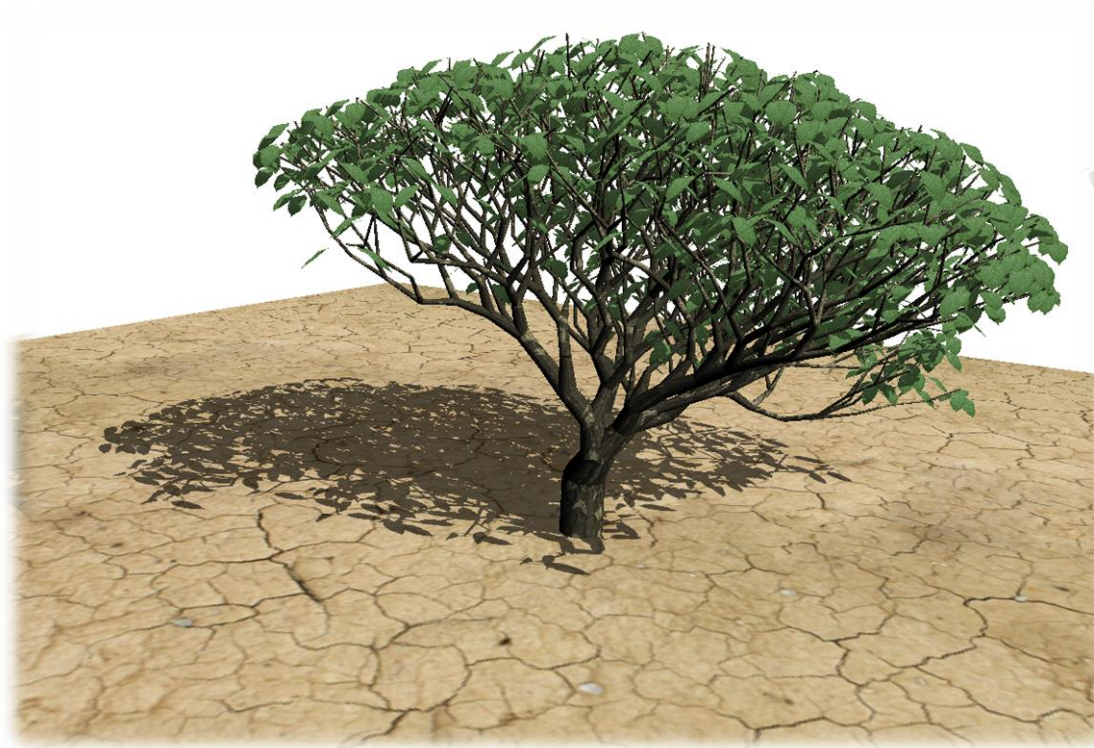


Competition for Resources



Competition for Space

- Branches compete for space



Competition for Resources

- at the level of an ecosystem

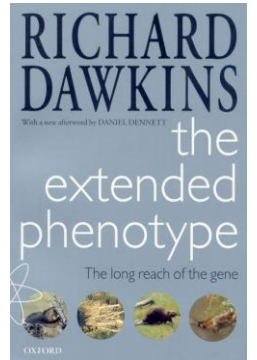


image from
Palubicki, W., Horel, K., Longay, S.,
Runions, A., Lane, B., Měch, R.,
and Prusinkiewicz, P., (2009) Self-
organizing tree models for image
synthesis. ACM Trans. Graph. 28,
3, Article 58 (July 2009), 10 pages.



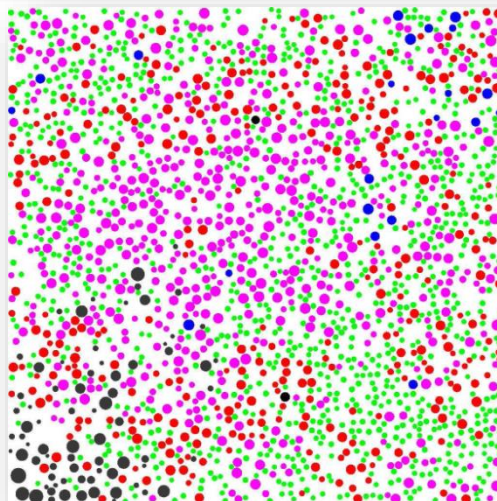
Ecosystems

- A module, so far, was a part of a plant
- An entire plant can be thought of as a module
- Plants compete for resources (Extended Phenotype – Dawkins)
- Result of the competition are ecosystems

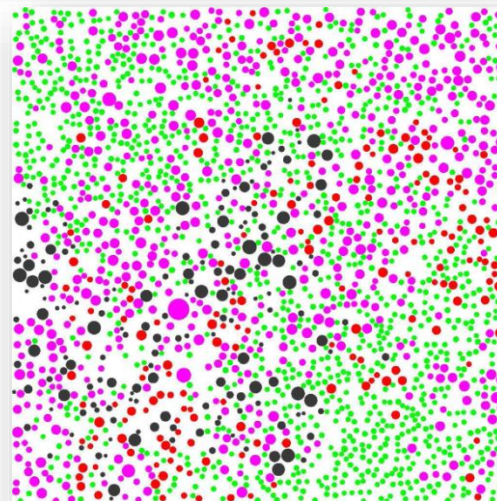


Ecosystems

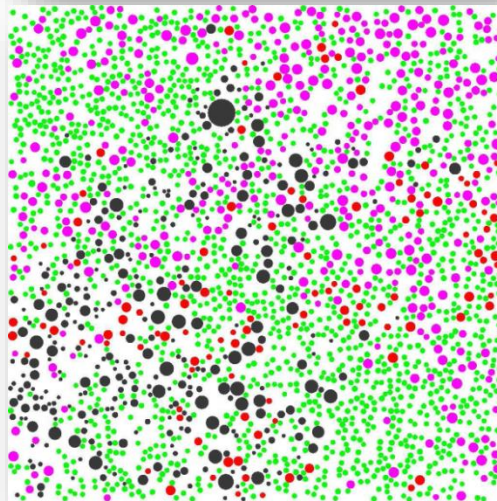
25 years



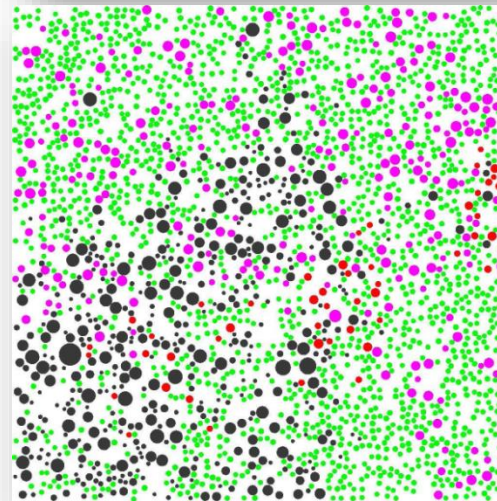
75 years



100 years



125 years





Urban Ecosystems



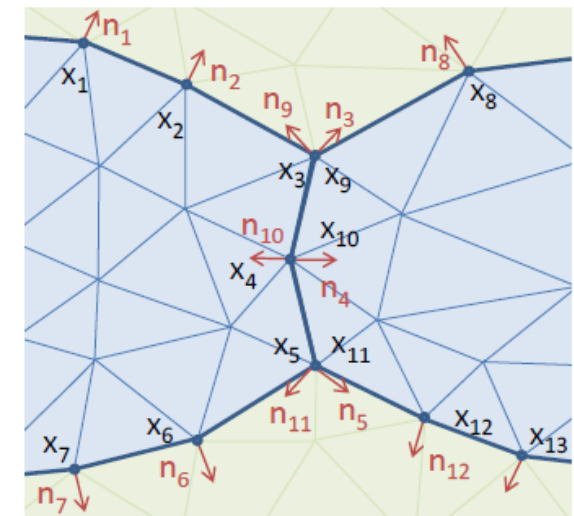
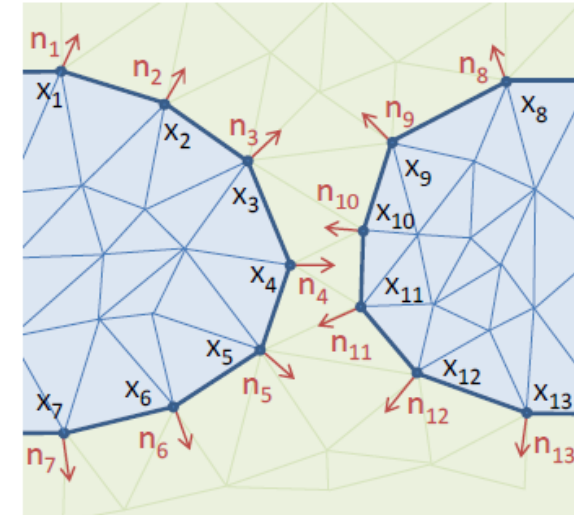
Cambial (Secondary) Growth

Kratt, J., Spicker, M., Guayaquil, A., Fiser, M., Pirk, S., Deussen, O., Hart, J.C., and Benes, B., (2015) Woodification: User-Controlled Cambial Growth Modeling in Computer Graphics Forum (Proceedings of Eurographics 2015), 33 (2), 361-372 (DOI=10.1111/cgf.12566)



Cambial (Secondary) Growth

- Uses deformable simplicial complexes
- Propagate vertices based on growth function
- Detection of collisions and self-intersections
- Adds cracks





Cambial (Secondary) Growth



Used References

- Benes, B., Andryscio, N., and Stava, O., (2009) *Interactive Modeling of Virtual Ecosystems*, in EG Workshop on Natural Phenomena, pp. 9-16
- Benes, B., Massih, M-A., Jarvis, P., Aliaga, D.G., and Vanegas, C., (2011) *Urban Ecosystem Design*, in Proceedings of I3D, pp: 167-174
- de Reffye, P.; Edelin, C.; Françon, J.; Jaeger, M. & Puech, C. (2988) *Plant models faithful to botanical structure and development*, in SIGGRAPH Computer Graphics, ACM, 1988, 22, 151-158
- Palubicki, W., Horel, K., Longay, S., Runions, A., Lane, B., Měch, R., and Prusinkiewicz, P., (2009) *Self-organizing tree models for image synthesis*. ACM Trans. Graph. 28, 3, Article 58 (July 2009), 10 pages.
- Kratt, J., Spicker, M., Guayaquil, A., Fiser, M., Pirk, S., Deussen, O., Hart, J.C., and Benes, B., (2015) *Woodification: User-Controlled Cambial Growth Modeling in Computer Graphics Forum* (Proceedings of Eurographics 2015), 33 (2), 361-372 (DOI=10.1111/cgf.12566)

Modeling Plant Life in Computer Graphics

Environmental Response

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Overview

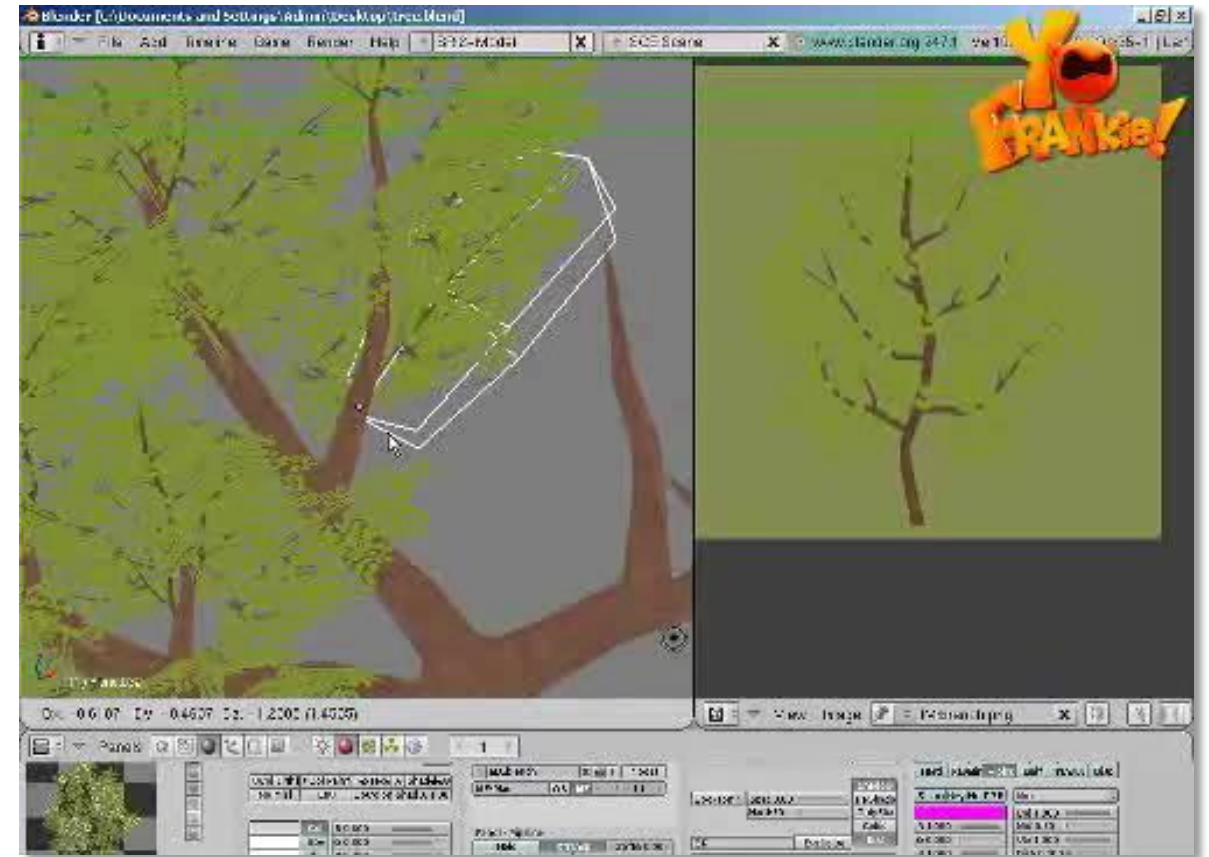
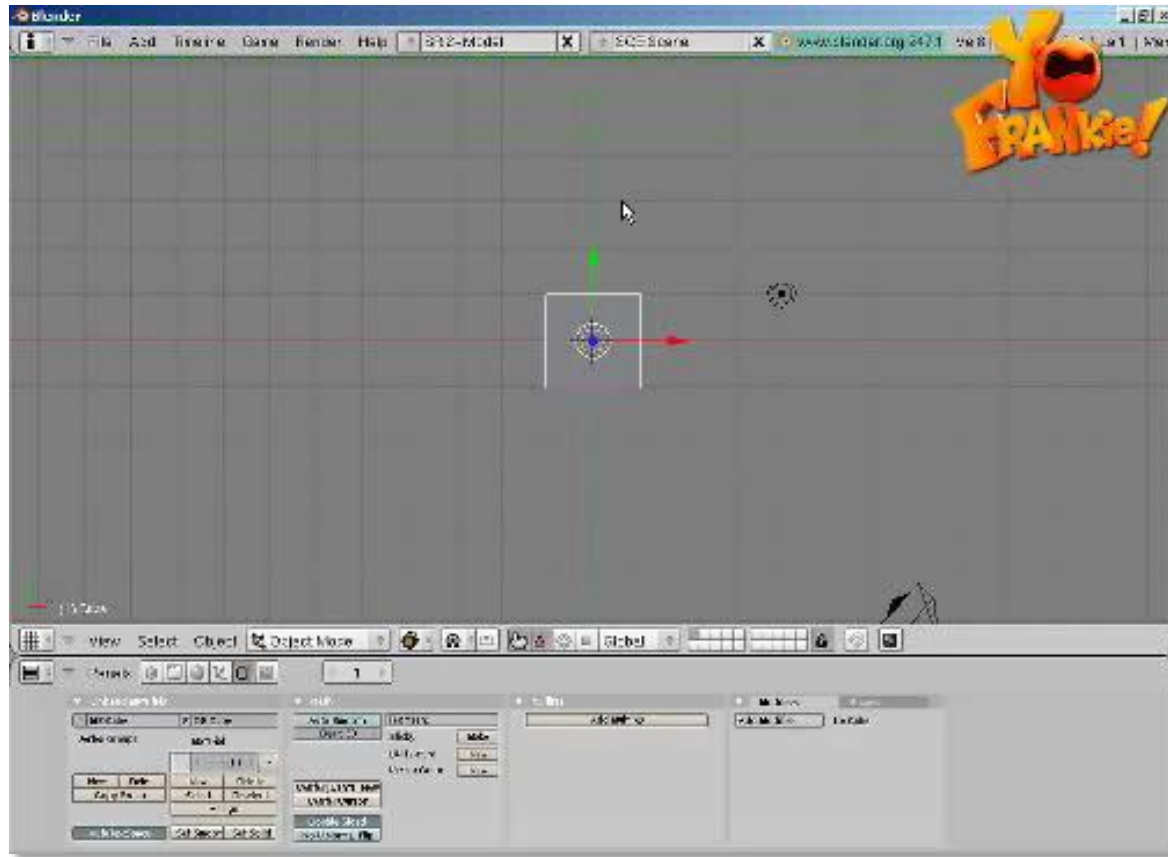
Environmental response [20 minutes]

- Real-time sensitivity of tree models **(Pirk)**
- Capturing growth response **(Pirk)**
- Physics response to wind **(Pirk)**

Tree models are static



3D Tree Modeling



Pablo Vazquez - <http://vimeo.com/2956756>

Plastic Trees: Interactive Self-Adapting Botanical Tree Models

Pirk, S., Stava, O., Kratt, J., Said, M. A. M., Neubert, B., Mech, R., Benes, B., Deussen, O.

Plastic trees: interactive self-adapting botanical tree models.

ACM Trans. on Graph. 31, 4, 50:1–50:10, 2012.

Environment Aware Trees



Automatic modification of 3D tree models



Skeletal Graph



Skeletal Graph

- Branch Age
- Growth Rate

Tree Analysis - Tropisms



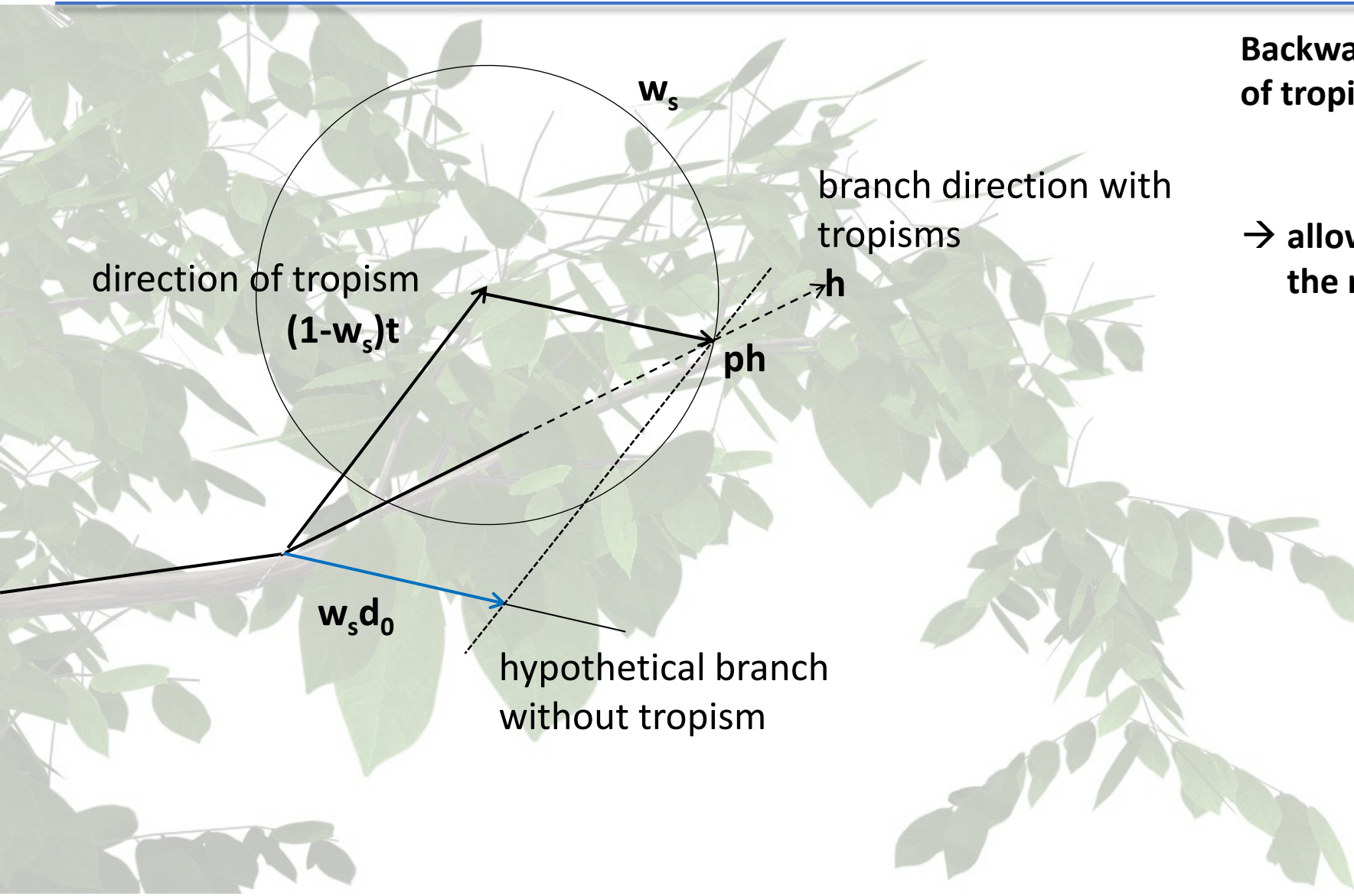
Phototropism



Gravitropism



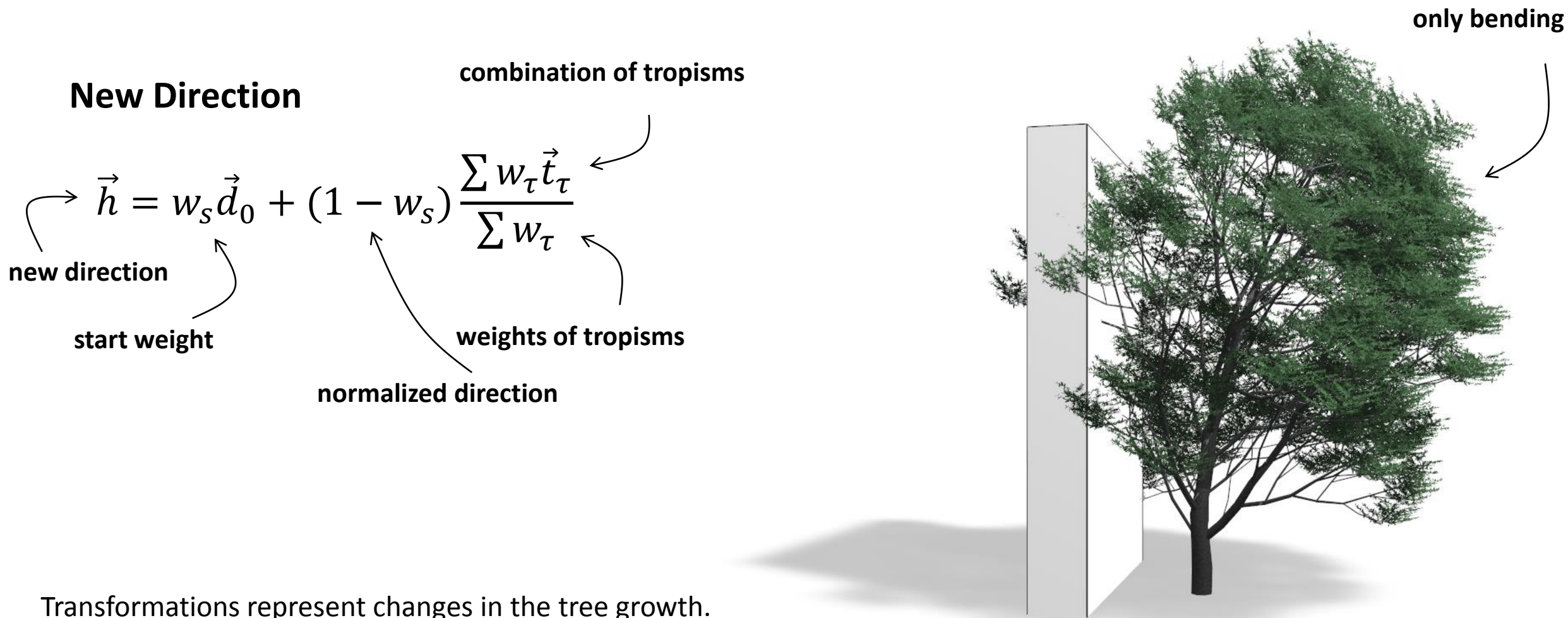
Inverse Tropism



Backward modeling to estimate influence of tropisms to the original model

→ allows to apply tropisms triggered by the new environment

Dynamic Interaction - Bending



Transformations represent changes in the tree growth.

Dynamic Interaction - Pruning

Approach similar to [Palubicki et al. 2009]

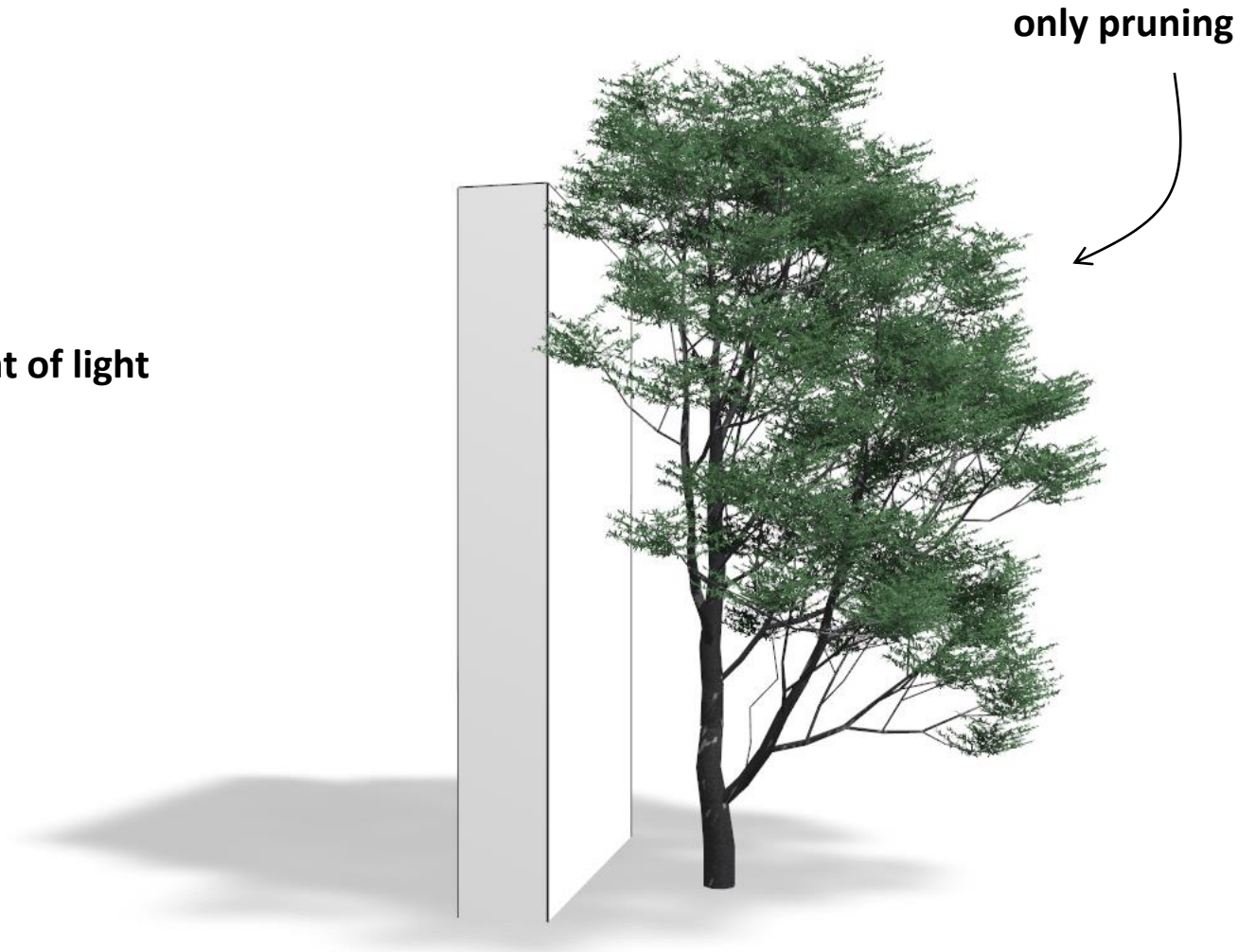
Amount of Light received by the leaf-cluster.

$$\varphi_{t_s} = \sum_{c \in C_s} 2\pi r_c^2 i_c$$

φ_{t_s} : amount of resources (light)
 r_c : radius of a given cluster
 i_c : normalized amount of light

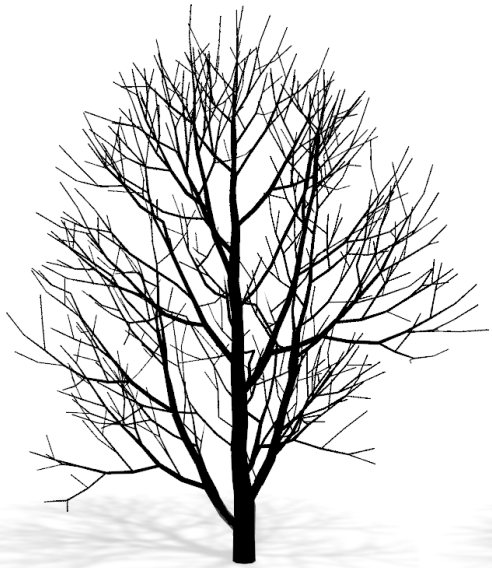
l_t : sum of distances

Branch is pruned when ratio $\varphi_{t_s}/l_t < thres$

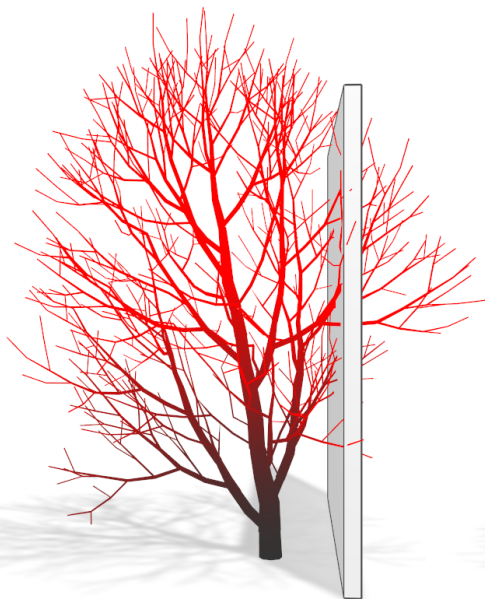


Tree/Obstacle Interaction

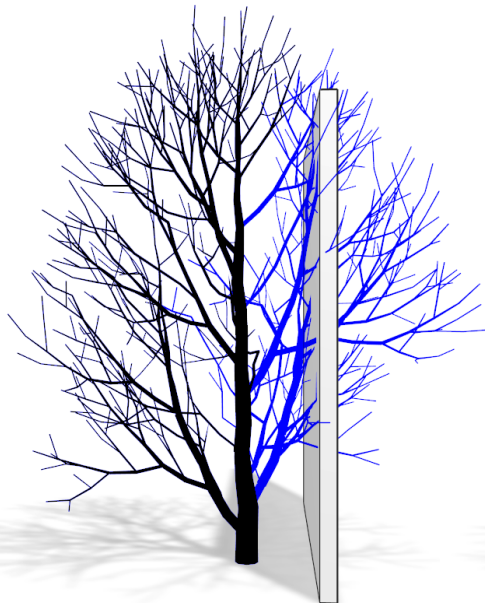
Original Model



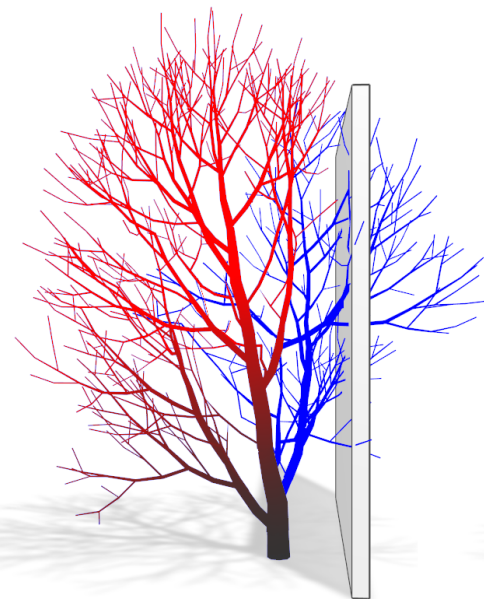
Bending



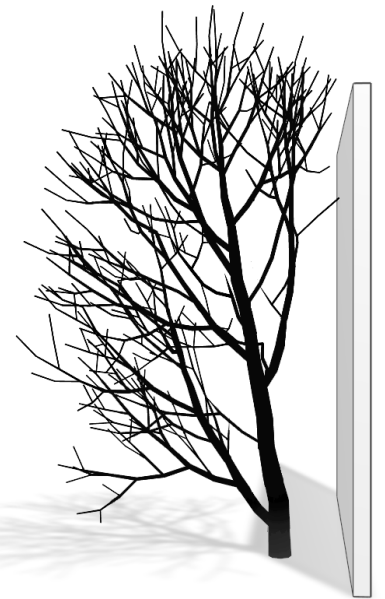
Pruning



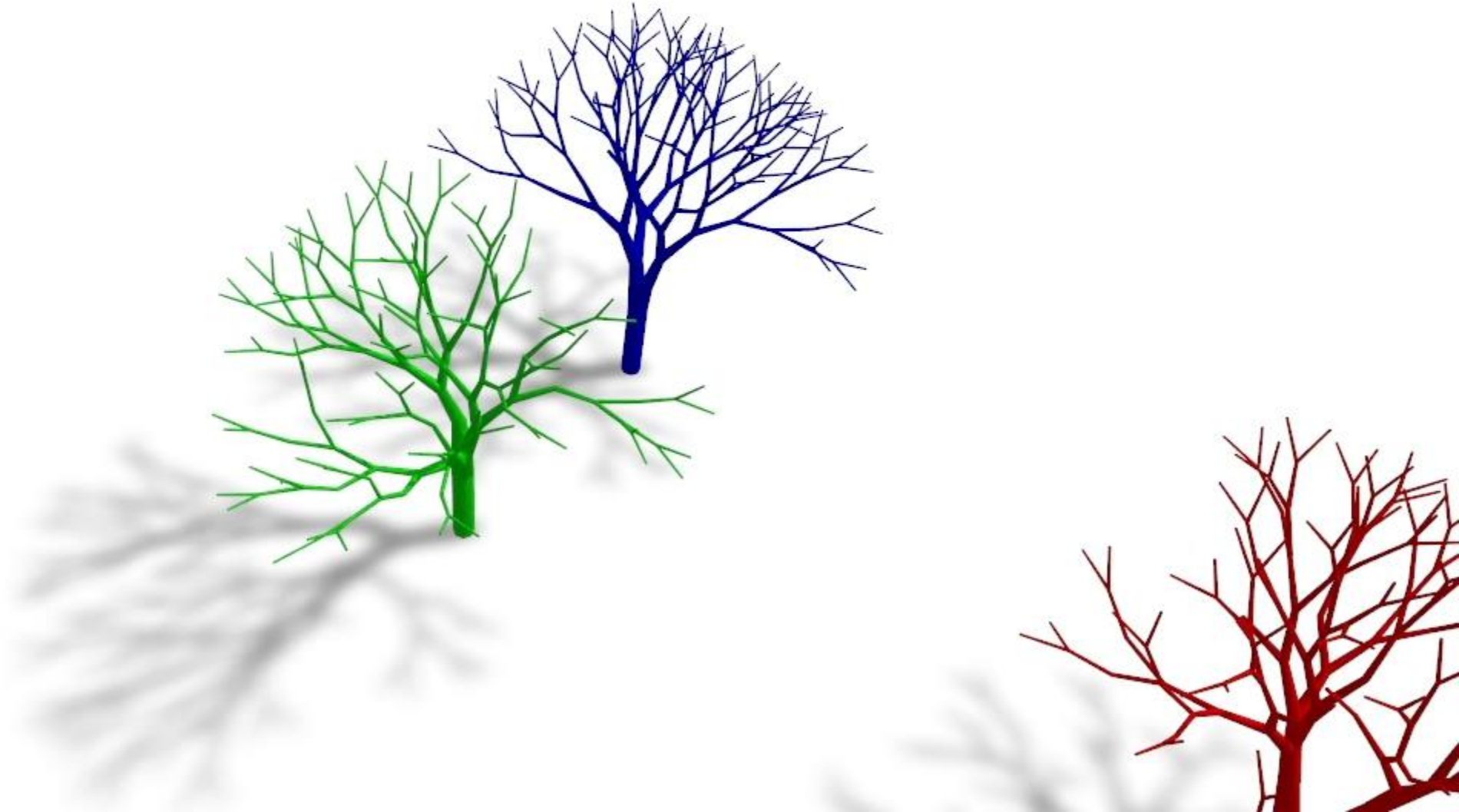
Bending + Pruning



Result



Tree/Tree-Interaction



Bending/Pruning Result



<http://www.flickr.com/photos/harveydogson/4095300141/>



<http://www.flickr.com/photos/jlwhitfield1/2731012752/>



Tree/Tree-Interaction



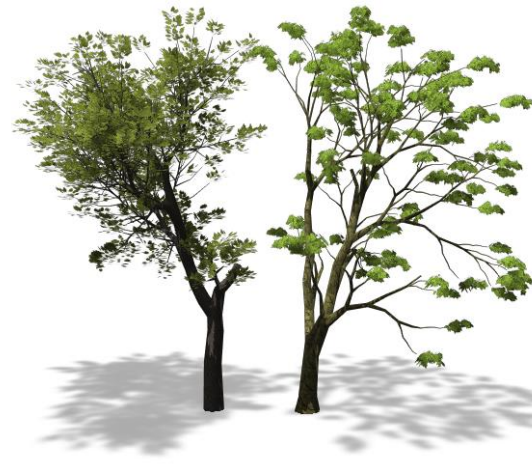
Static Models



Bending and Pruning



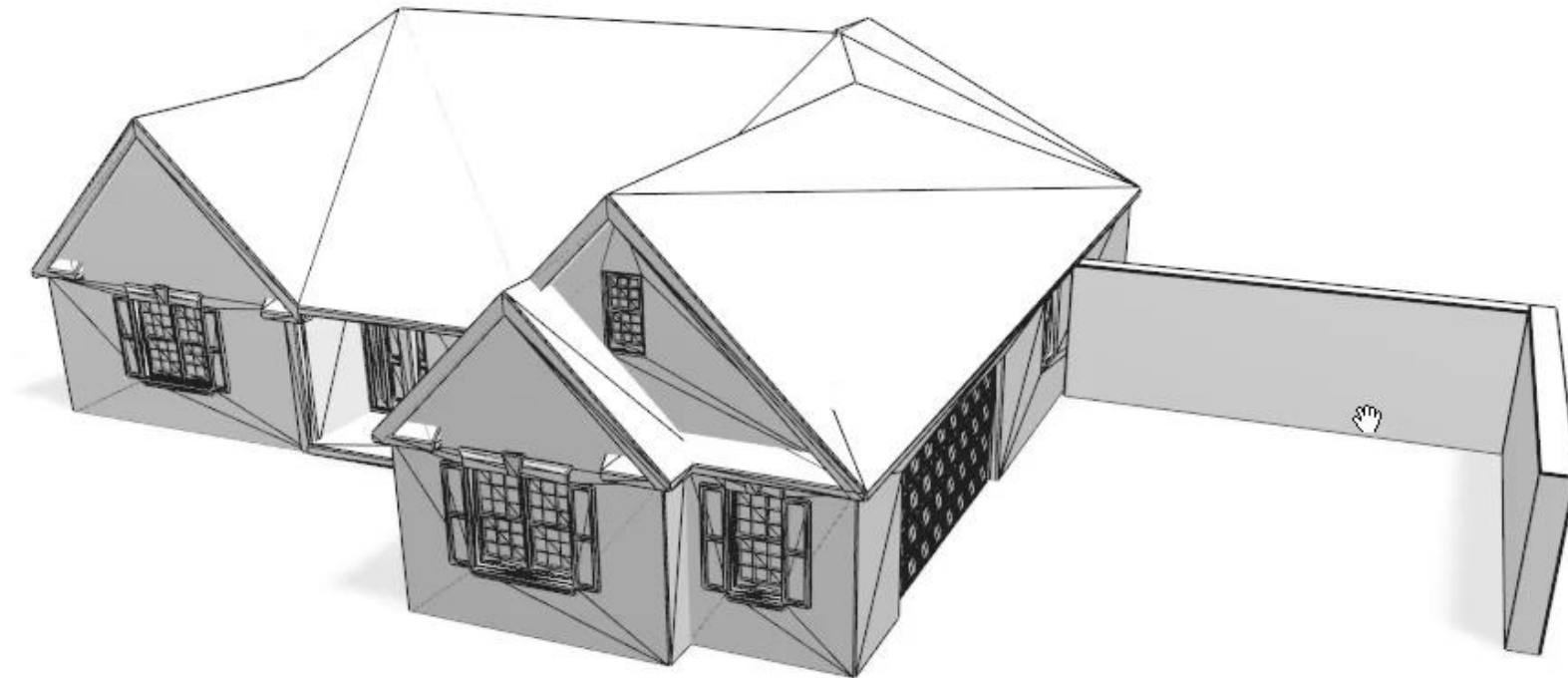
Strong Pruning



Exaggerated Bending



Editing



Capturing and Animating the Morphogenesis of Polygonal Tree Models

Pirk, S., Niese, T., Deussen, O., Neubert, B.

Capturing and animating the morphogenesis of polygonal tree models.

ACM Trans. on Graph. 31, 6, 169:1–169:10, 2012.



Continuous Animations of Growth

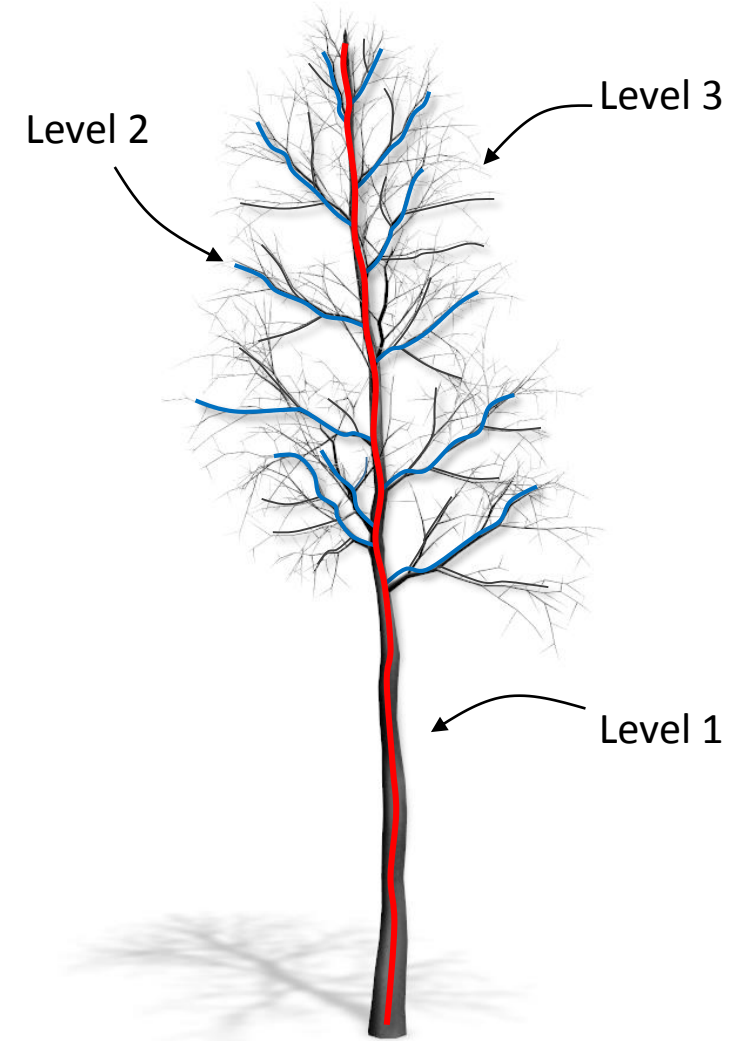
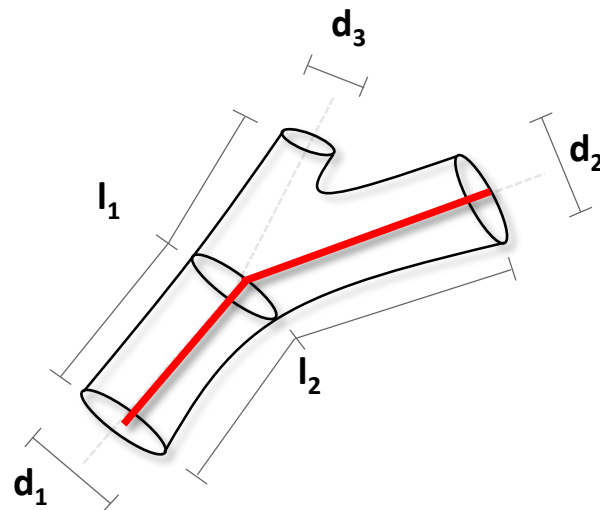


Gravelius Order

Ordering method for identifying hierarchies.

Determine main trunk based on angle between branches.

Also considering length and thickness of a branch.



Pipe Model Theory



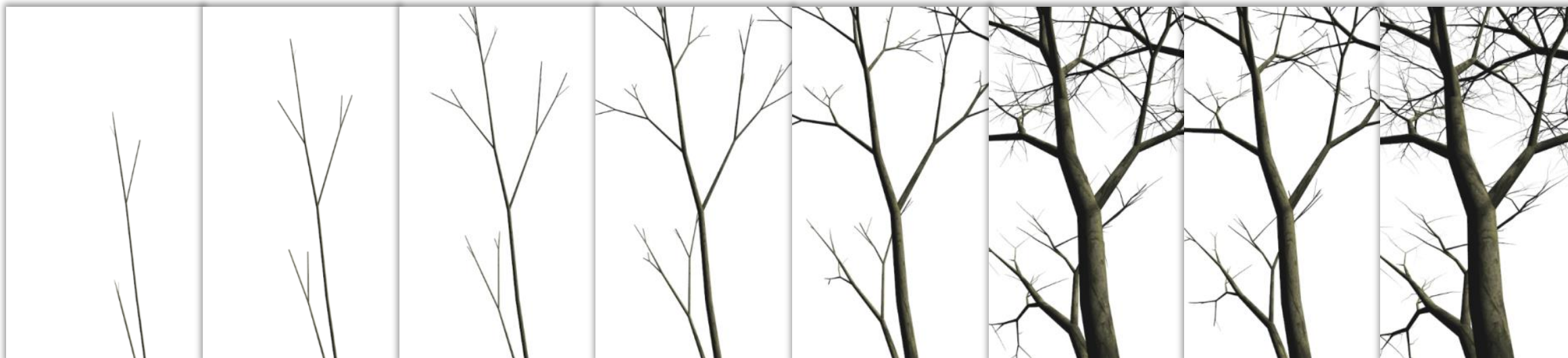
[Shinozaki et al. 1964]

Plant forms emerge from vascular systems.

Assembly of leaf units connecting the leaves to the root.

Provides us with branch radii.

Angle/Radii Interpolation



Angle Interpolation

Current Angle

Initial Angle

Duration

Angular Velocity

$$\vartheta_{\alpha} = \frac{\alpha_i - \alpha_{init}}{\Delta t}$$

Radii Interpolation

Child Radii

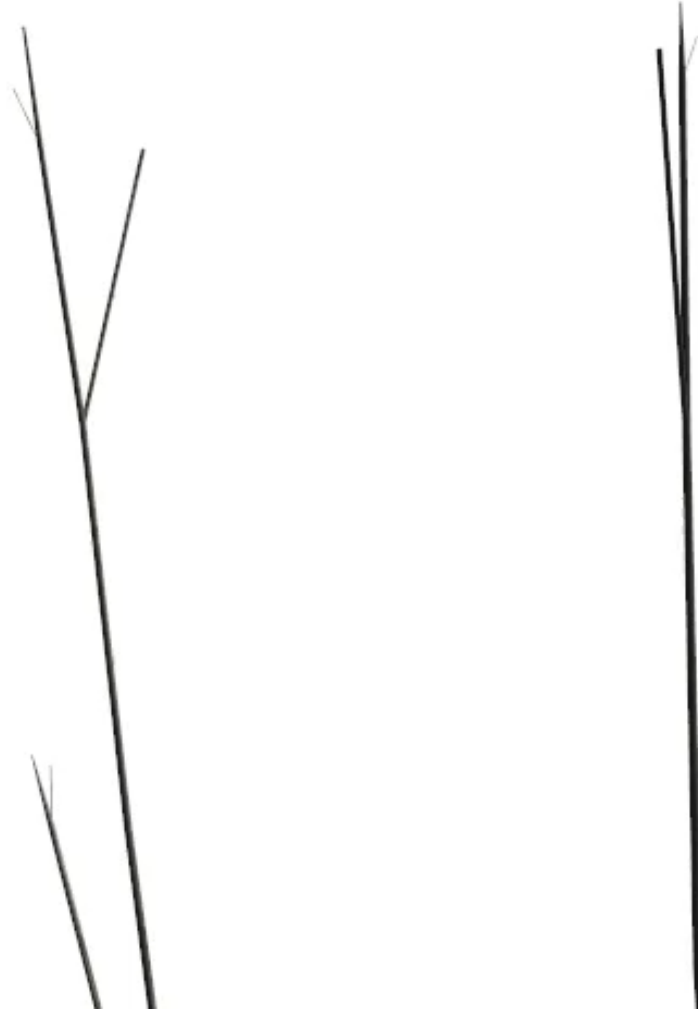
Current Radius

Original Model Coefficient

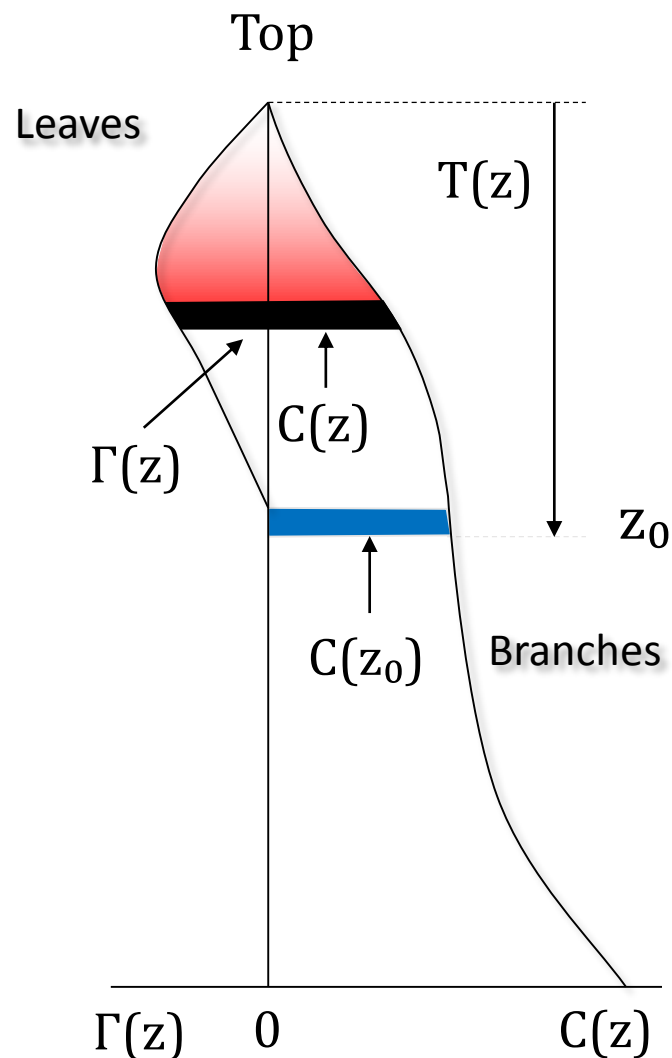
Power Law of Branching

$$r_p = \left(\frac{\sum r_i^u}{b^p} \right)^{\frac{1}{u}}$$

Angle/Radii Interpolation



Profile Diagram



Similar Among Plant Communities.

Represents vertical distribution of leaves.

Distribution of leaves needs to be consistent.

→ Tells us where geometry is missing.

→ How to measure densities?

[Chiba 1990, Chiba 1991]

Measuring Densities

Stratified Clipping (STC)

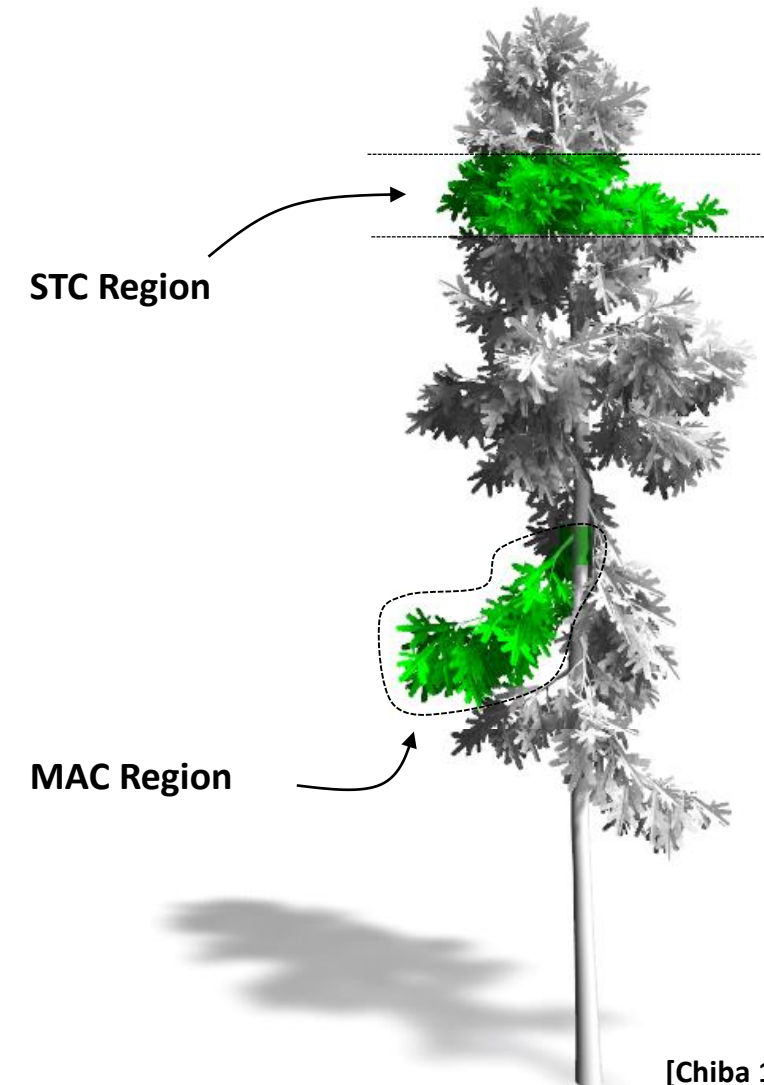
Vertical range of the tree is selected.

All branches and leaves in this region are used for measuring biomass.

Main Axis Cutting (MAC)

Part of the main axis is selected.

All branches and leaves attached to this part are used for measuring biomass.



Crown Ratio

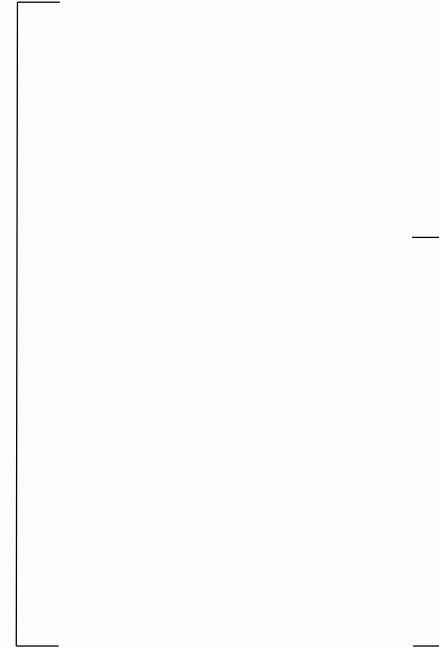


Add geometry where no information was available in the original model.

Remove geometry during animation to maintain plausibility and to eventually reach the input.

Crown Ratio

Overlap Region



Growth-based Editing



Individual Growth
of Branches



Windy Trees: Modeling Stress Response for Developmental Tree Models

Pirk, S., Niese, T., Hädrich, T., Benes, B., and Deussen. O.

Windy trees: computing stress response for developmental tree models.

ACM Trans. Graph. 33, 6, Article 204 ,11 pages, 2014.

Tree/Wind Interaction

Render the Possibilities
SIGGRAPH2016



Wind as Developmental Factor



Alex Bamford



Rich Price



Walberth Mascarenha



Fedderica Gentile

Windy Trees

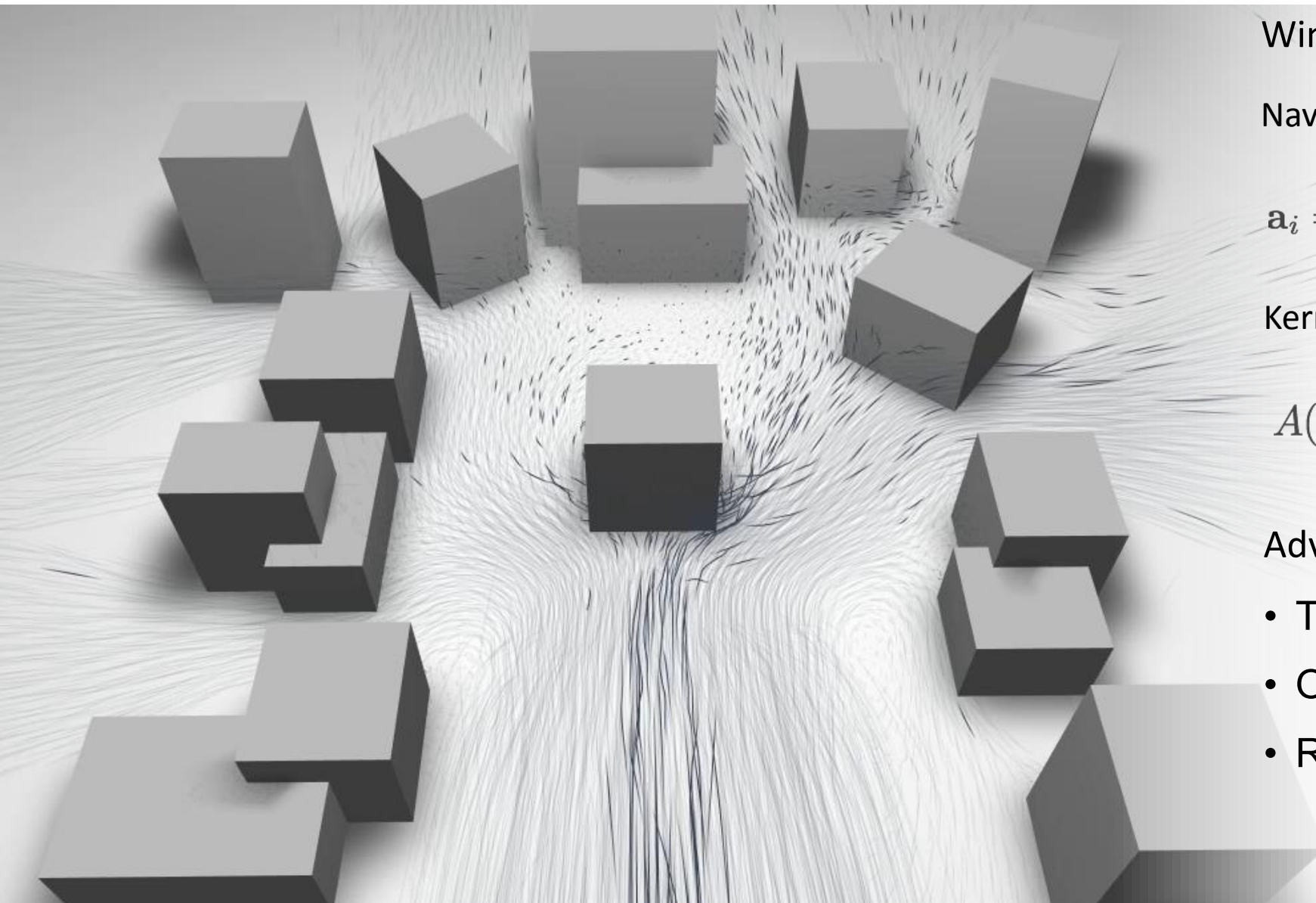


Growth Model

- Pipe Model Theory
- Gravelius Order
- Branching Angles
- Branch Radii
- Growth Rate



Smoothed Particle Hydrodynamics (SPH)



Wind Simulation

Navier Stokes - Acceleration

$$\mathbf{a}_i = \frac{d\mathbf{v}_i}{dt} = \frac{-\nabla p + \mu \nabla^2 \mathbf{v} + \rho \mathbf{g}}{\rho_i}$$

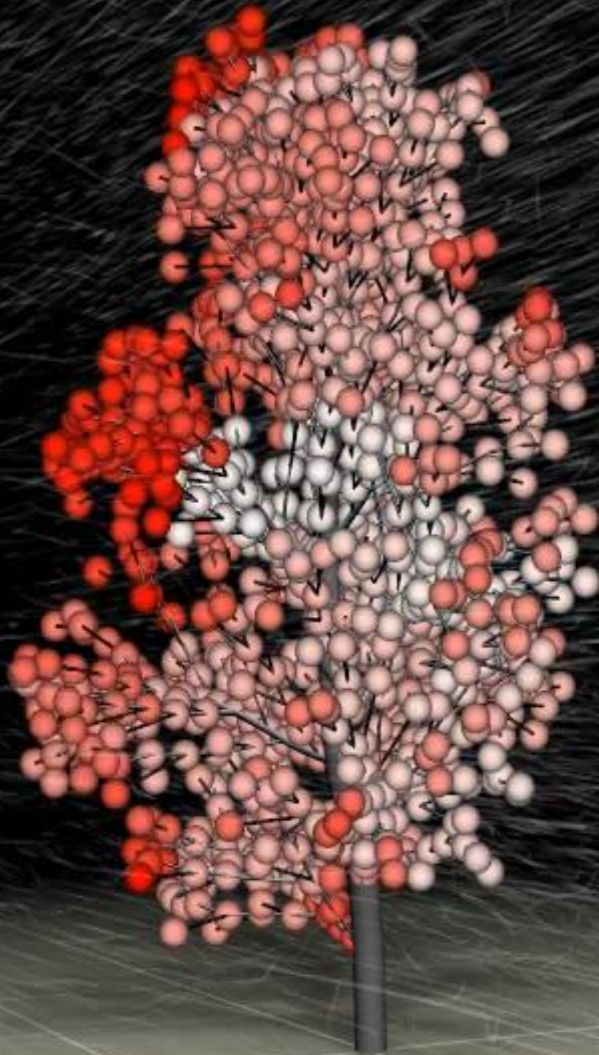
Kernel Smoothing Function

$$A(\mathbf{x}) = \sum_{j=1}^N \frac{m_j}{\rho_j} A_j W(\mathbf{x} - \mathbf{x}_j, h)$$

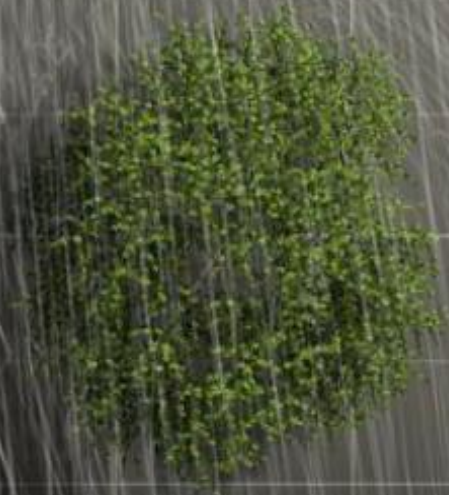
Advantages

- Tracking of individual collisions
- Occlusion handling (wind shadow)
- Real-time simulation

Sensor Particles



Two-Way Coupling



Force Model for Branches

Torque

$$N = I \frac{d\omega}{dt}$$

Moment of Inertia (rod)

$$I = \frac{mr^2}{3}$$

$$F_W = S_b \sigma \nu$$

Wind Force

$$D = -(\hat{\omega} \times \hat{e}) \mu \omega |\omega|$$

Damping Force

$$\mathbf{F} = \mathbf{F}_W + \mathbf{R} + \mathbf{D} + \mathbf{P} + \mathbf{L}$$

Restoration Force

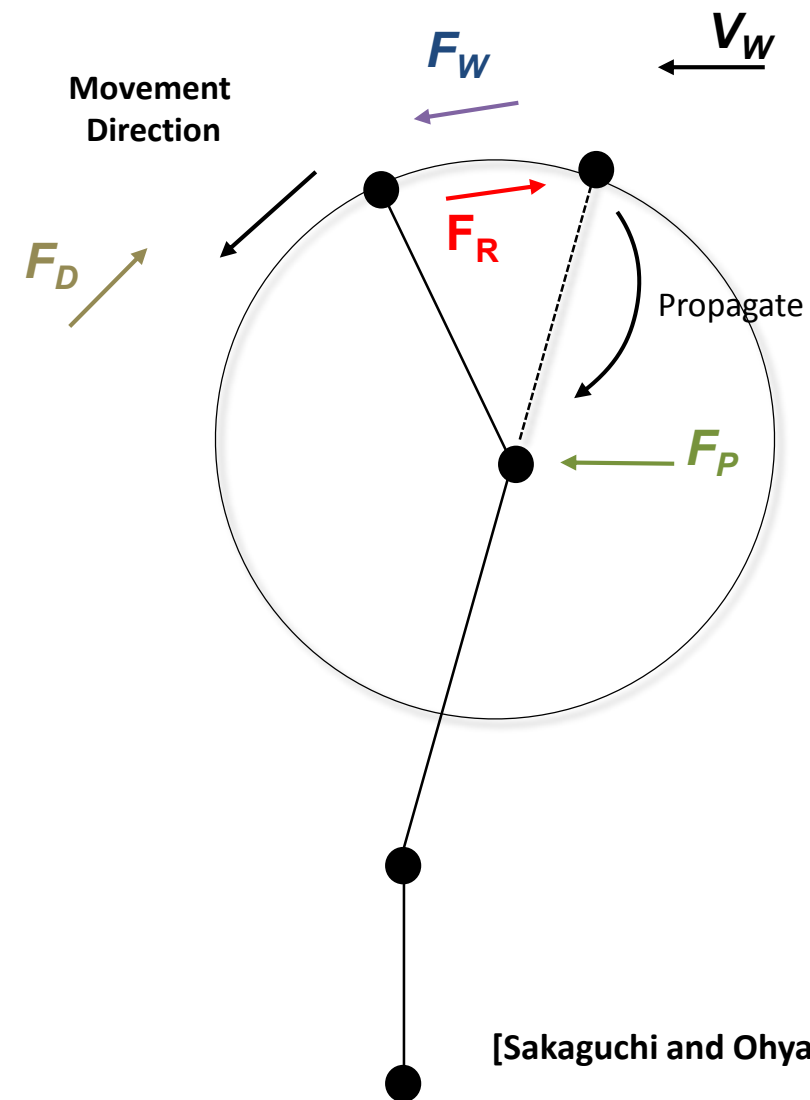
$$\mathbf{R} = d_r k \alpha$$

Propagation Force

$$\mathbf{P}_{i-1} = - \sum k_i \mathbf{F}_{Ri}$$

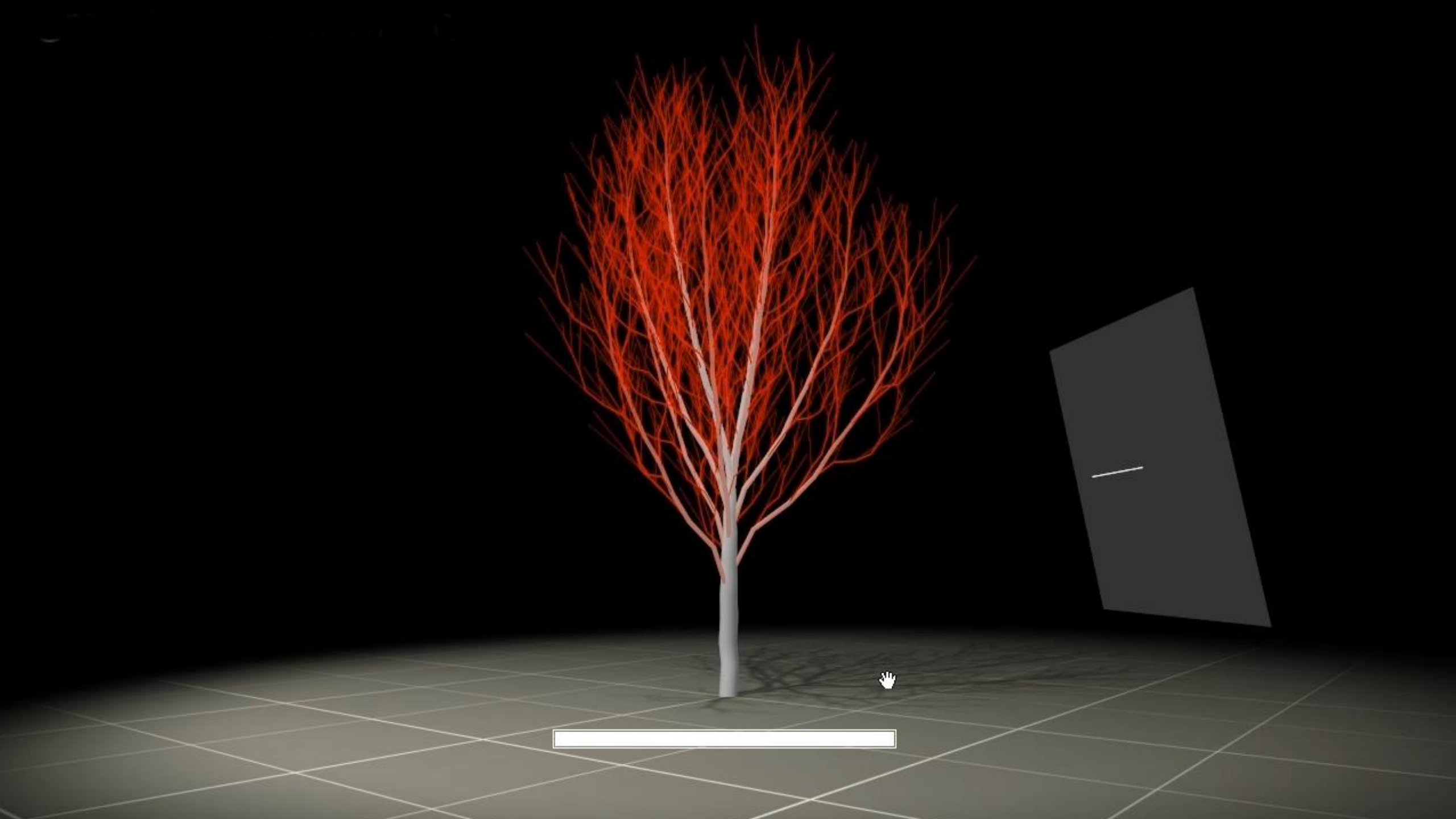
Leaf Force

$$\mathbf{L} = S_l \sigma \nu \mathbf{c}$$



[Sakaguchi and Ohya 1999]





Breaking of Branches

- Branch breaks when the acting forces exceed a certain level of stress
- Wood is a highly inhomogeneous material
- Approximating Young's Modulus and Hook's law

Young's Modulus Coefficient

Bending Moment

Stress

$$\sigma = \frac{4cM}{3\pi r^2}$$

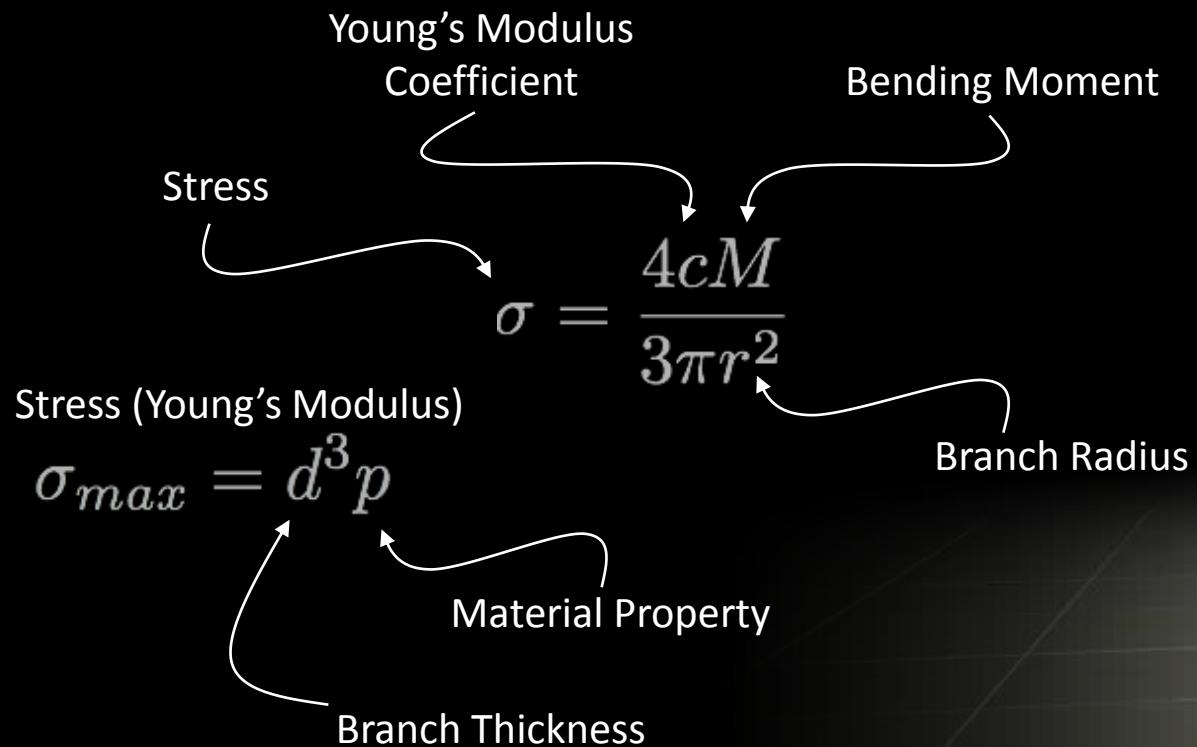
Stress (Young's Modulus)

$$\sigma_{max} = d^3 p$$

Material Property

Branch Radius

Branch Thickness

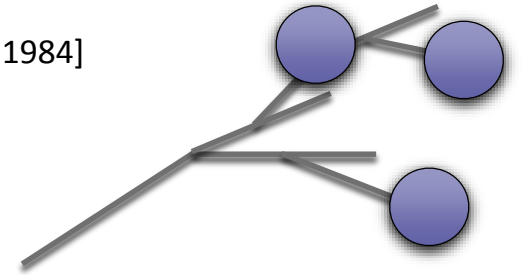




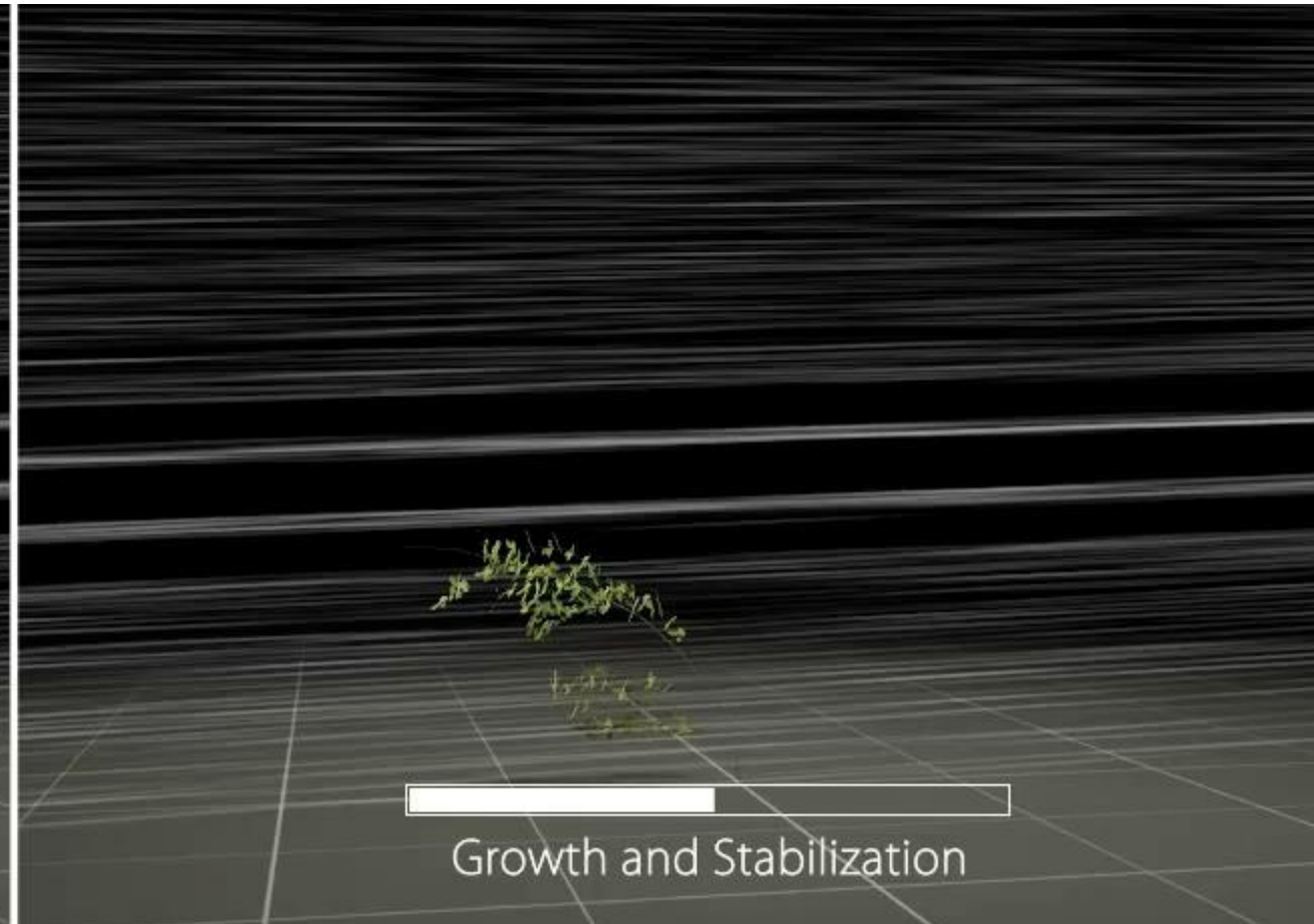
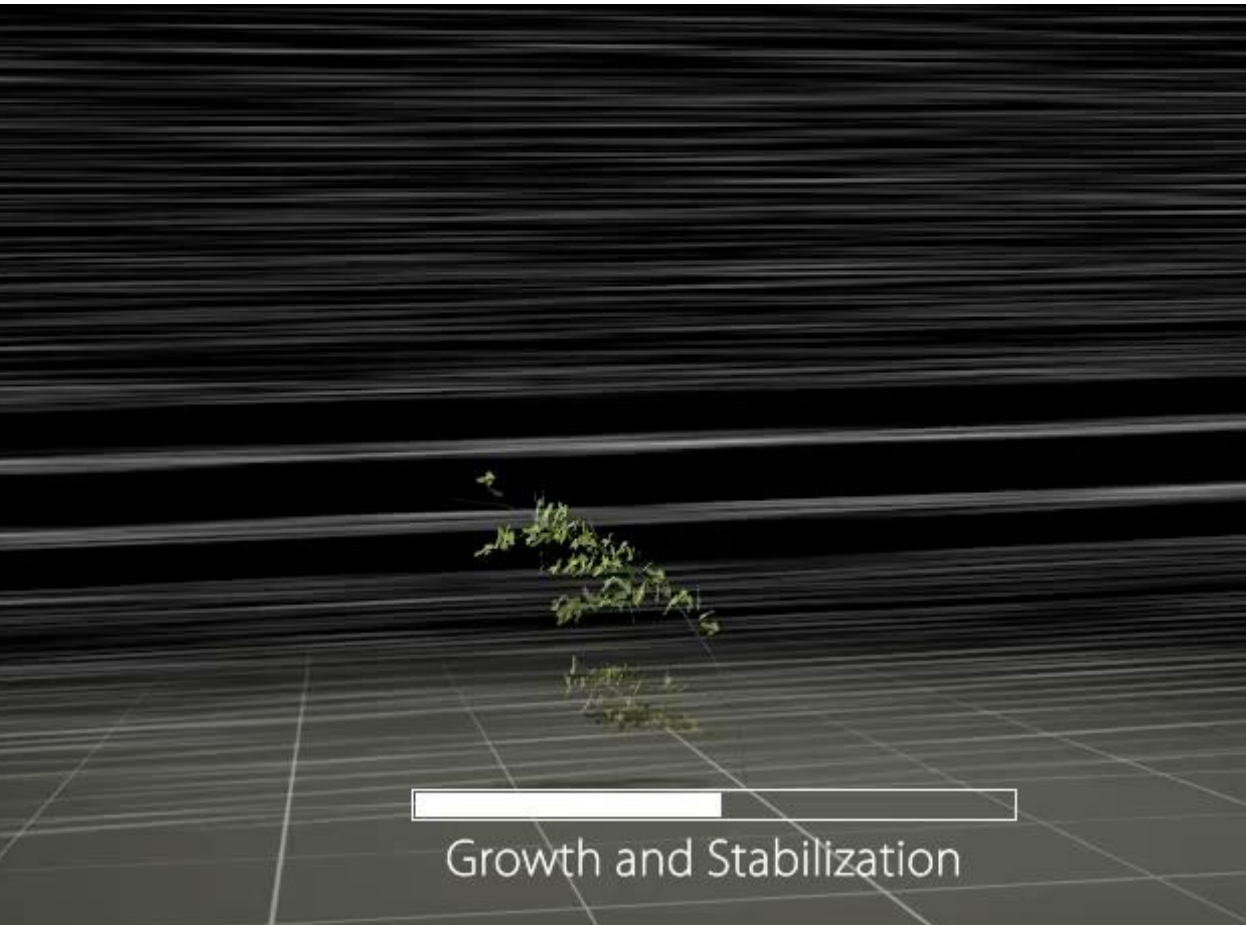
Bud Abrasion and Drying

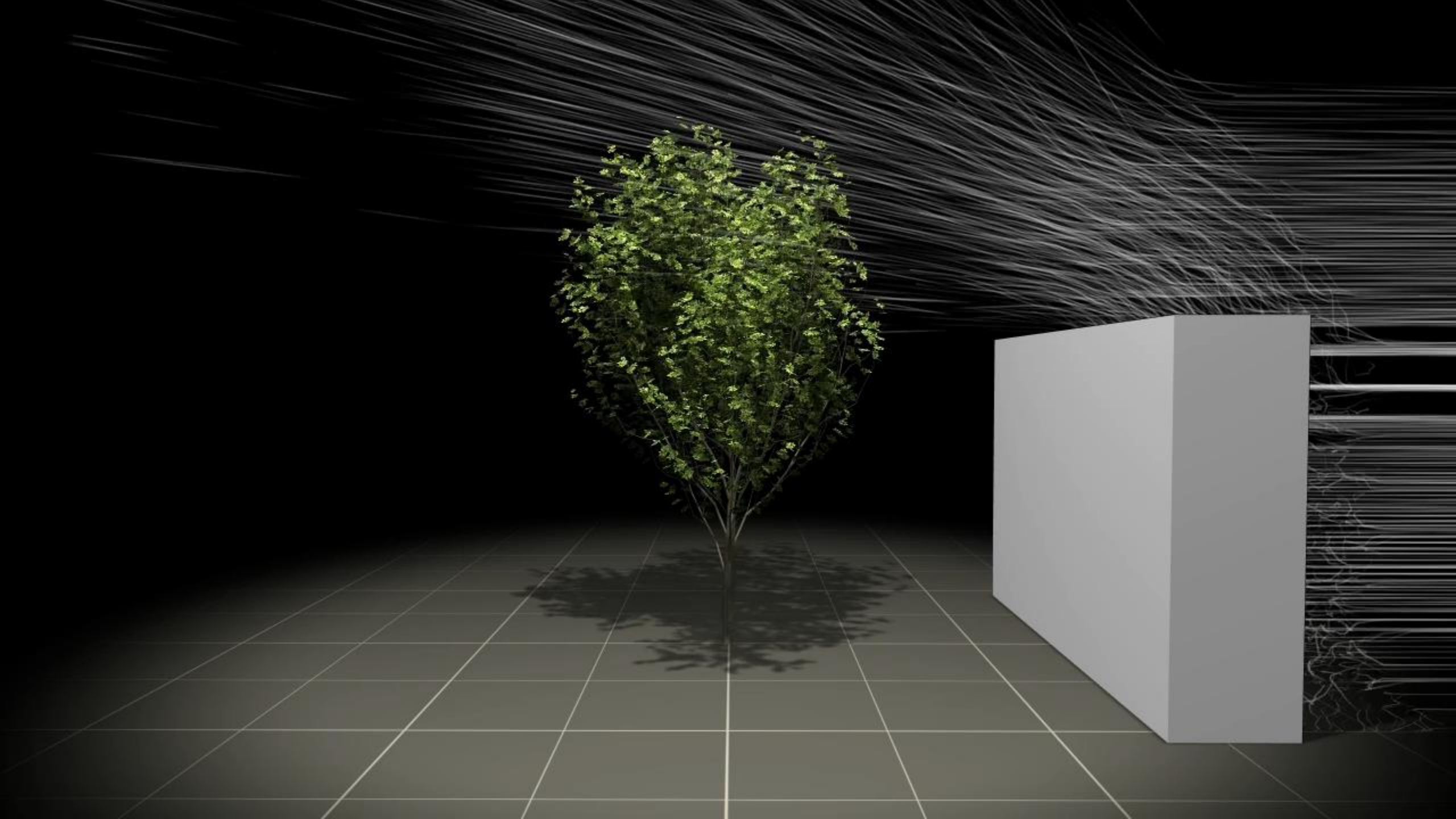
- Wind dries out or abrades buds
- Detect particles and neighboring branches
- User-defined threshold to terminate buds

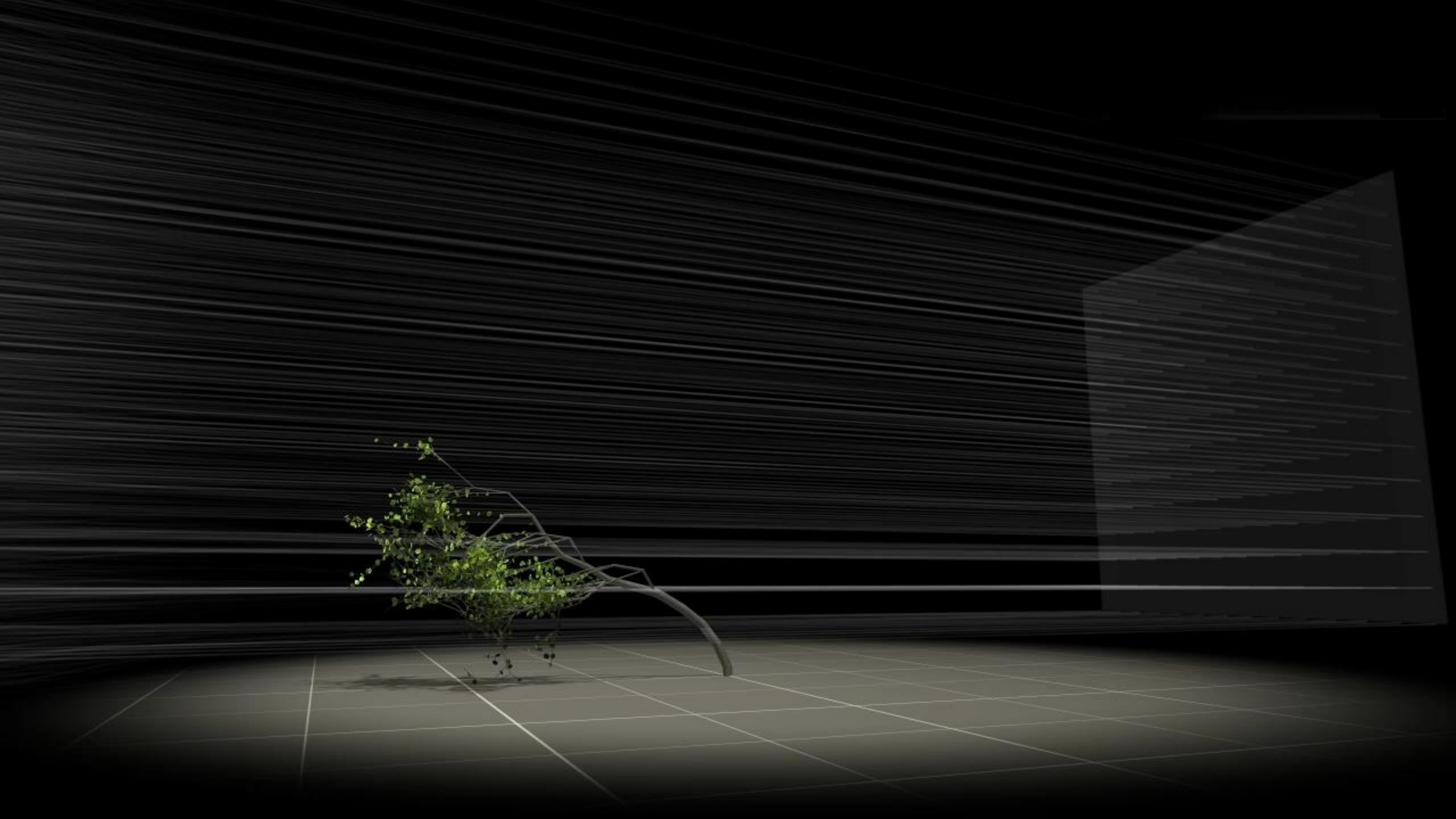
[Putz and Parker 1984]



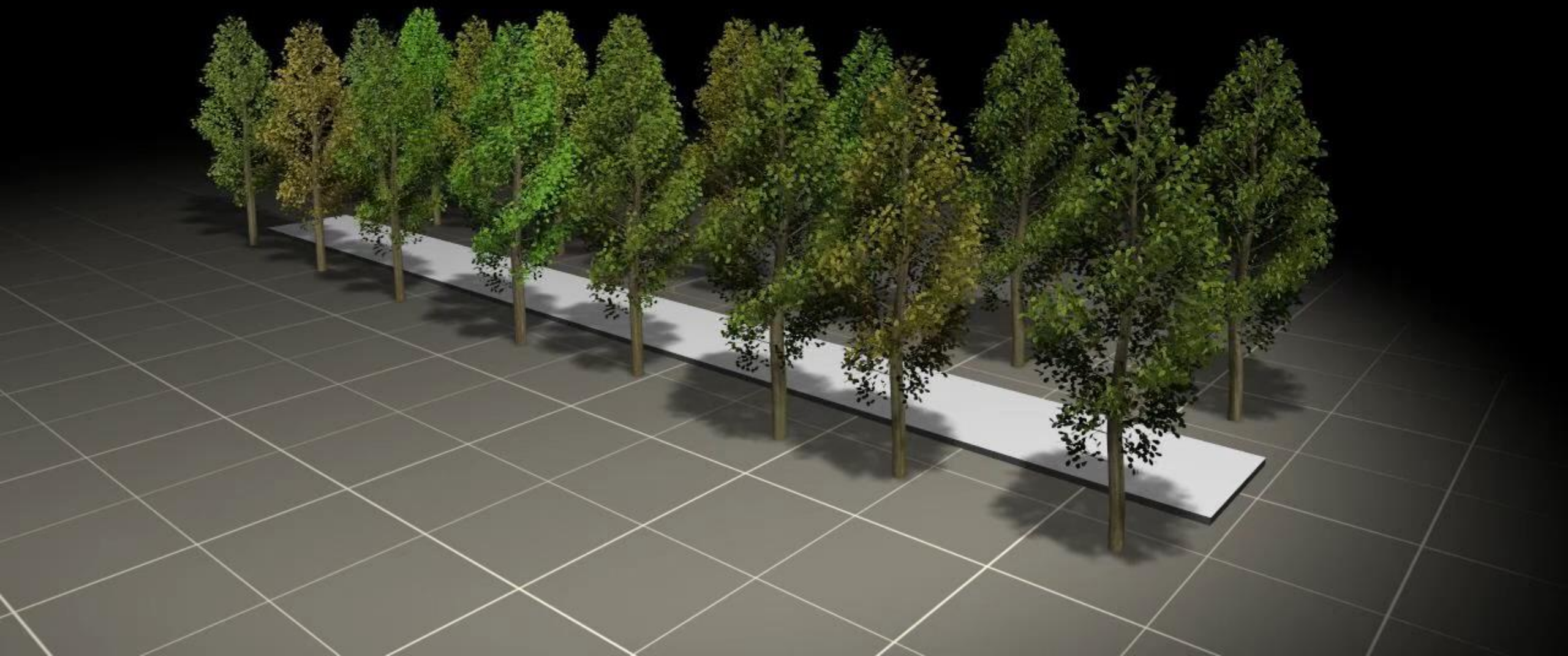
Off On







5 x faster



Modeling Plant Life in Computer Graphics

Reconstruction and Inverse Procedural Modeling

Siggraph 2016 Course

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Oliver Deussen, Baoquan Chen, Radomír Měch

Overview

Reconstruction and Inverse Procedural Modeling [30 minutes]

- From CT scans, flowers (**Ijiri**)
- From point sets (**Pirk, Chen**)
- Inverse Procedural Modeling (**Mech, Benes**)

Flower Modeling via X-ray Computed Tomography

- Takashi Ijiri, Shin Yoshizawa, Hideo Yokota, Takeo Igarashi. **Flower Modeling via X-ray Computed Tomography**, ACM Trans. Graph. Volume 33, Issue 4, Article No. 48, July 2014.



Background

Flower and plant modeling is important topic in CG

- CG Scene design / Simulation / Electric encyclopedia

Flower modeling is difficult



Many free-form components



Occluded structure

Goal- Reconstruct complicated and realistic flowers



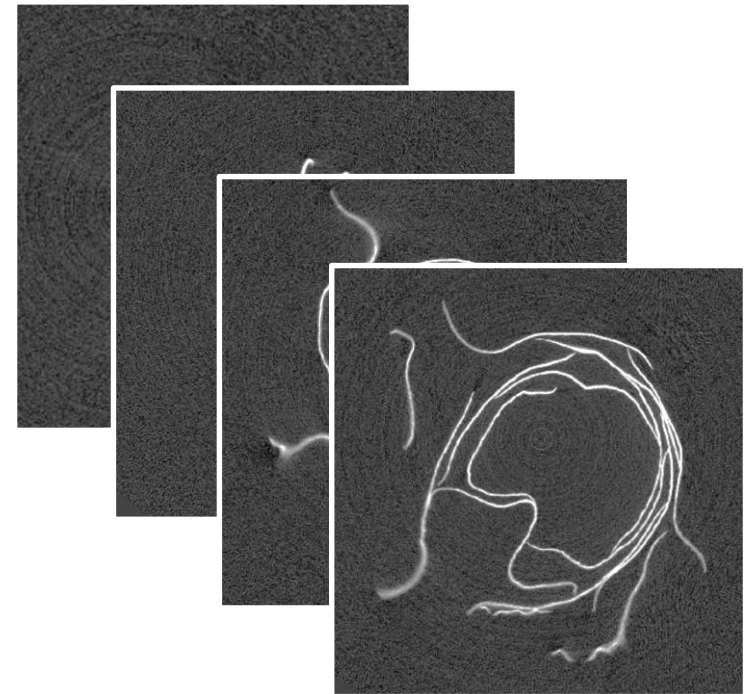
Approach Use X-ray CT



Fix a sample
on a tube



Scan the sample by industrial CT
Matsusada precision: *μ Ray8700*

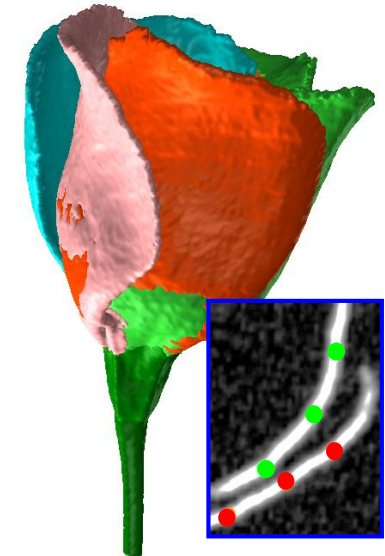
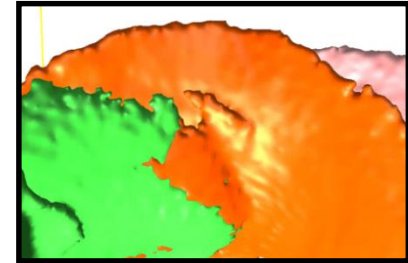
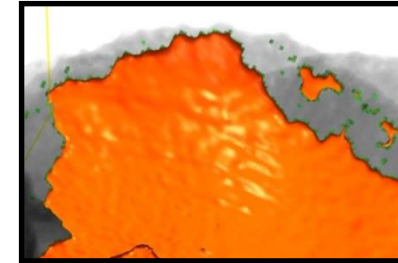
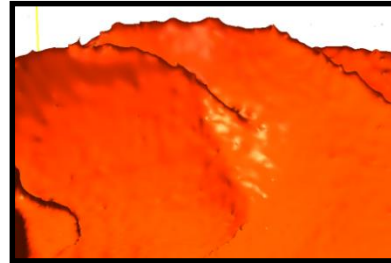
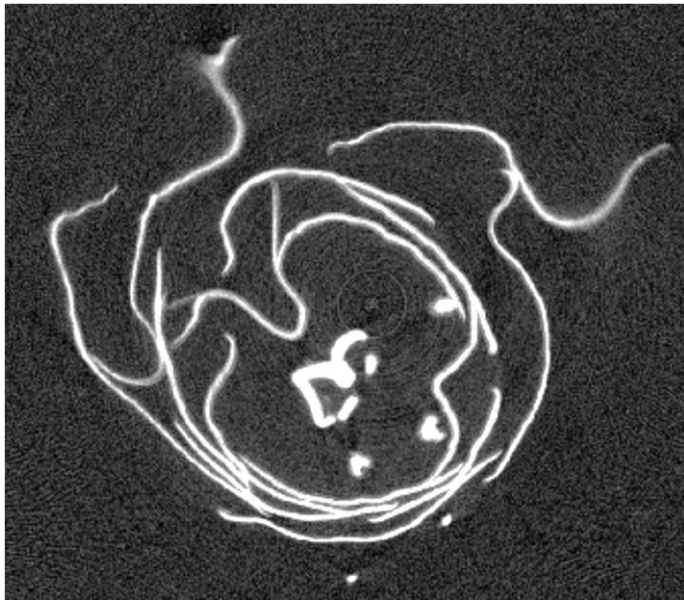


Obtain occlusion-free
flower CT volume image

Challenge – Segment volume into flower components

Flower components

- Thin shapes
- Similar CT intensity
- Contact one another



Iso surface

[Lorensen et al 1987]

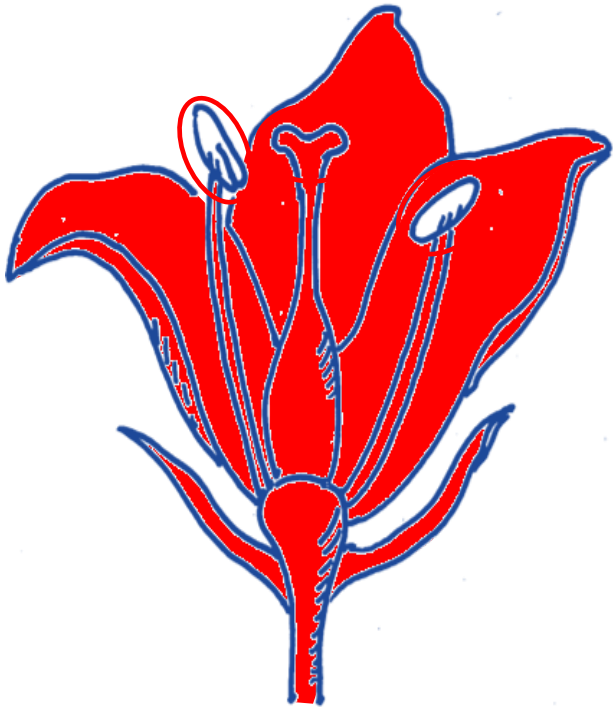
Graph Cut

[Boykov et al 2001]

Region Grow

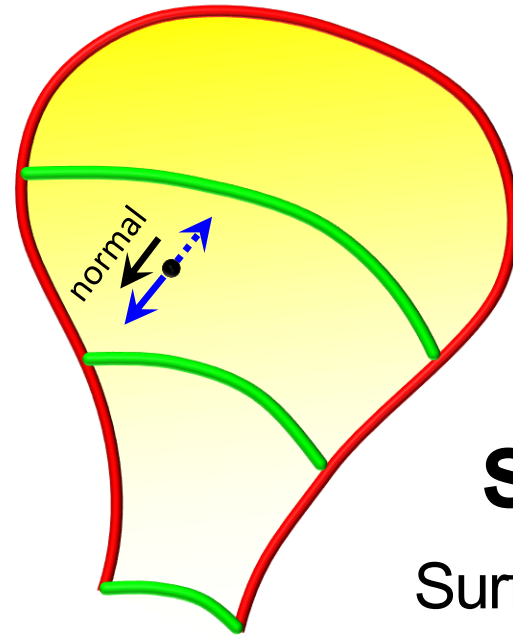
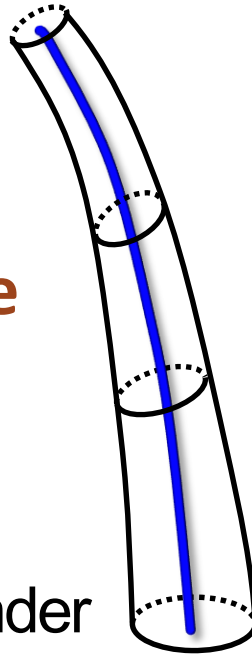
[Adms 1994]

Key idea – Approximate flower components with simple **primitives**



Pistils
Stamens
Receptacle
Stem
shaft

Curved cylinder
radius varies along axis



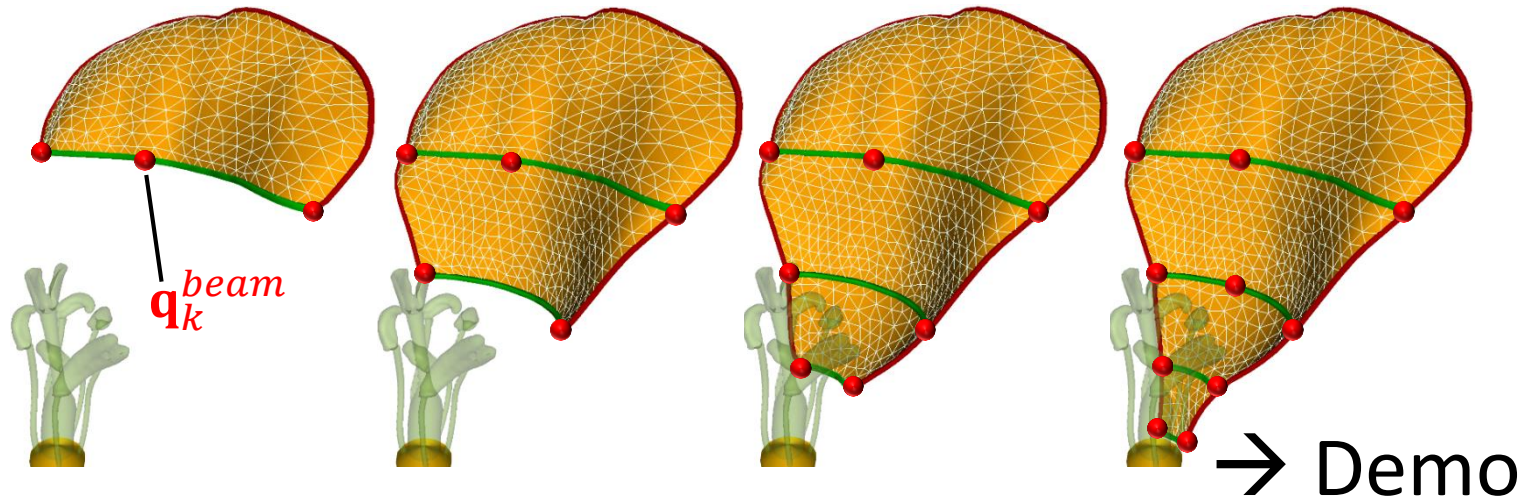
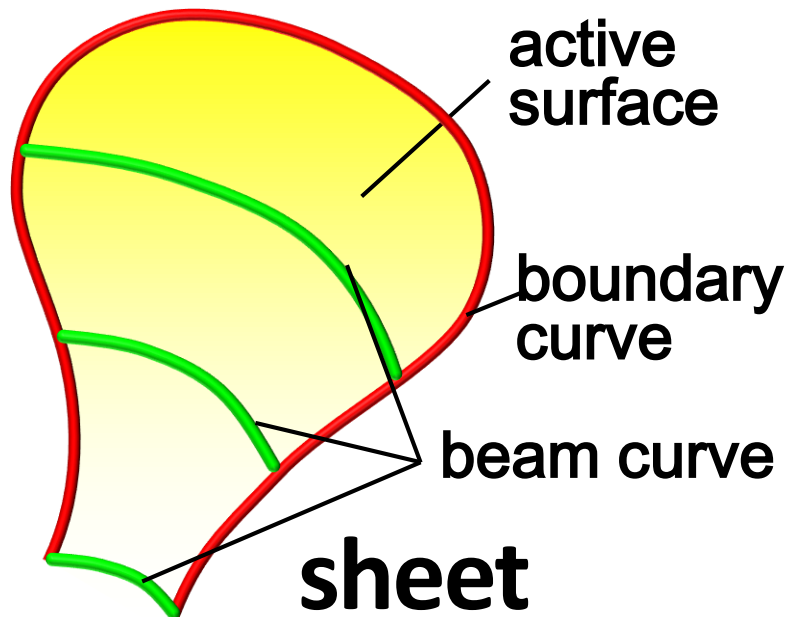
Petals
Sepals
sheet

Surface with
adaptive thickness

Present a UI to place primitives

Present novel active curve/surface to fit primitives

Modeling Petals & Sepals



Petal often appears as a curve on a horizontal cross section

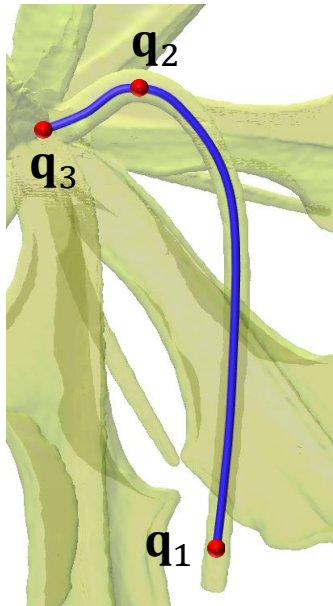
The user places CPs on a curve of the target petal

→ Beam/boundary curves & active surface is computed

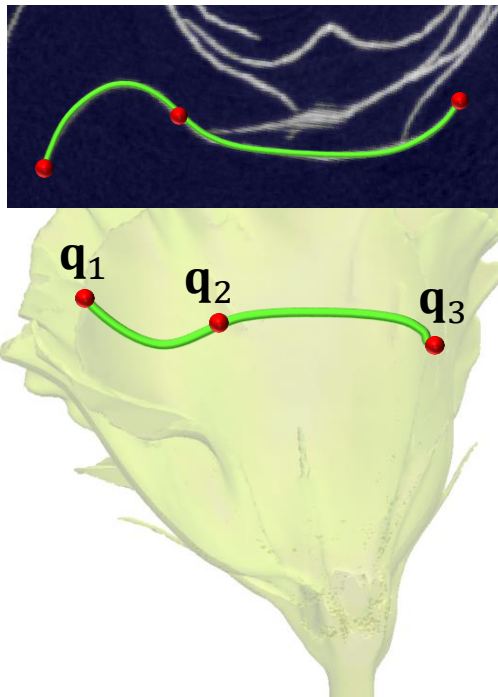
Active curves $C(t)$

Interpolate CPs ($\mathbf{q}_1, \mathbf{q}_2, \dots, \mathbf{q}_M$) smoothly

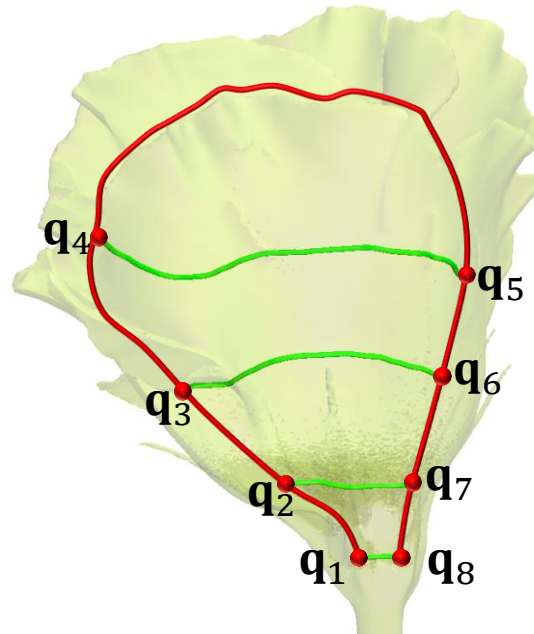
Trace their targets regions



Shaft axis



Beam

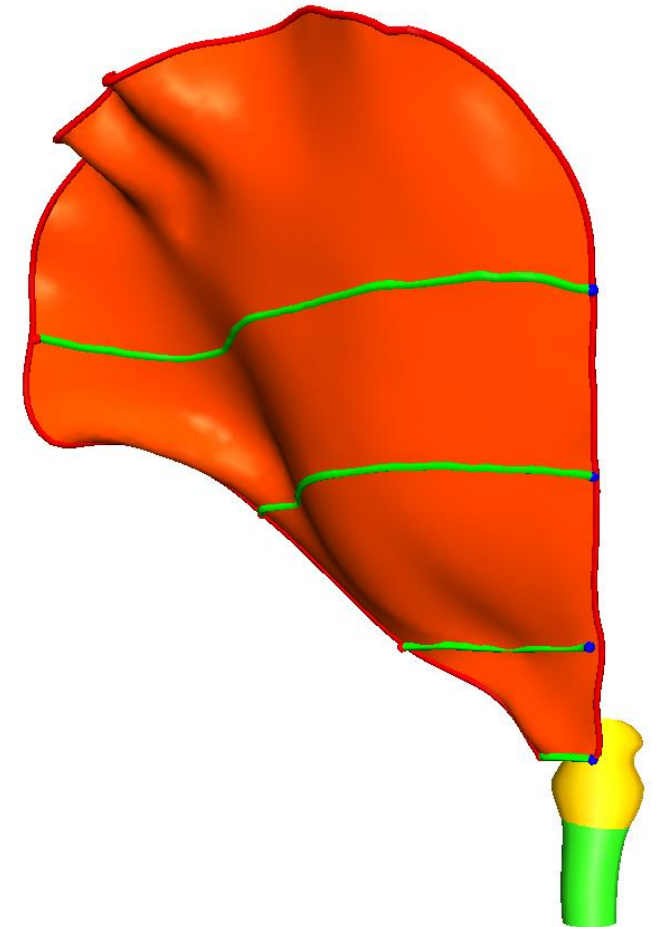


Boundary

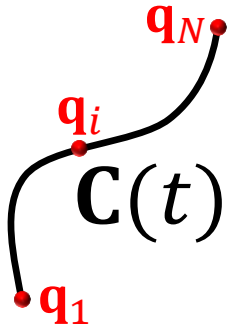
Active surface $S(u, v)$

Interpolate curve network

Trace target region



Active curves / surface energies



$$E_c = \int_{\Omega_c} \frac{1}{2} |\mathbf{C}''(t)|^2 + \alpha |\mathbf{C}'(t)^T \mathcal{M}(\mathbf{C}(t)) \mathbf{C}'(t)| dt$$

Smoothing effects

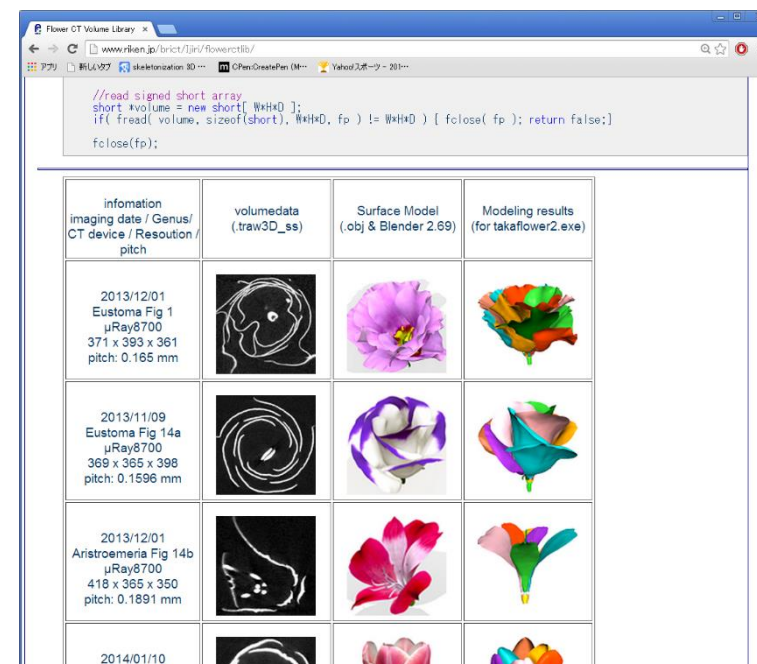


$$E_s = \int \int_{\Omega_s} \frac{1}{2} (\mathbf{S}_{uu}^2 + 2\mathbf{S}_{uv}^2 + \mathbf{S}_{vv}^2) + \beta |\mathcal{B}\mathbf{S}_u \times \mathcal{B}\mathbf{S}_v| dudv$$

Results

Present a flower modeling method via X-ray CT scanner

Achieved to reconstruct flowers with complicated structures



Our CT volumes are available
Google “**Flower CT volume library**”



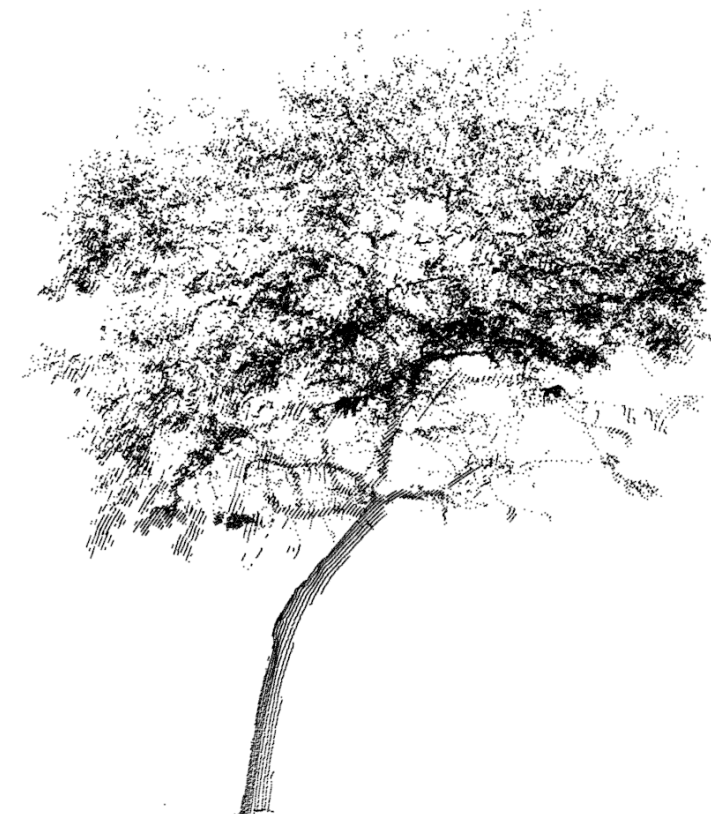
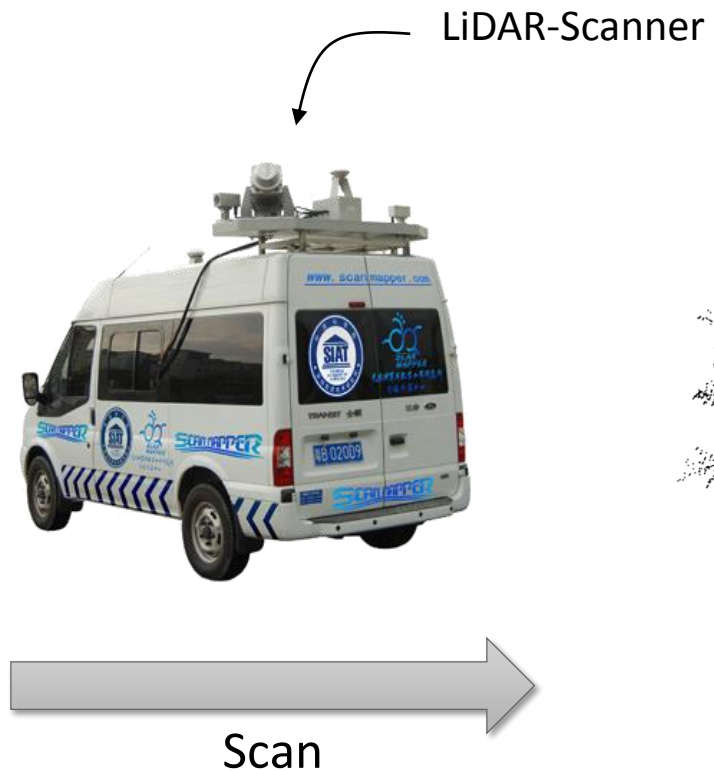
Texture-lobes for tree modelling

- Livny, Y., Pirk, S., Cheng, Z., Yan, F., Deussen, O., Cohen-Or, D., Chen, B. (2011) **Texture-lobes for tree modeling**. ACM Trans. Graph. 30, 4, 53:1–53:10.

Reconstruction of Urban Scenes

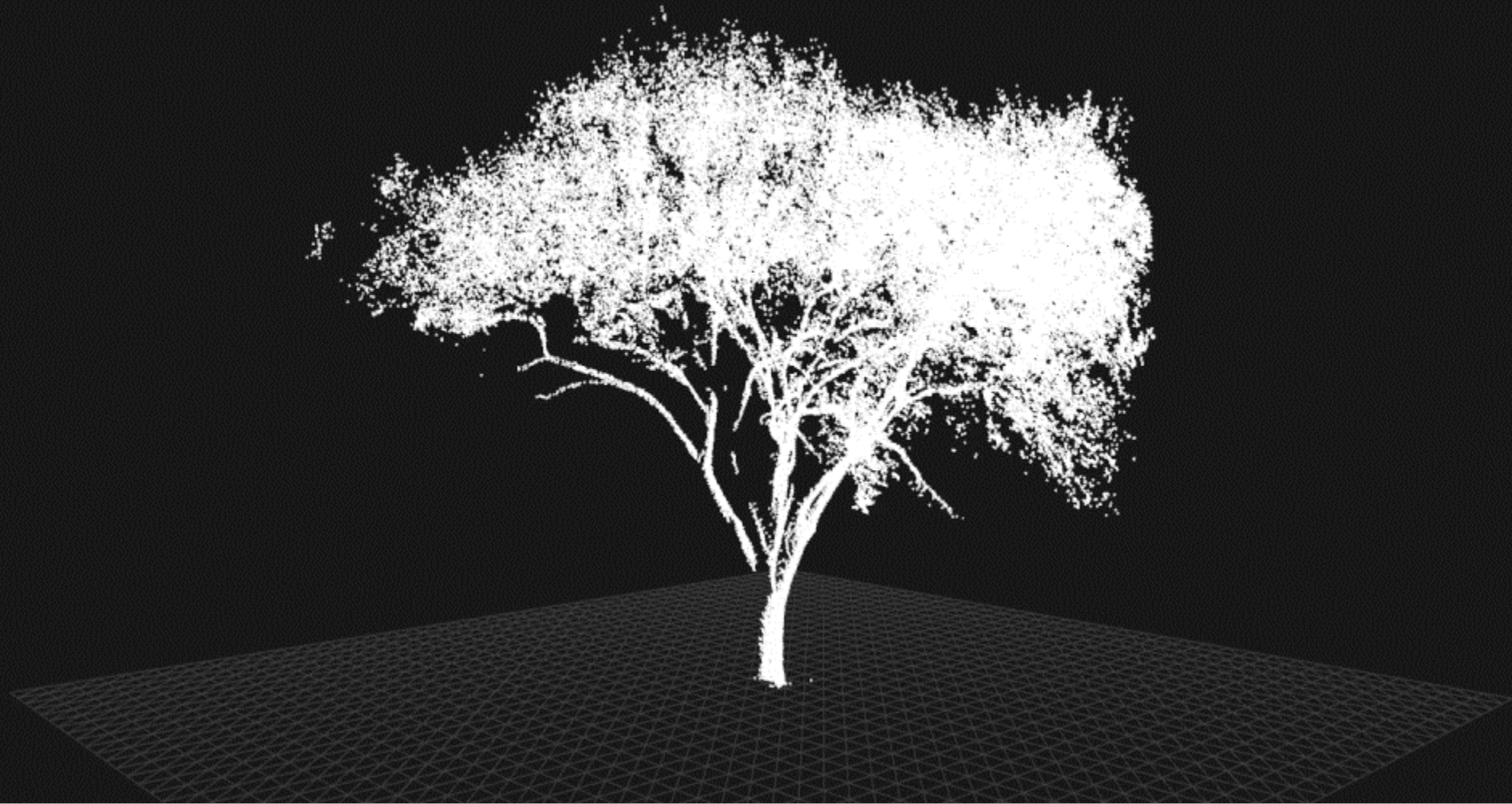


Real Tree

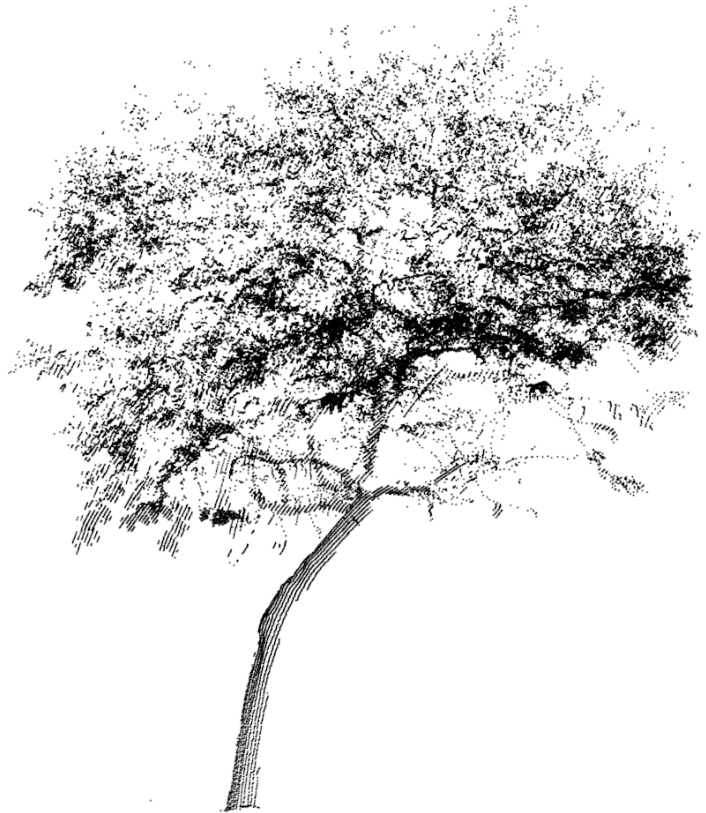


3D Point Cloud

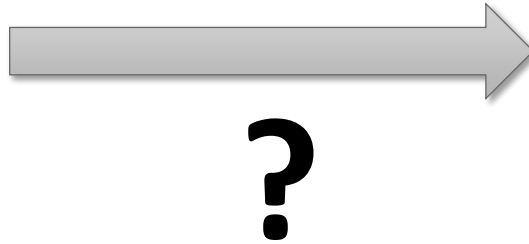
3D Point Sets



From Point Sets to Meshes



3D Point Cloud



3D Tree Model

A Tree is Complex



Human visual bandwidth is limited → abstraction

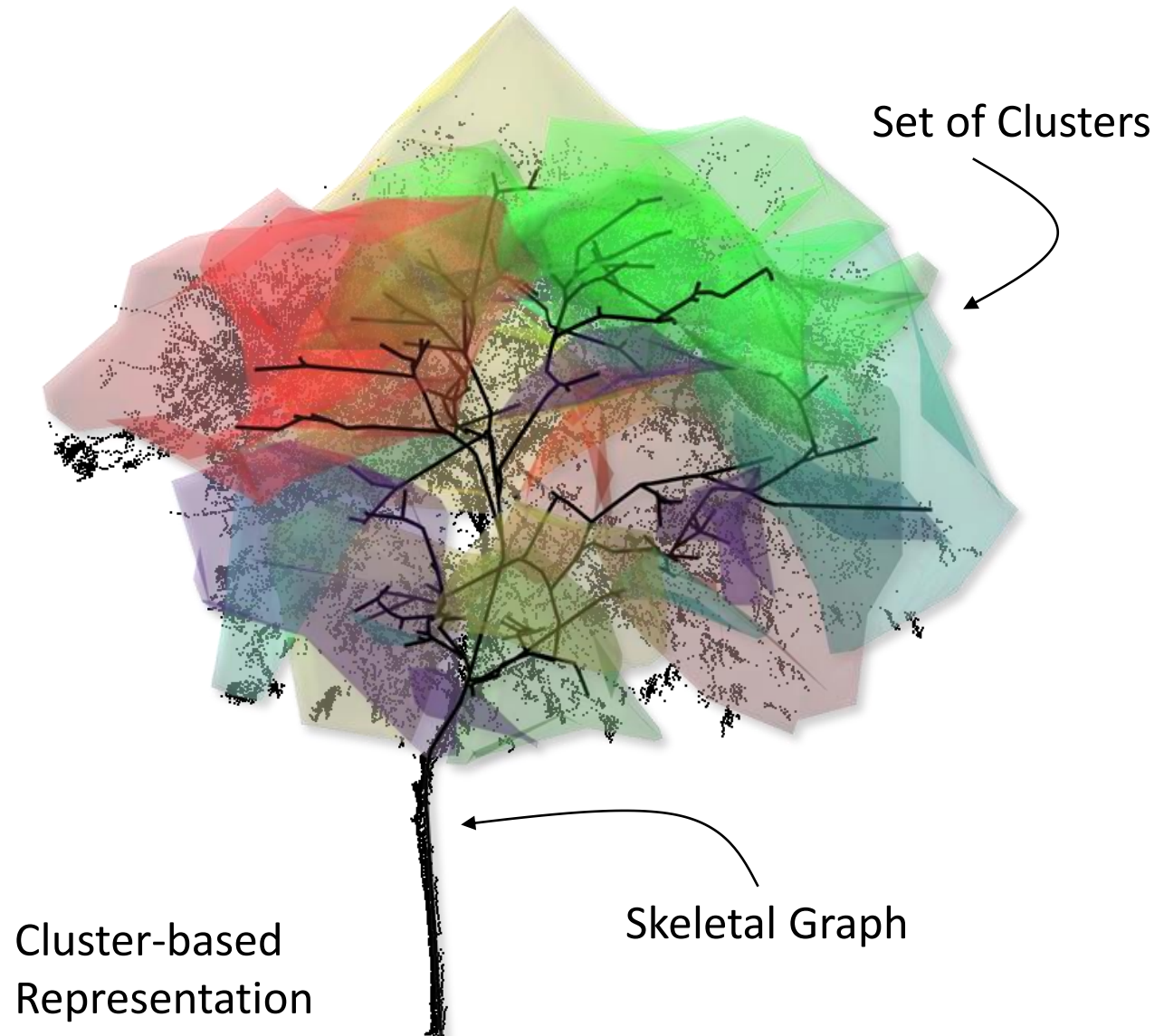
Cluster-based Representation

Separate leaf-points and branch-points.

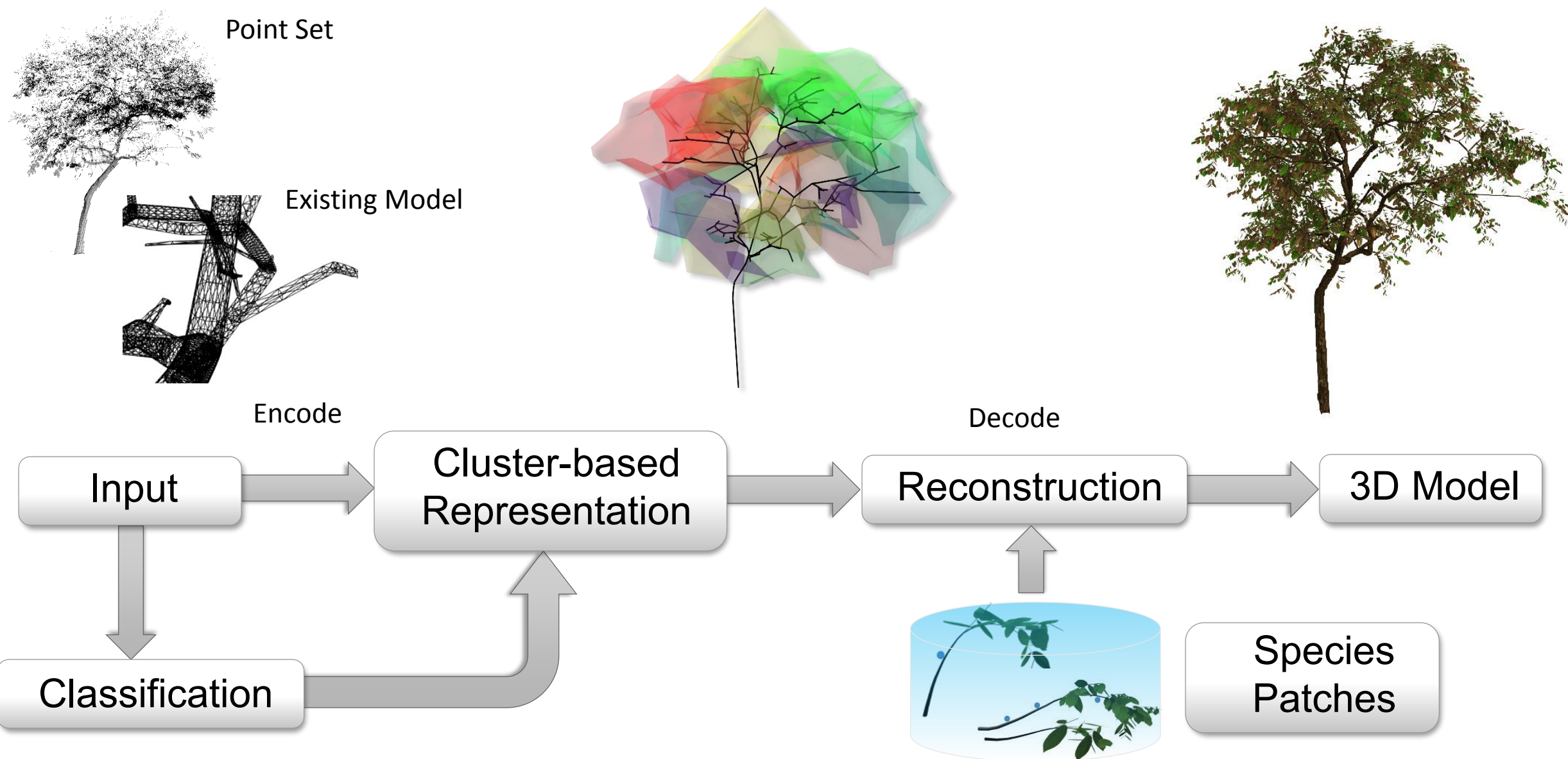
Minimum-weight spanning tree over the input.

Determine thickness of branches based on allometric rules.

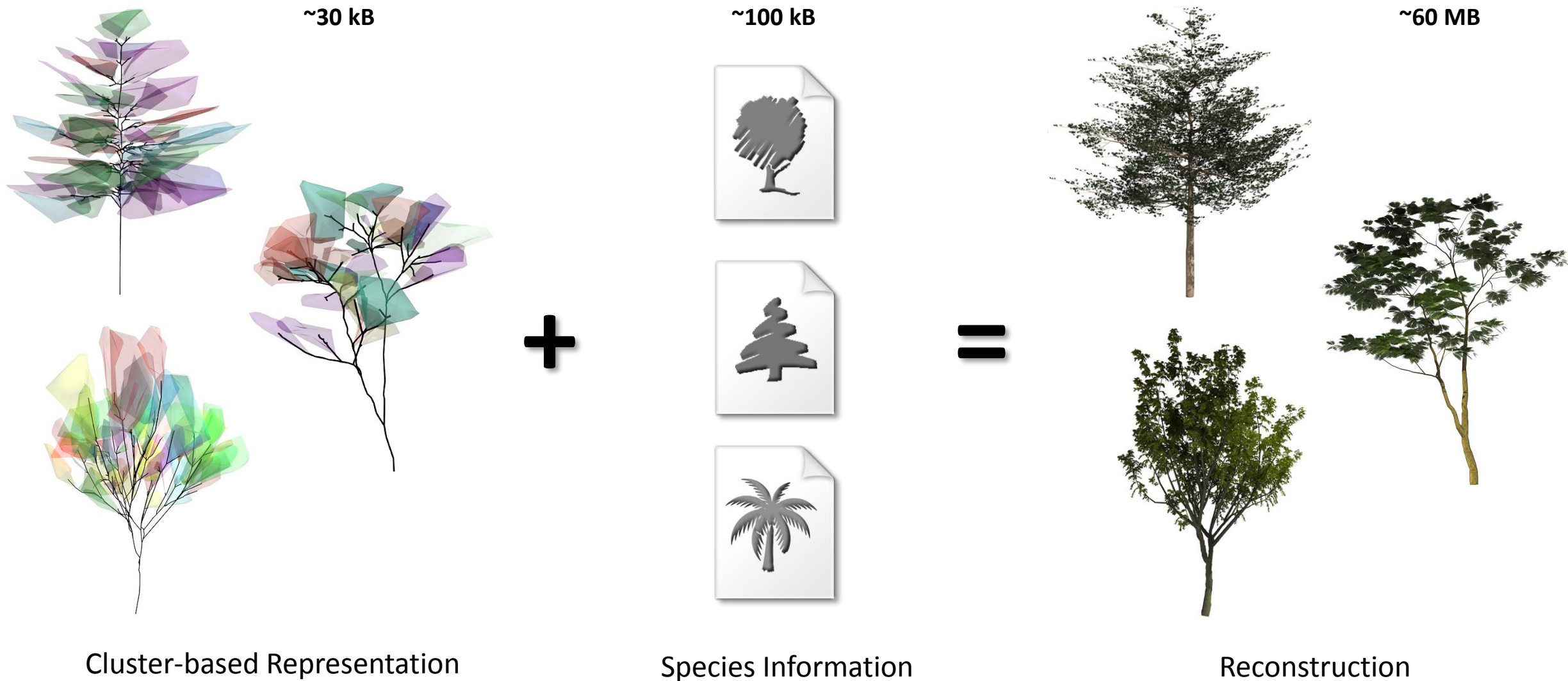
[Livny et al. 2011]



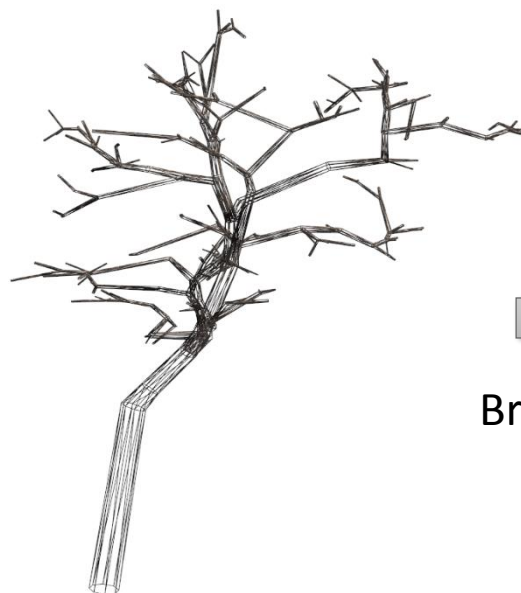
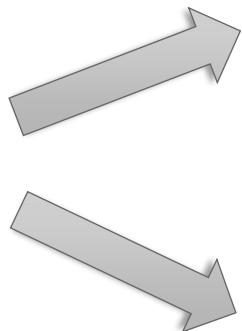
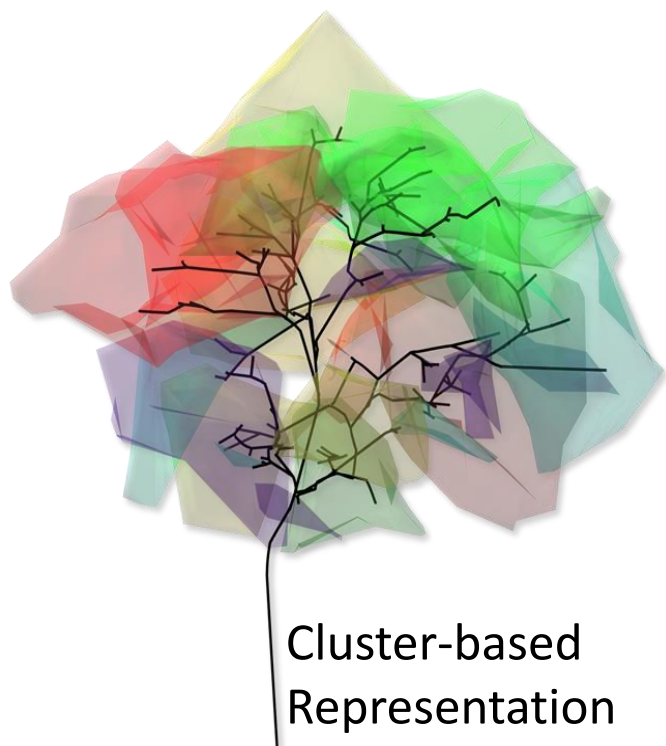
Pipeline



Resource Requirements

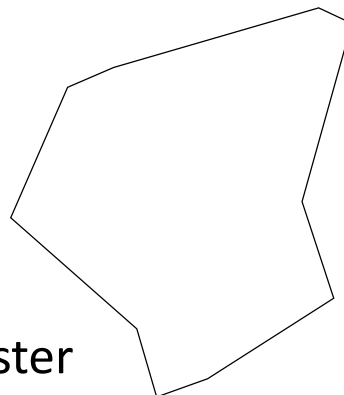


Reconstruction



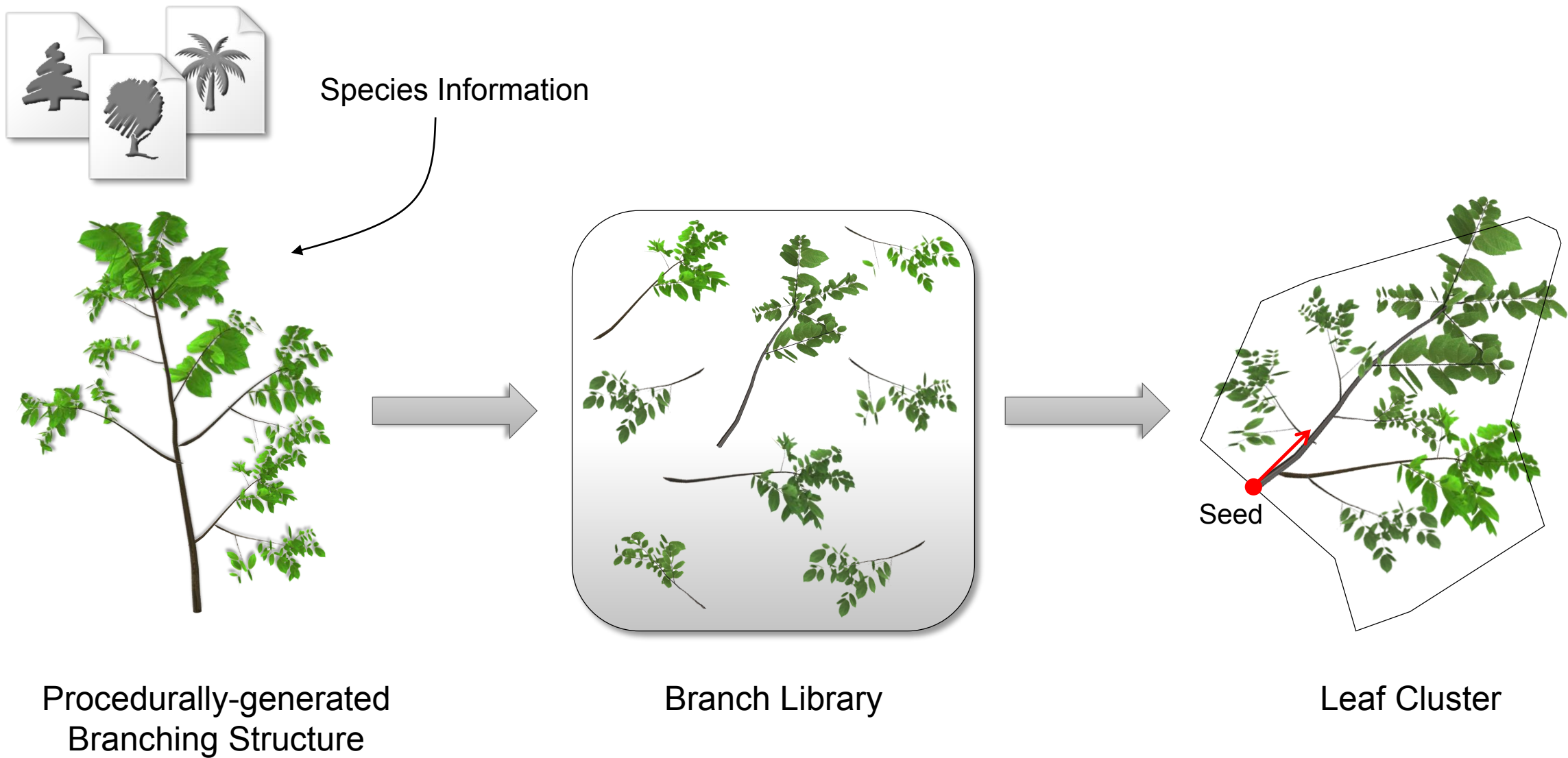
Twigs + Leaves

Cluster

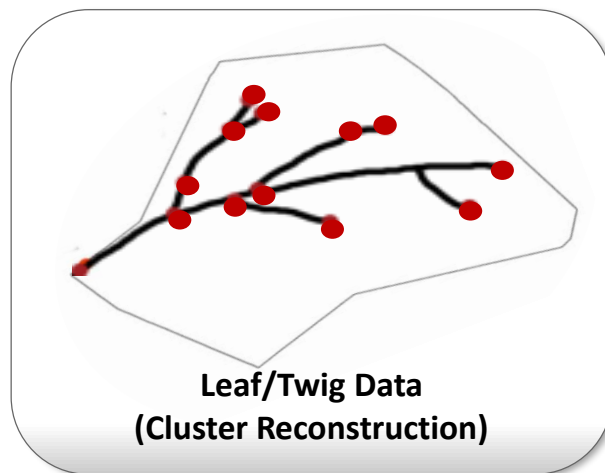
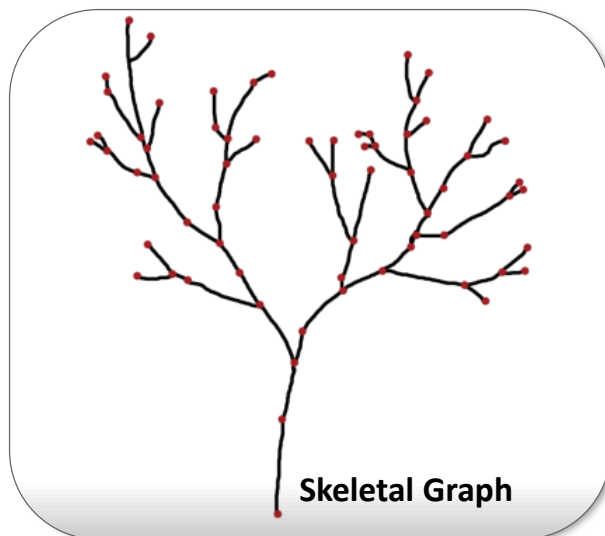


?

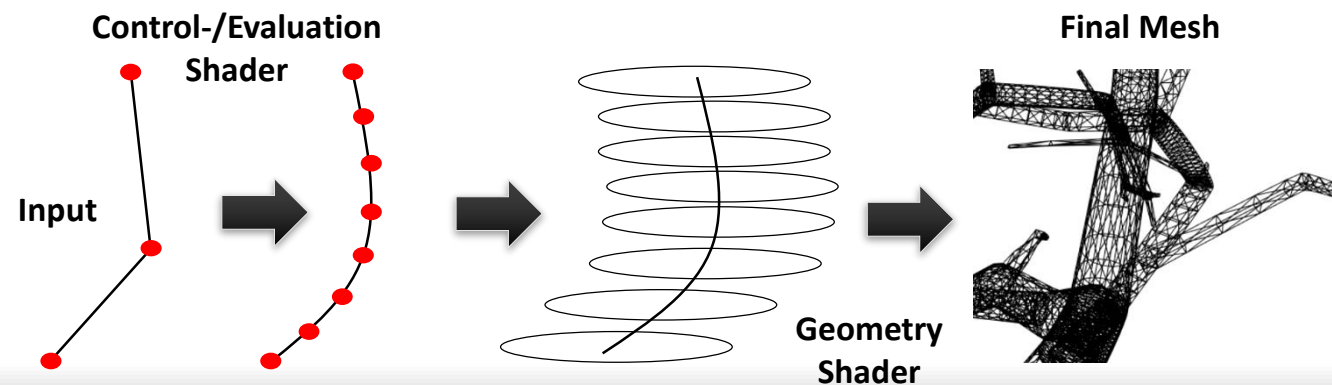
Geometry Synthesis



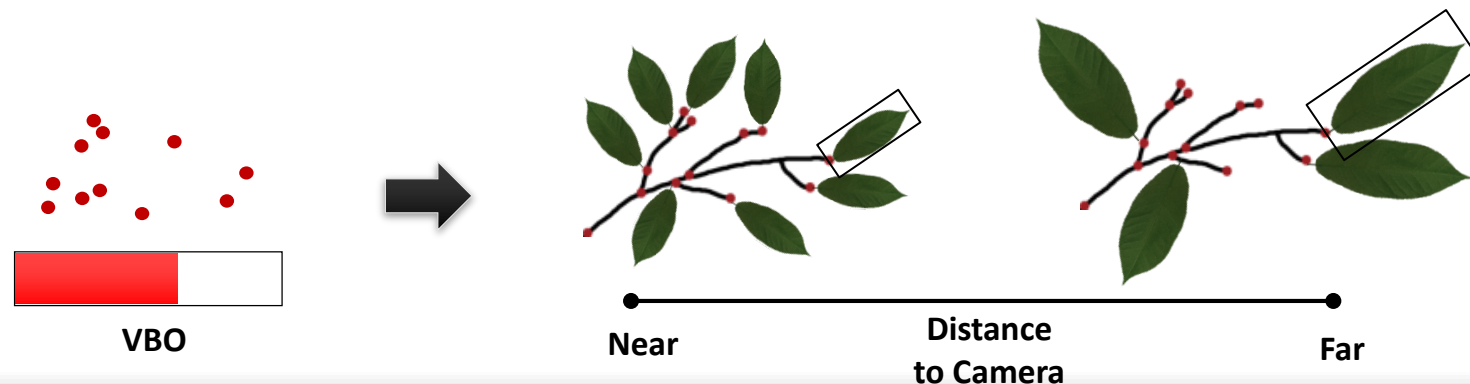
Mesh Construction



Branches: Mesh Generation [Bloomenthal 1985]



Leaves



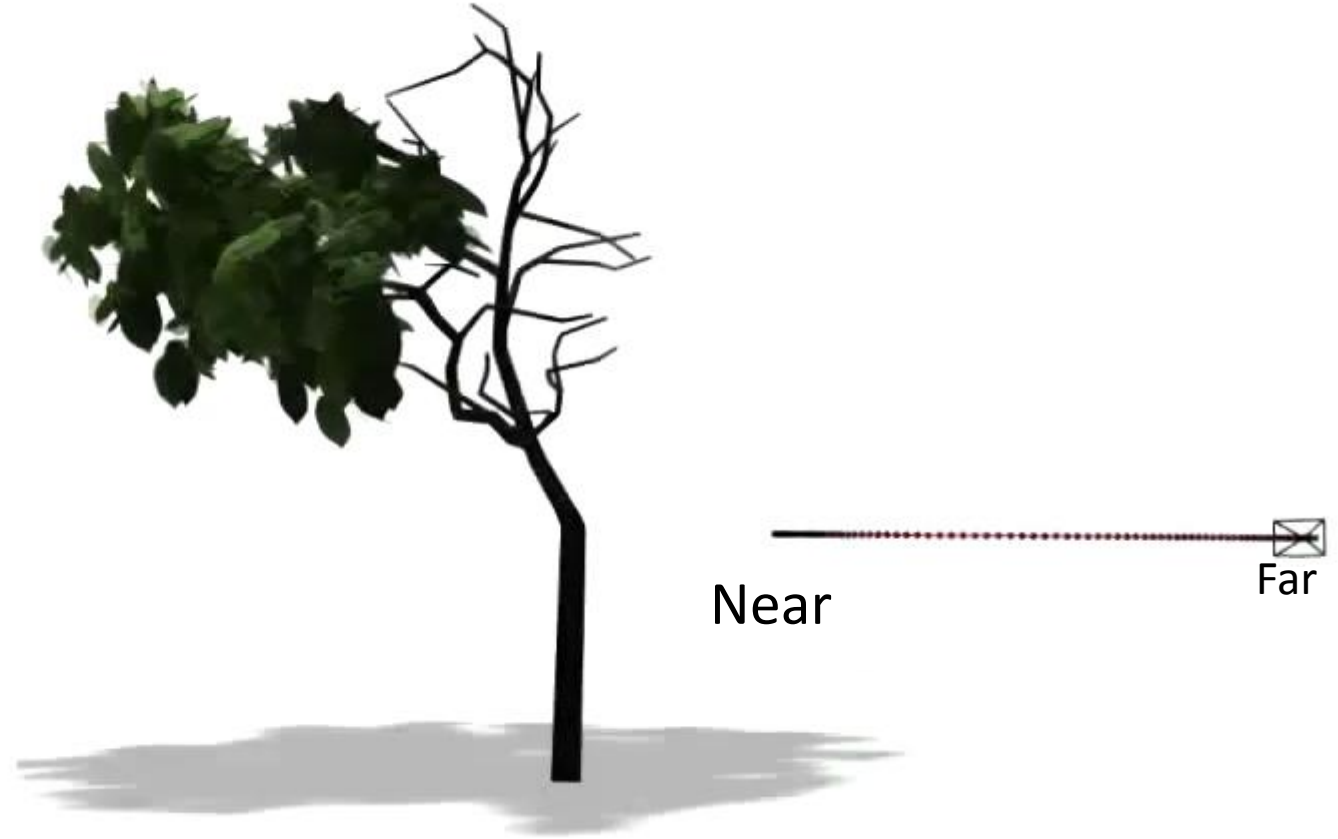
CPU | GPU

Dynamic Level of Detail

[Cook et al. 2007]

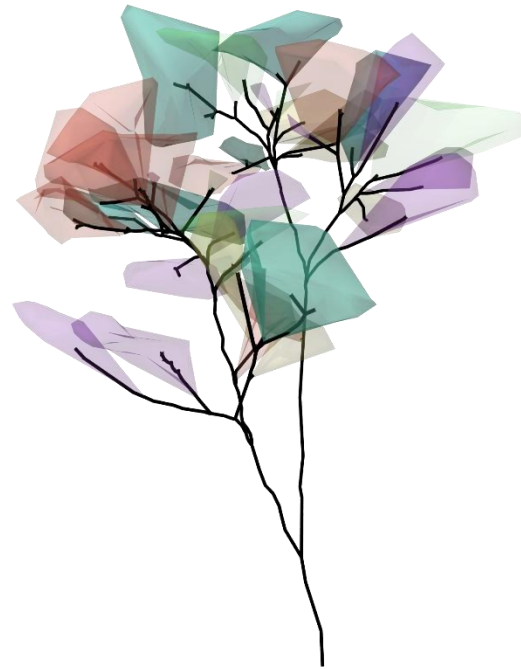


Camera View



Object View

Results: Delonix



Urban Reconstruction



Analyzing Growing Plants from 4D Point Cloud Data

- Li, Y. Fan, X., Mitra, N. J., Chamovitz, D., Cohen-Or, D., Chen, B. (2013). **Analyzing growing plants from 4D point cloud data.** *ACM Trans. Graph.* 32, 6, Article 157

Time-lapse images of growing plants



Video courtesy to [Neil Bromhall](#) on Youtube: [Sycamore seedling growing time lapse](#)₁



Time-lapse of 3D Point Cloud (4D Point Cloud)



Day 12

Charactering Plant Growth (1)

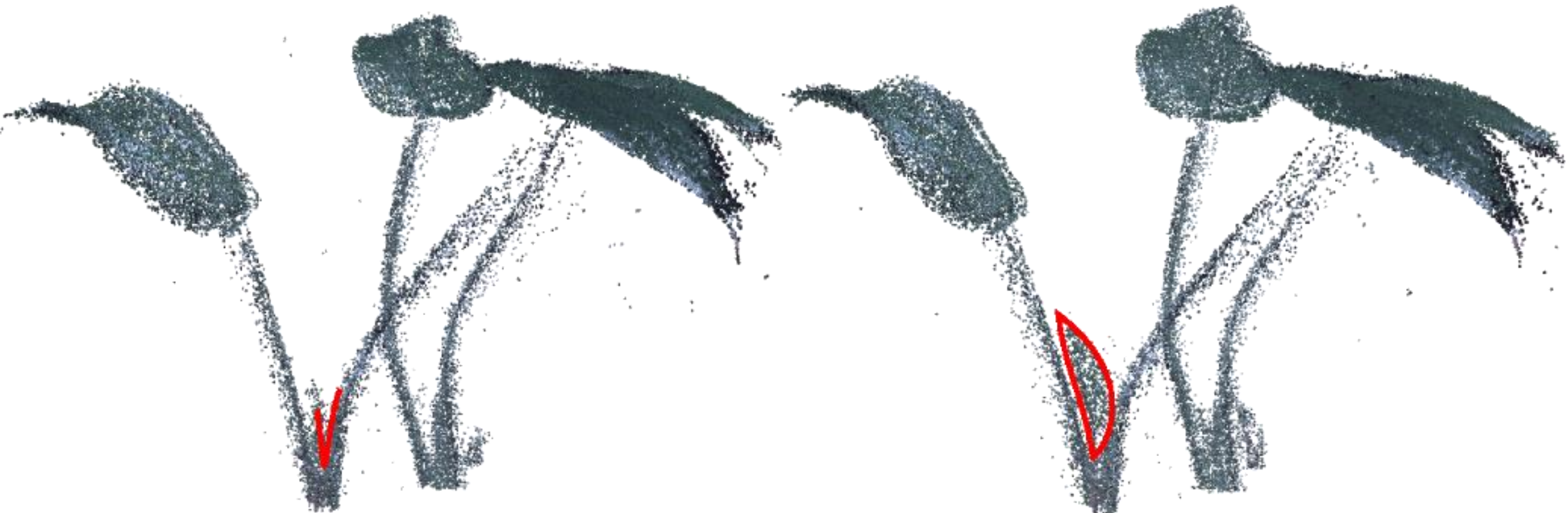
- Quantitative properties
 - Area, volume, etc.
 - Better in organ level

Huge amount of work!!!



Charactering Plant Growth (2)

- Growth events (qualitative changes)



Day 33

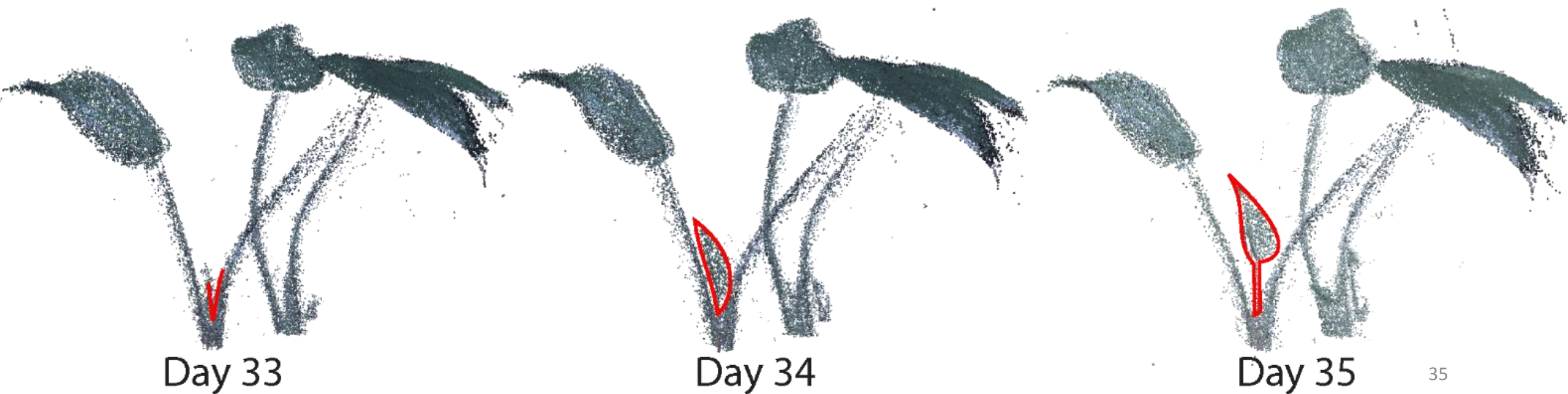
Bifurcation

Day 34

Budding

Challenges

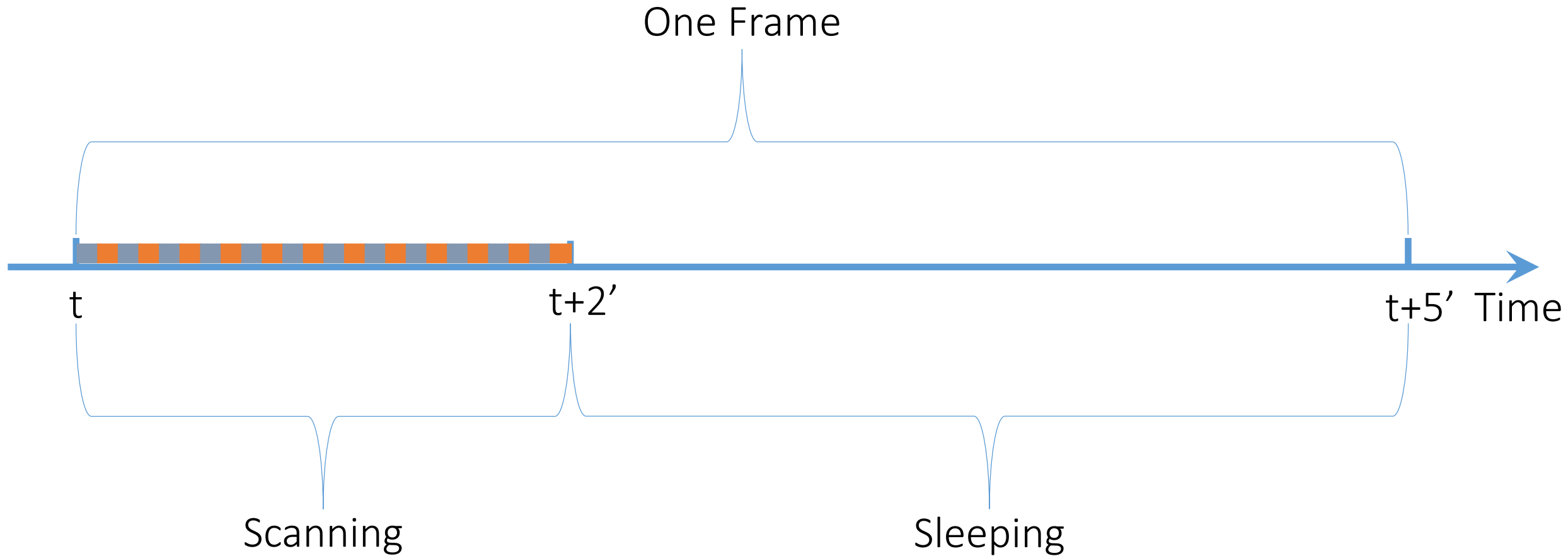
- Large deformation (violating incompressibility assumption)
- Large topology change
- No shape template
- Growth events
 - Subtle start (ending)
 - Similar, but not same
 - Ambiguities



Scanning system (1)



Scanning system (2)



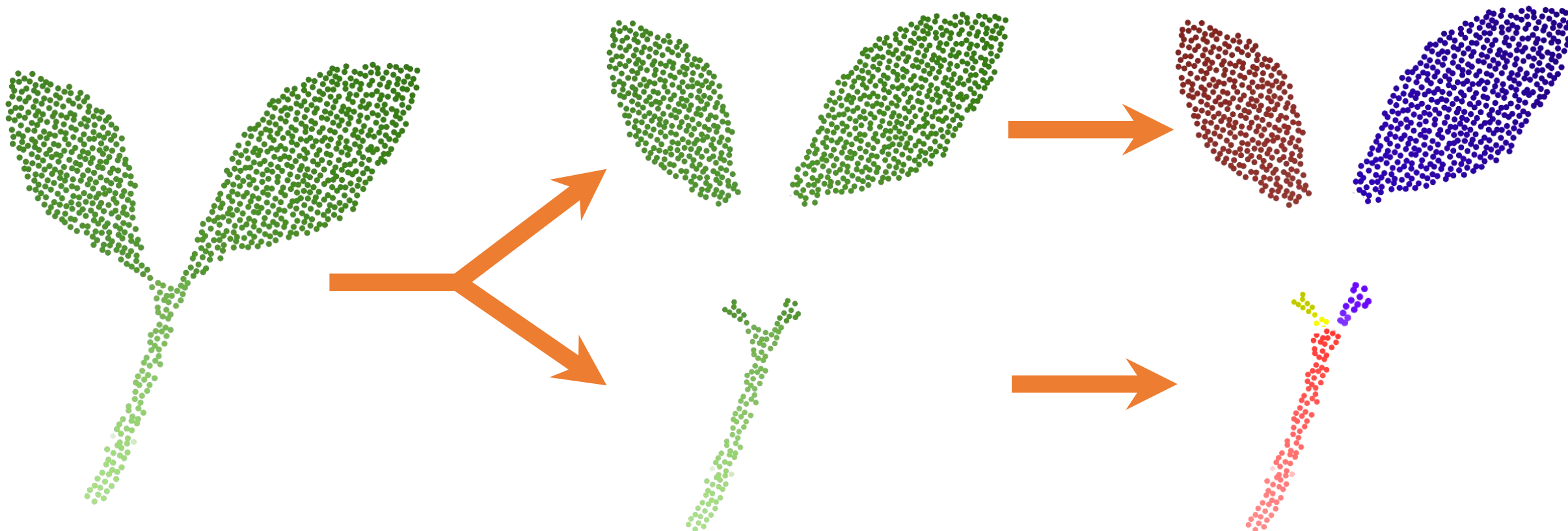
- structured light capturing
- turn table rotation (30°)

Detecting growth events → counting organ number



Counting organ number → point cloud segmentation

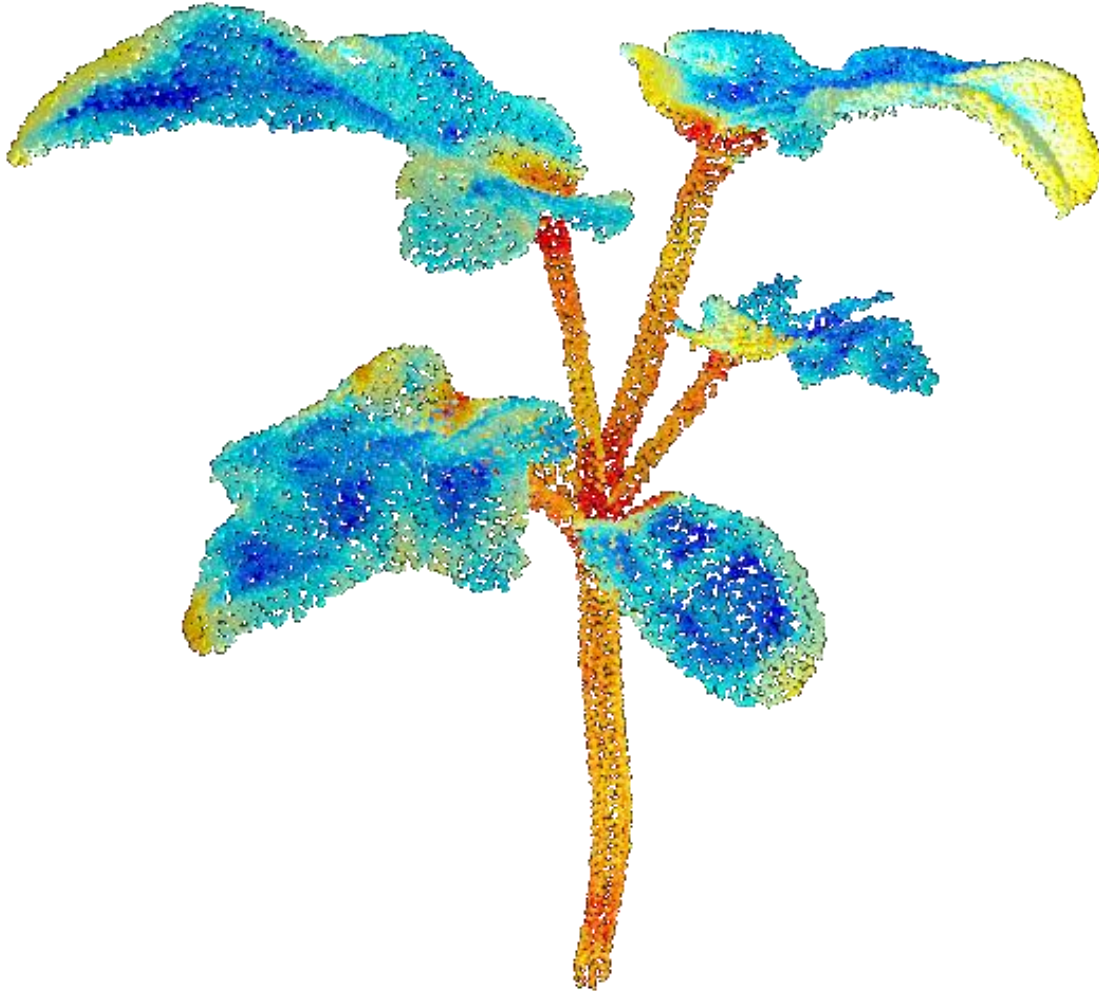
Algorithm pipeline: Two-stage Segmentation



Leaf-stem classification
Binary labelling problem

Individual organ segmentation
Multi-labelling problem

Leaf-stem classification: discriminative feature



Leaves are more “flat”!

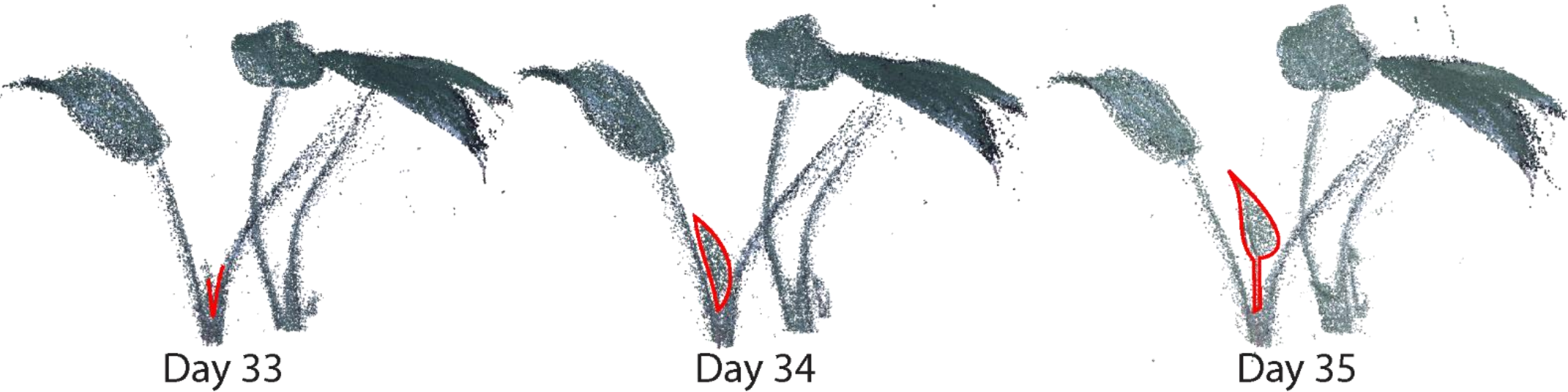
Find $f_B: P^t \rightarrow \{L, S\}$

$$f_B(p^t) = \begin{cases} S, & \text{if } C(p^t) > t \\ L, & \text{if } C(p^t) \leq t \end{cases}$$

Curvature $C(p^t)$ of Plant Points

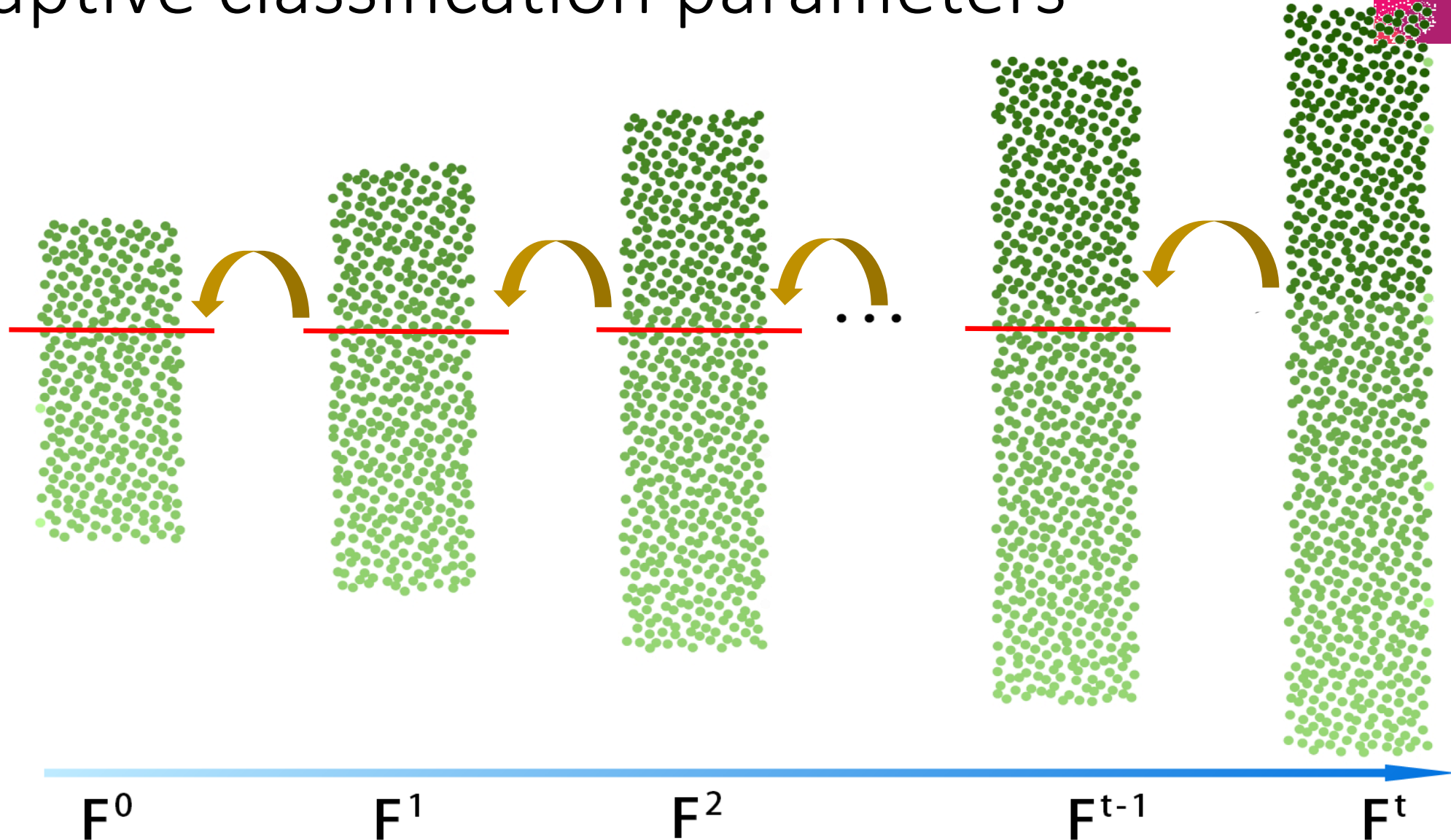
Mature leaves are more “flat” than stems.

New leaves can be less “flat” than some stems.



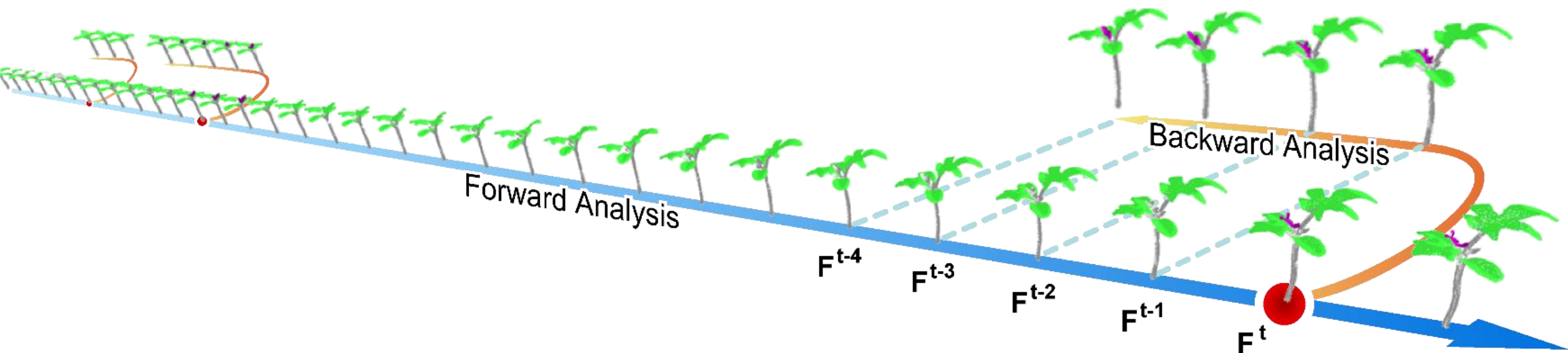
$$f_B(p^t) = \begin{cases} S, & \text{if } C(p^t) > t \\ L, & \text{if } C(p^t) \leq t \end{cases}, t \text{ has to be adaptive!}$$

Adaptive classification parameters



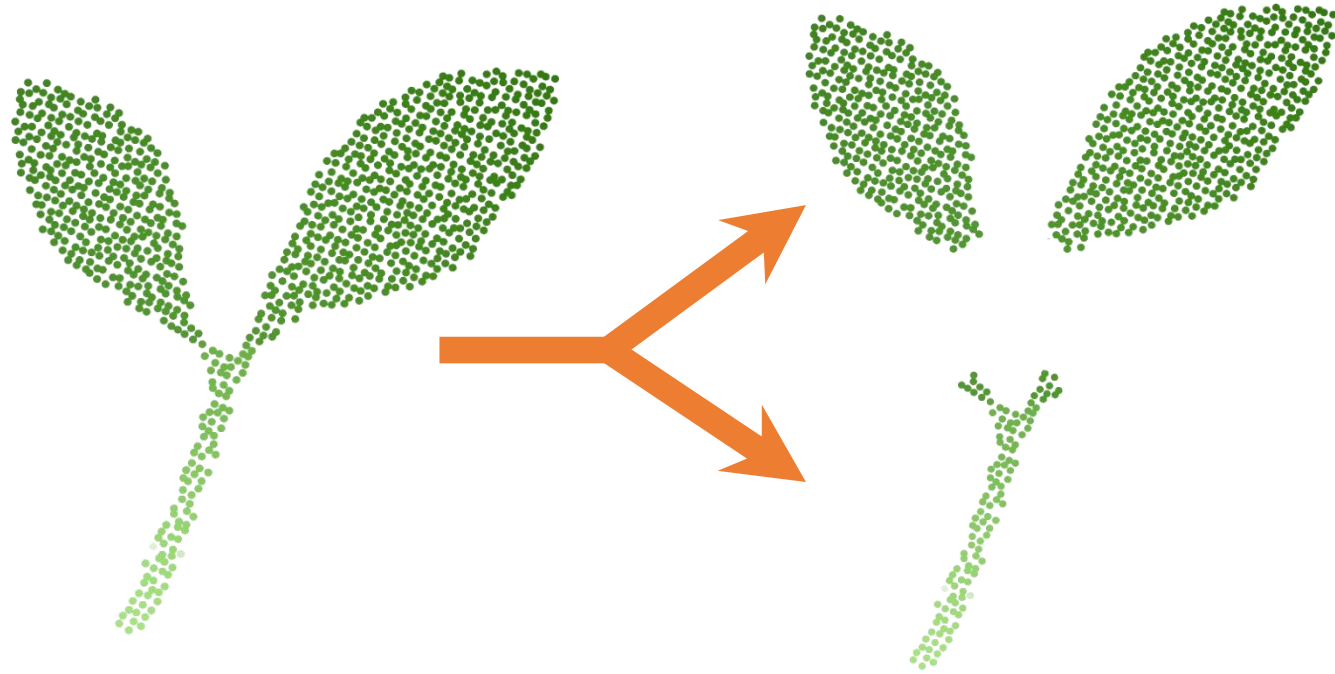
Growing leaf and stem in the feature space

Fwd-bwd analysis: bring back information from future



- Fwd analysis: detecting strong evidences
- Bwd analysis: smarter with the “after-effect”

Leaf-stem classification: MRF with known labels



Find $f_B: P^t \rightarrow \{L, S\}$, that minimizes

$$E(f_B) = \sum_{p^t \in P^t} D_{p^t}(f_B(p^t)) + \sum_{p^t, q^t \in N_{pt}} V(f_B(p^t), f_B(q^t)),$$

where $N_{pt} = \{(p^t, q^t) \in \text{Delaunay}(P^t): |p^t - q^t| < 3\text{mm}\}$.

Leaf-stem classification: data term (1)

$$D_{p^t}(L) = \begin{cases} \max(R(p^t) - R(L_{l_*}^{t\pm 1}), 0), & \text{if } \Phi > 0 \\ R(p^t) - \mathfrak{R}_L, & \text{if } \Phi = 0 \end{cases}$$

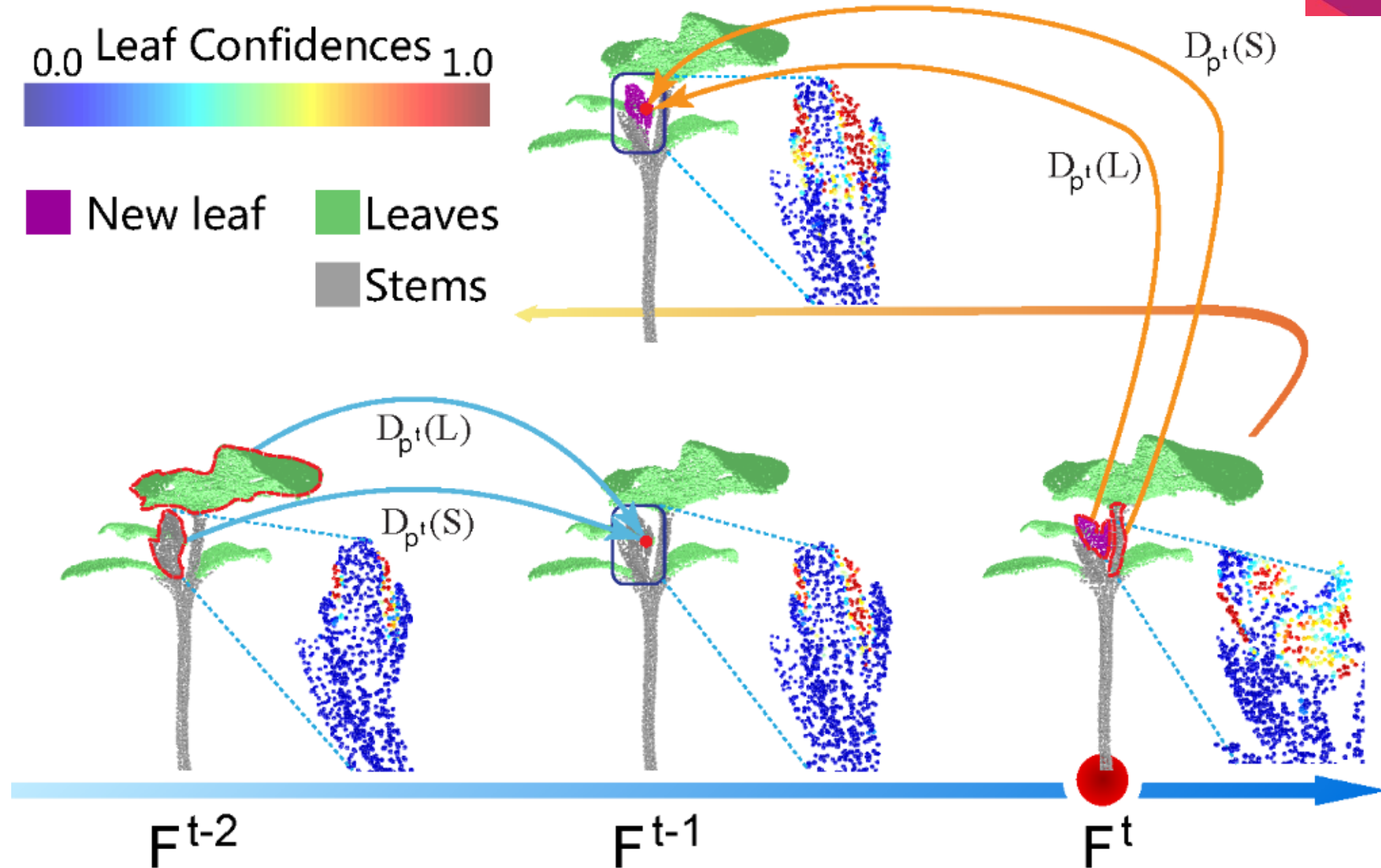
$$D_{p^t}(S) = \begin{cases} \max(R(S_{s_*}^{t\pm 1}) - R(p^t), 0), & \text{if } \Phi > 0 \\ \mathfrak{R}_S - R(p^t), & \text{if } \Phi = 0 \end{cases}$$

where $\Phi = |\{L_l^{t\pm 1}\}| \times |\{S_s^{t\pm 1}\}|$.

- **Spatial** and **temporal** adaption.
- Rarely relies on **global parameters**.



Leaf-stem classification: data term (2)

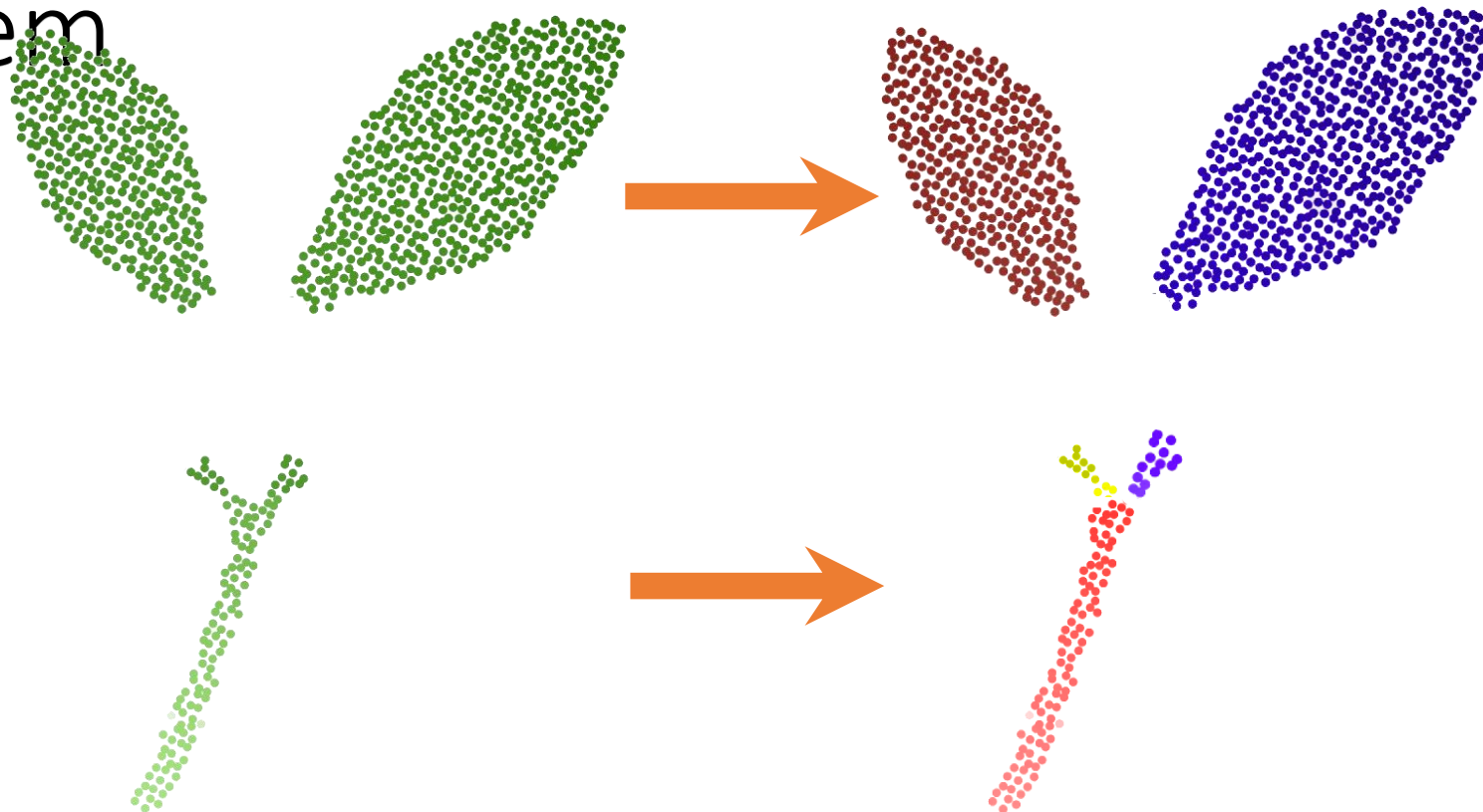




backward taking hints extractable only from future sequences

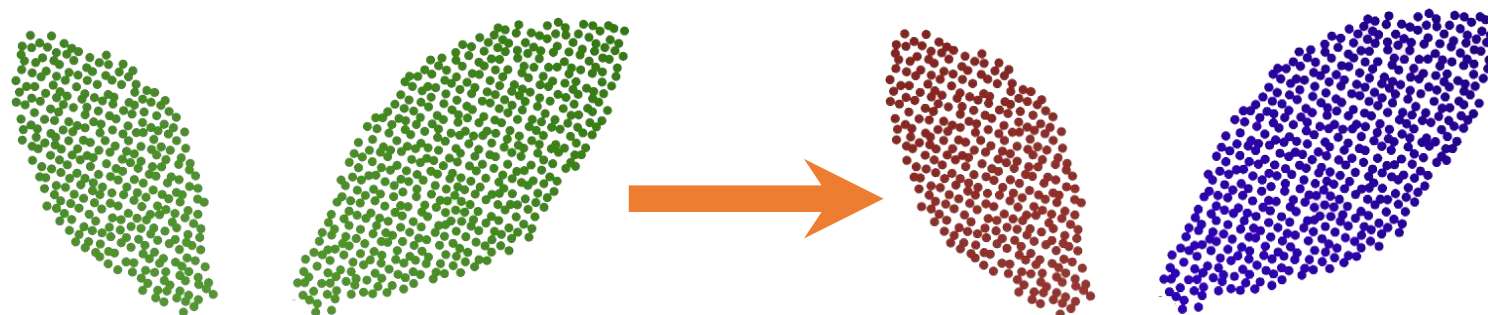


Individual organ segmentation: Multi-labelling problem

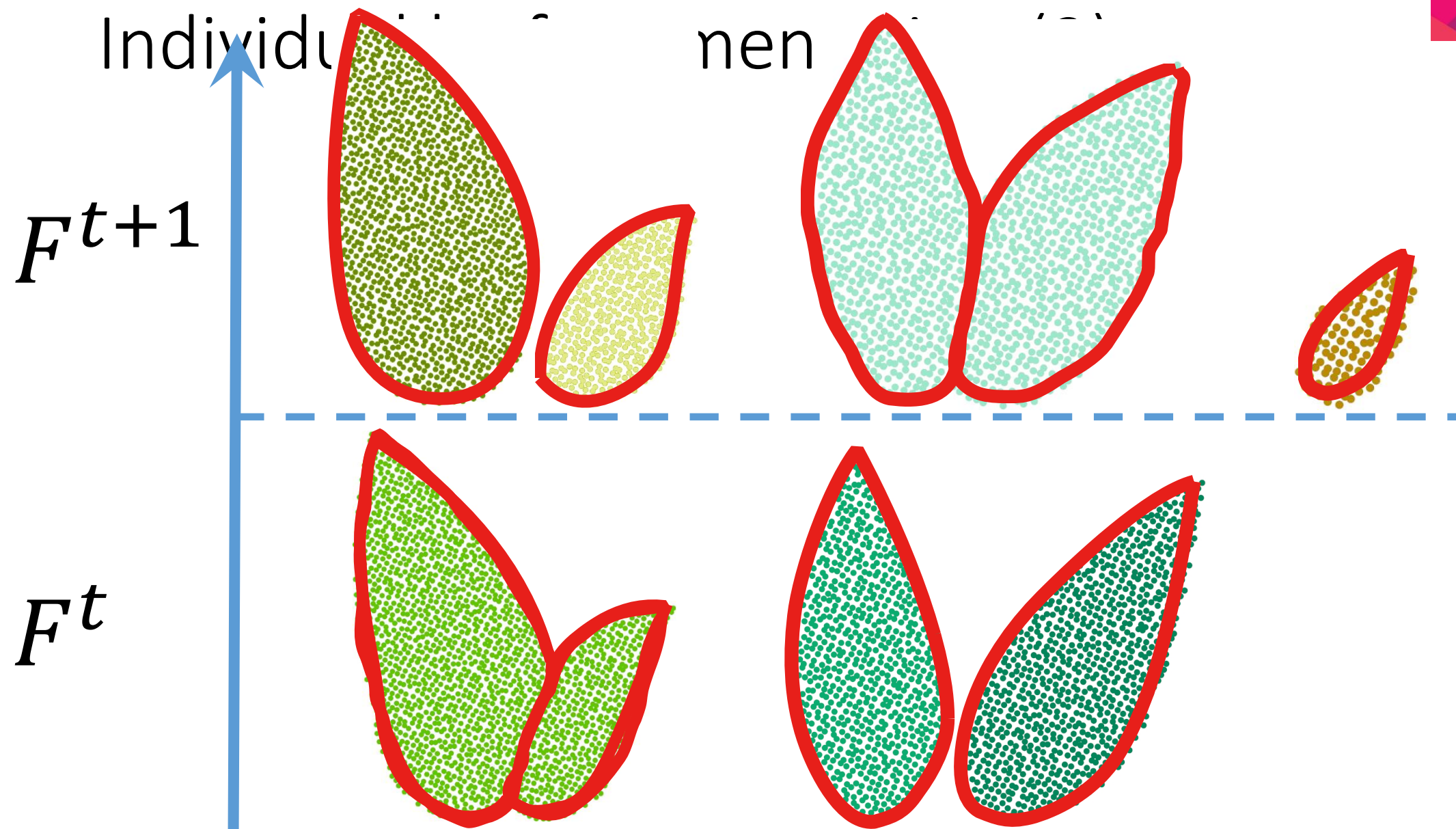


Label hypothesis generation + MRF optimization

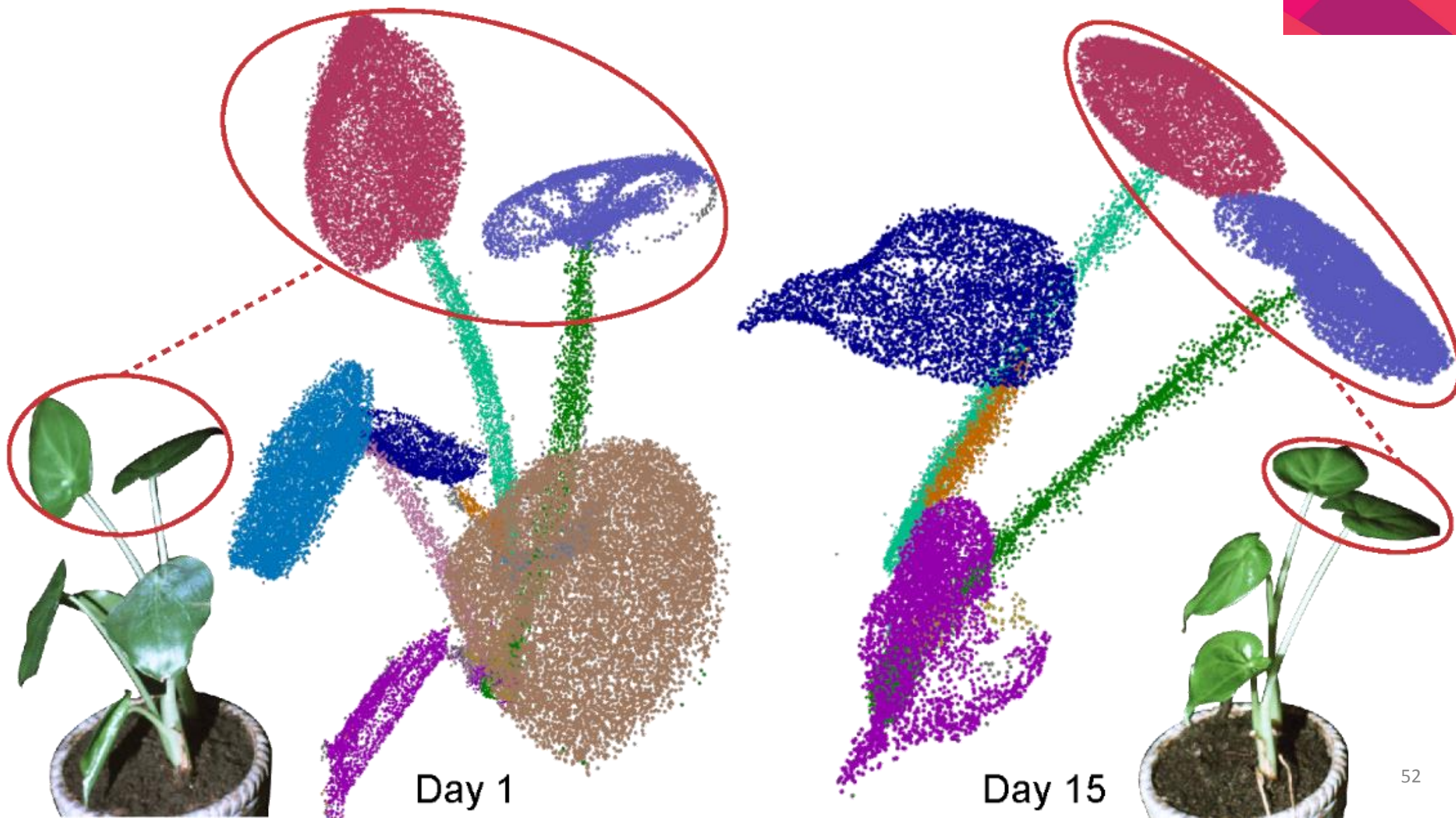
Individual leaf segmentation (1)

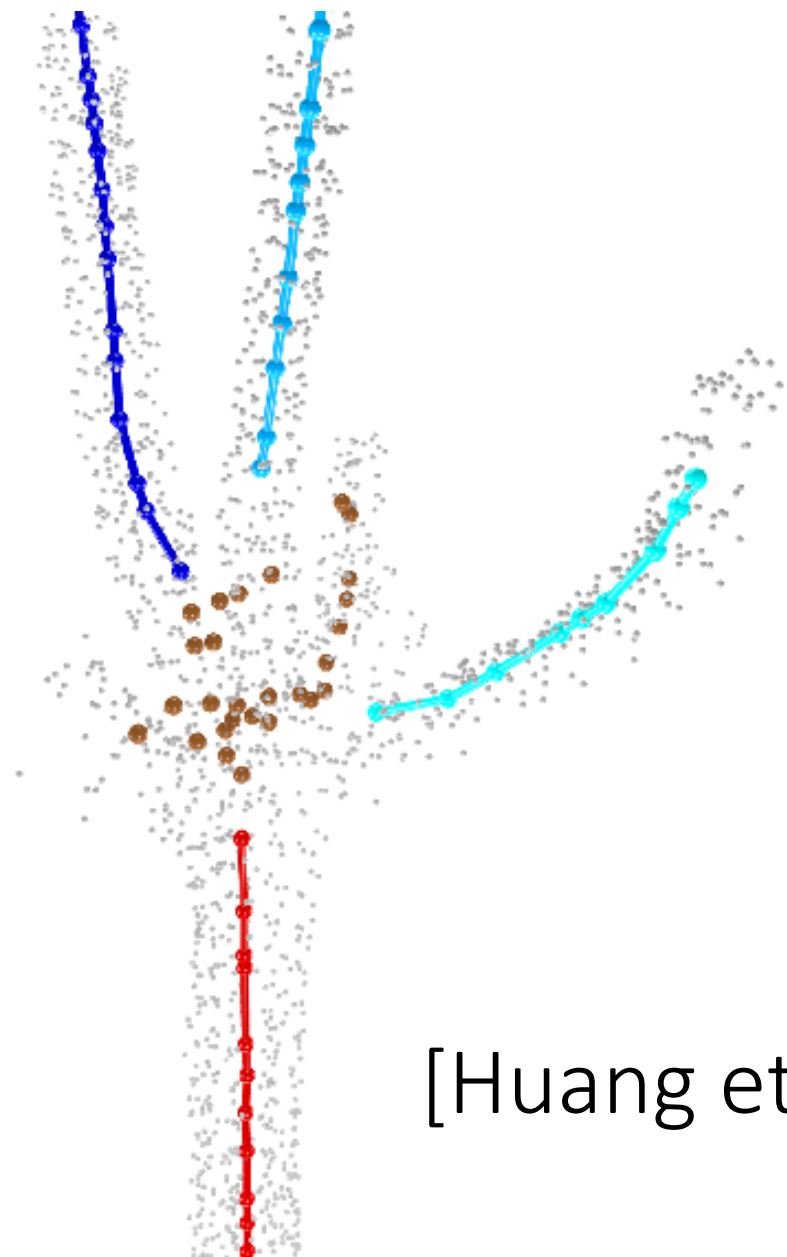
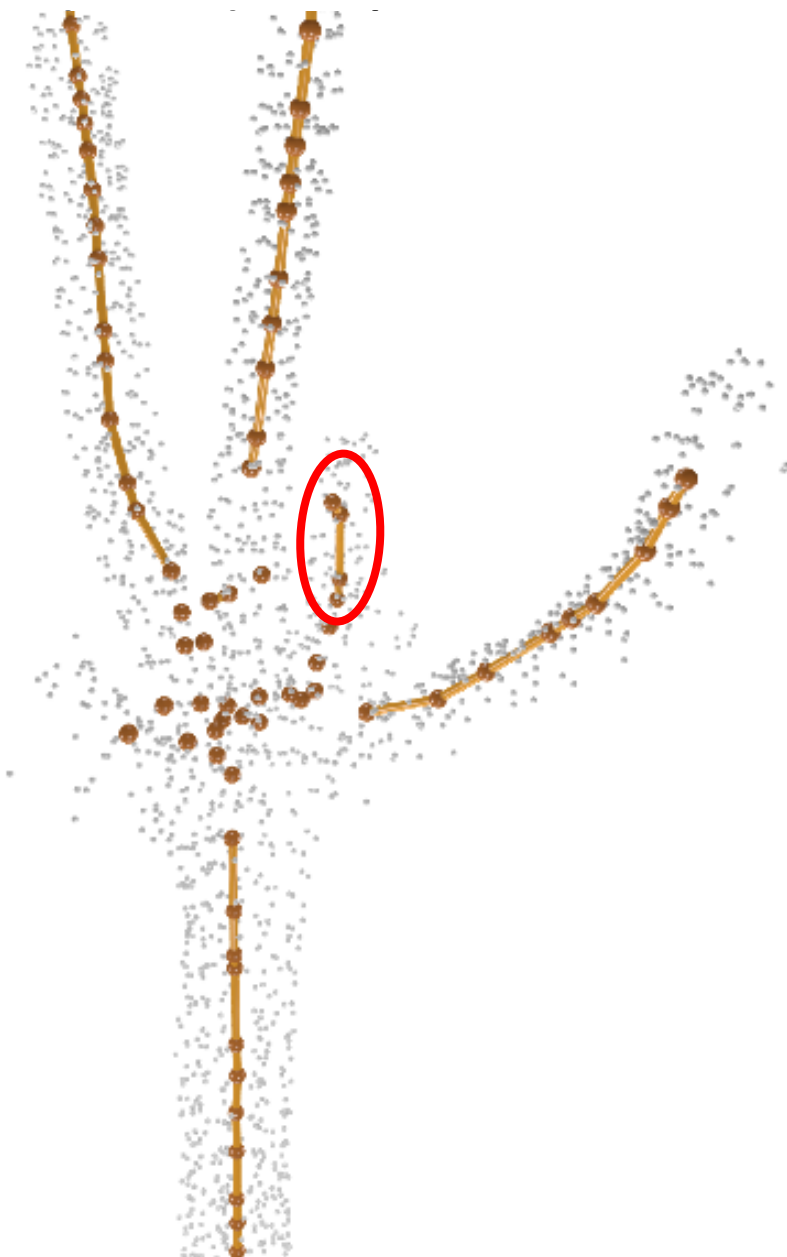


Individual leaf = one connected component
(true, if the leaves don't touch each other)



Transfer leaf information over time





[Huang et al. 2013]

[Dishlia]



Day 1

[Segmentation for Simulation]

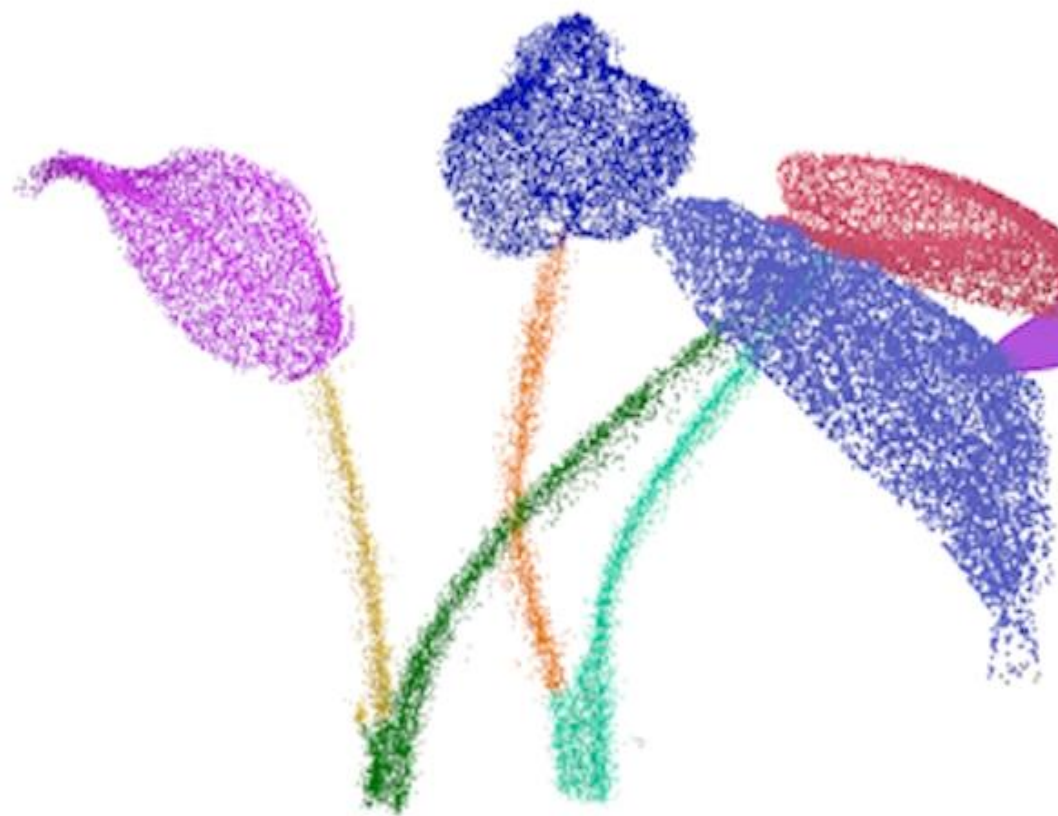
(using simulator from [Zhao and Barbič 2013])



[Organ Properties for Simulation]



[Synthesizing Live Plants]



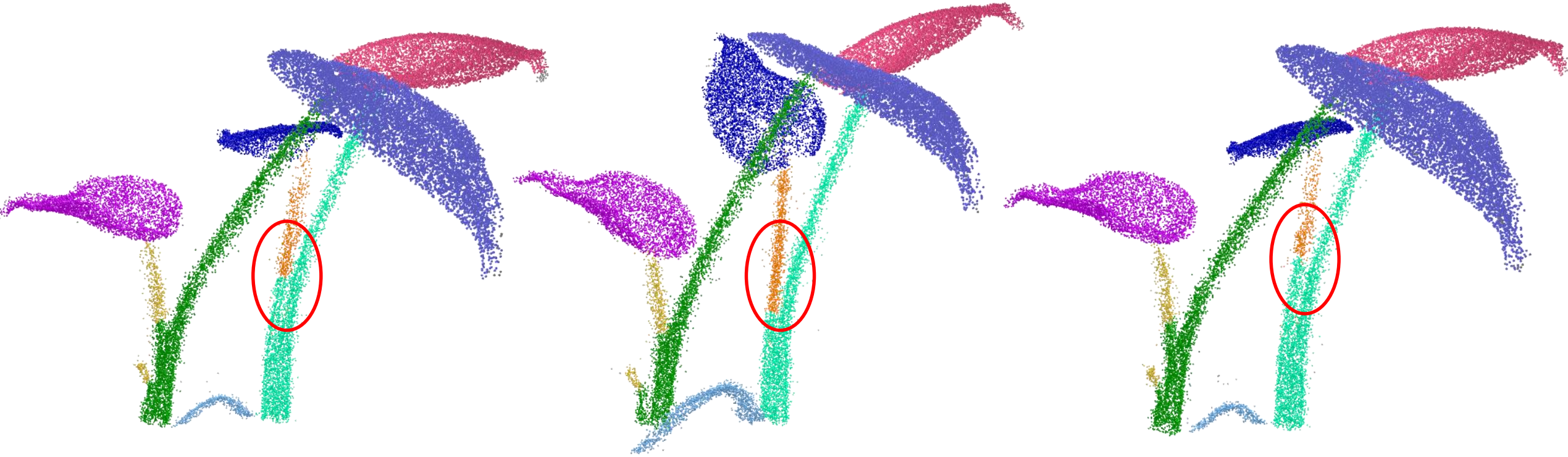
captured plant growth



synthesized plant growth



Future work: quantitative analysis



An important constraint is missing here:
the volume of each organ should change gradually!



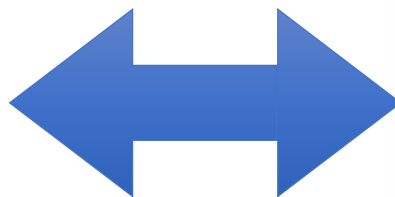
Inverse Procedural Modeling of Trees

- Stava, O., Pirk, S., Kratt, J., Chen, B., Měch, R., Deussen, O., & Benes, B. (2014). ***Inverse procedural modeling of trees***. In Computer Graphics Forum (Vol. 33, No. 6, pp. 118-131).

Procedural Modeling



?



```
Angle={COUNT} : set angle used by '+' and '-' below to 360/{COUNT}
Angle {COUNT} : set angle used by '+' and '-' below to 360/{COUNT}

Axiom={COMMANDS} : set starting set of commands to {COMMANDS}
Axiom {COMMANDS} : set starting set of commands to {COMMANDS}

{COUNT}+ : turn left {COUNT} times. if {COUNT} is omitted, use 1
{COUNT}- : turn right {COUNT} times. if {COUNT} is omitted, use 1

| : turn 180 degrees or the largest possible turn < 180 degrees

f : draw a line using the current direction/length
g : move forward instead of drawing

\{ANGLE} : turn left {ANGLE} degrees
/{ANGLE} : turn right {ANGLE} degrees

d : draw a line using the current direction/length
m : move forward instead of drawing

[ : save state (position, angle, size, etc.)
] : restore state

! : reverse the meaning of '+' and '-' and '\' and '/'

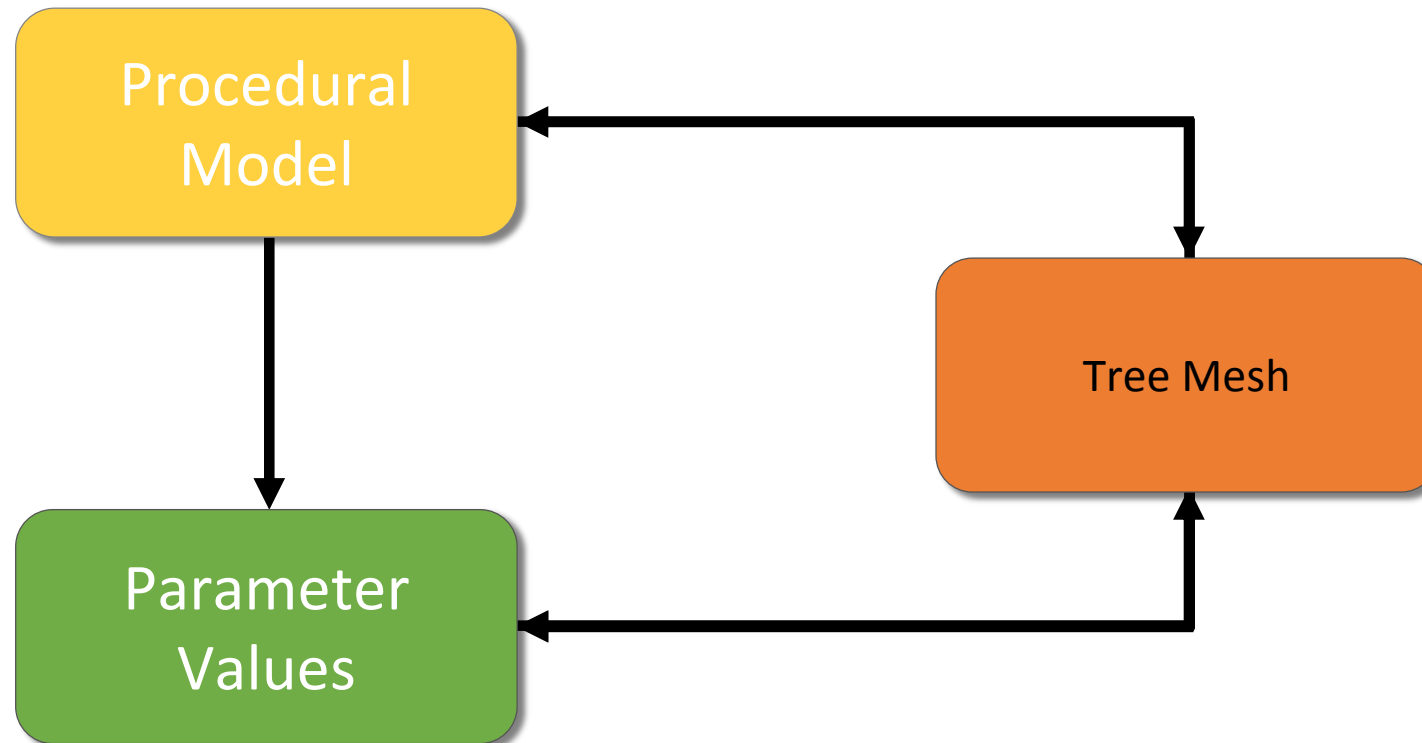
@{SCALE} : multiply the current line length by {SCALE}
@q{SCALE} : multiply the line length by the square root of {SCALE}
@I{SCALE} : multiply the line length by the reciprocal of {SCALE}

c{INDEX} : set color map index to {INDEX}

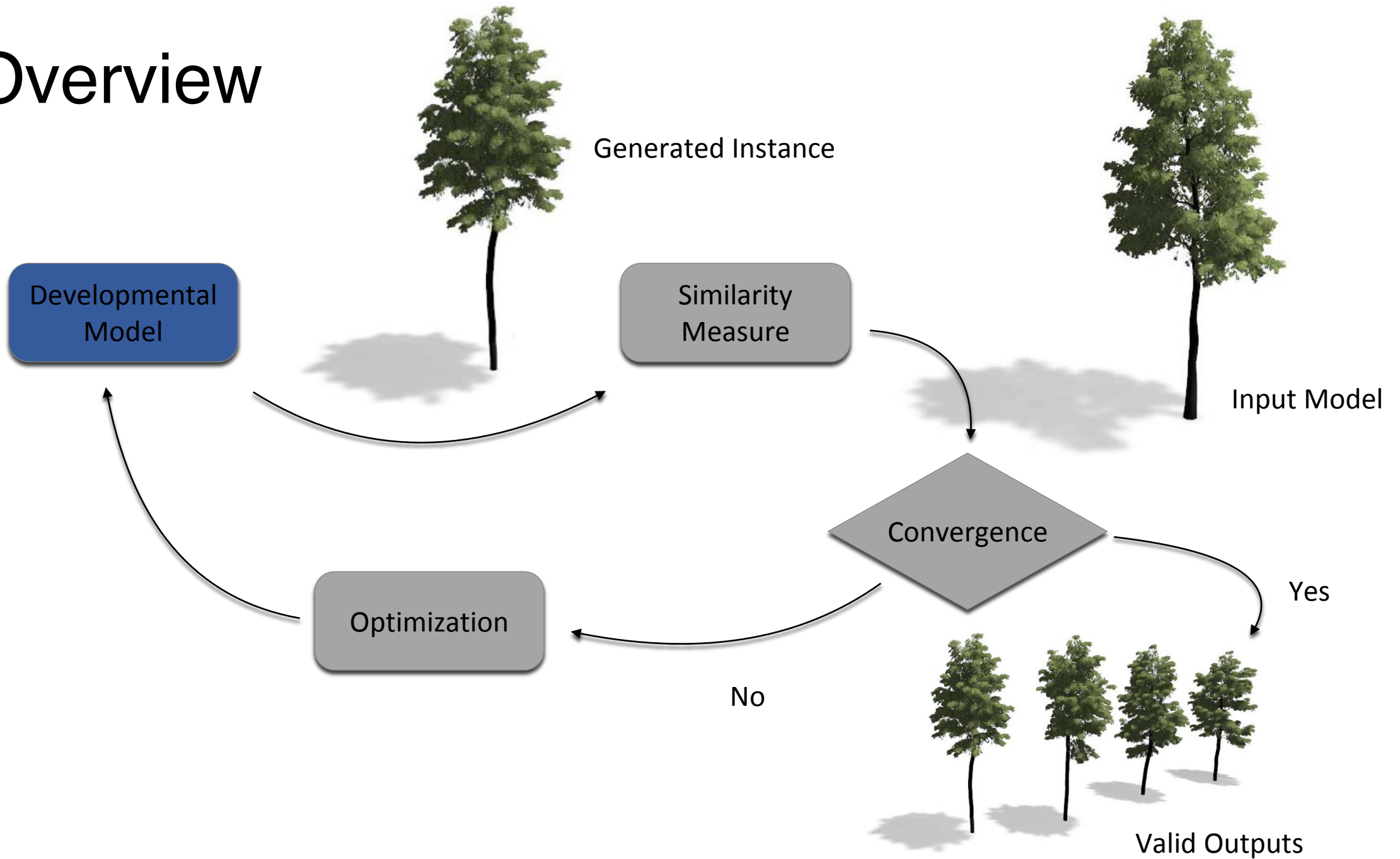
<{COUNT} : increment color map index by {COUNT}
>{COUNT} : decrement color map index by {COUNT}

{LETTER}={COMMANDS} : associate {COMMANDS} with character {LETTER}
```

Procedural Modeling

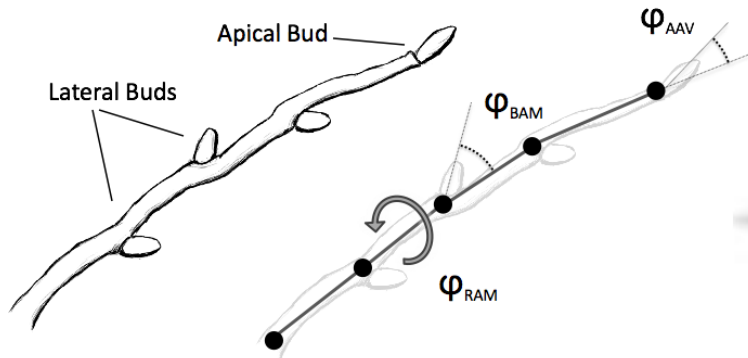


Overview



Developmental Model

- Captures new biological findings
[Cline et al. 2006, Cline et al. 2009]
- Geometric, environmental and bud fate parameters
- Patch-based foliage modeling
[Livny et al. 2011]



Developmental Model



Geometric Params

Growth Rate
Internode Length
Internode Angle Factor
Apical Control Level
Apical Dominance Factor

...

Environment Params

Gravitropism
Phototropism
Pruning Factor
Low Branch Pruning Factor
Gravity-bending Strength

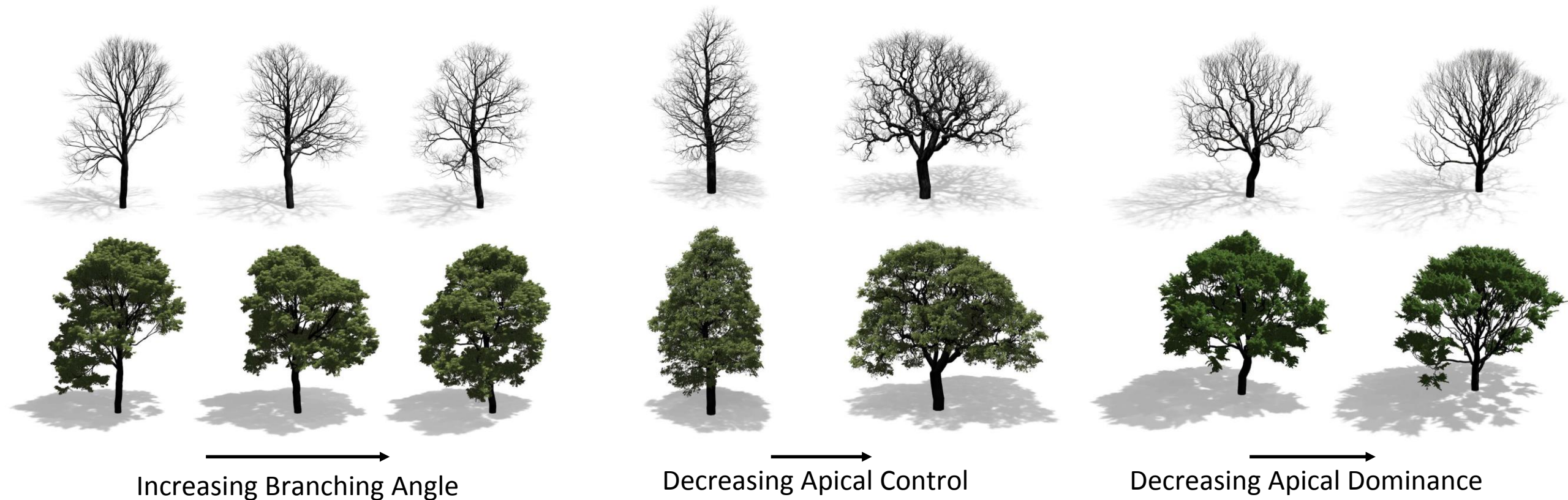
...

Bud Fate Params

Apical Angle Variance
Number of Lateral Buds
Branching Angle Mean and Variance
Roll Angle and Variance
Apical and Lateral Light Factor

...

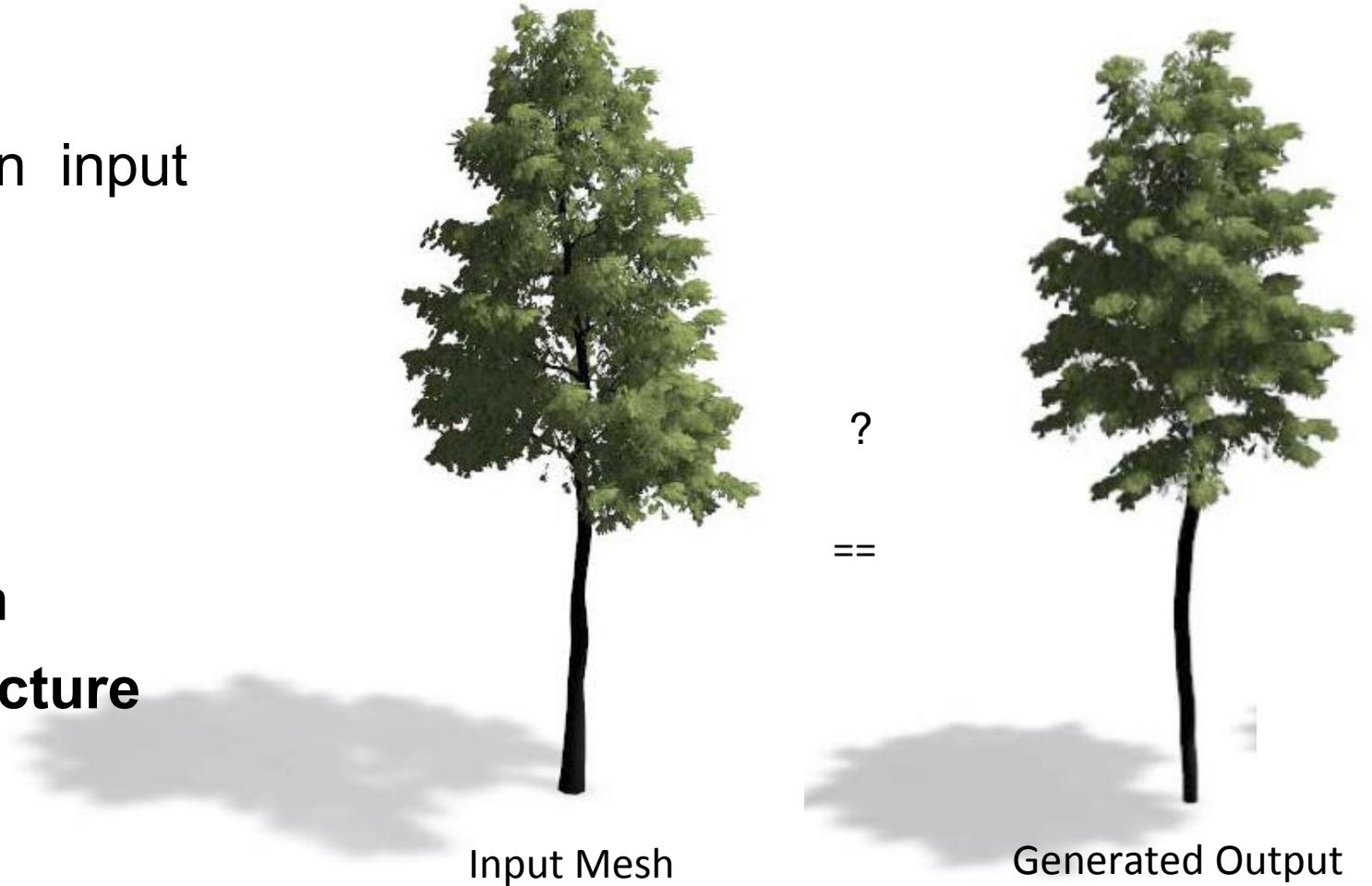
Developmental Model



Optimization

- Find parameters for developmental model
- Maximize similarity between input and generated instance
- What does similar mean?

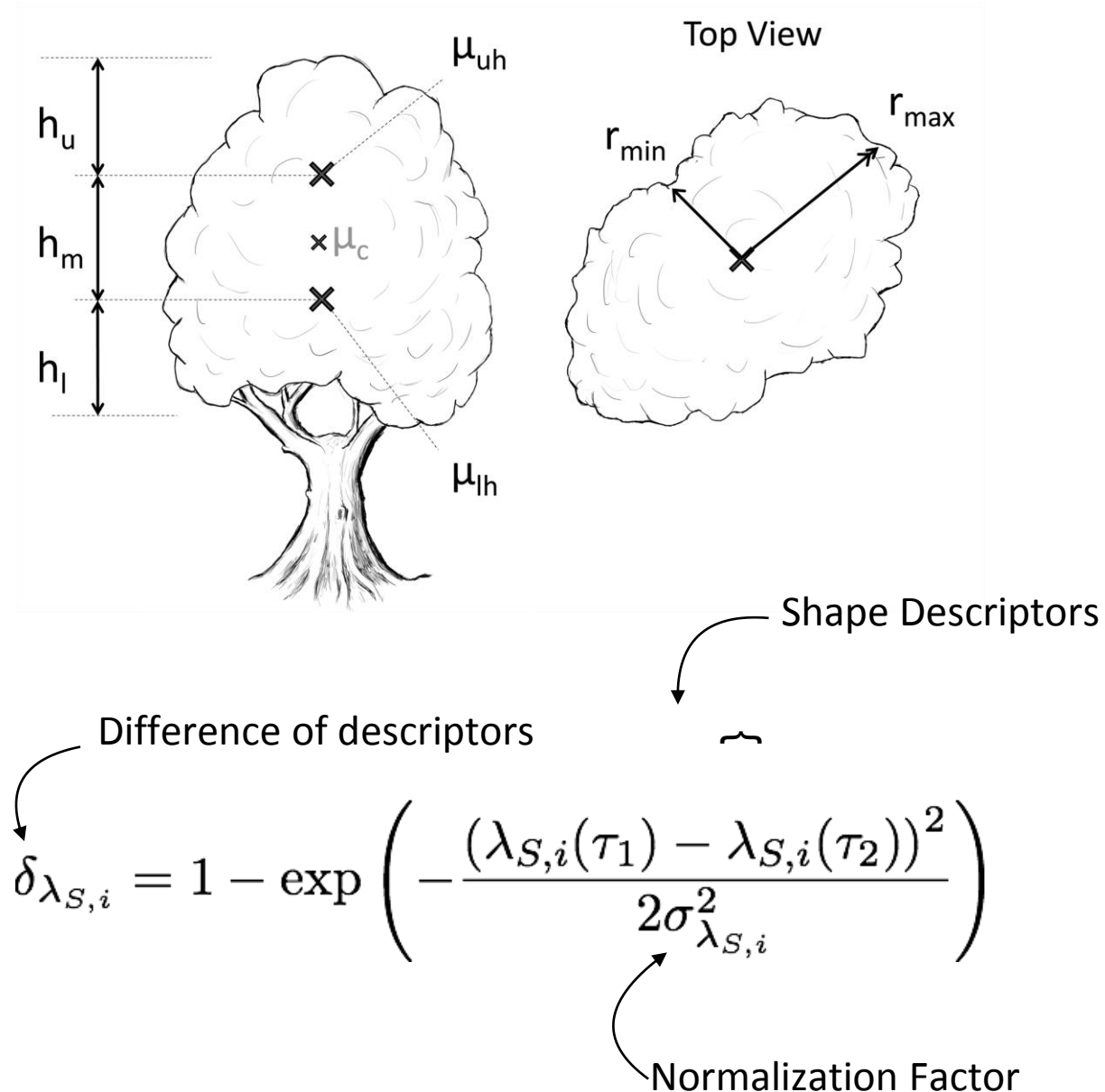
Fitness function based on geometry, shape and structure



Shape Distance

- Crown shape affected by distribution of branches
- Divide tree into slabs to capture variance
- Compute shape descriptors for each slab:

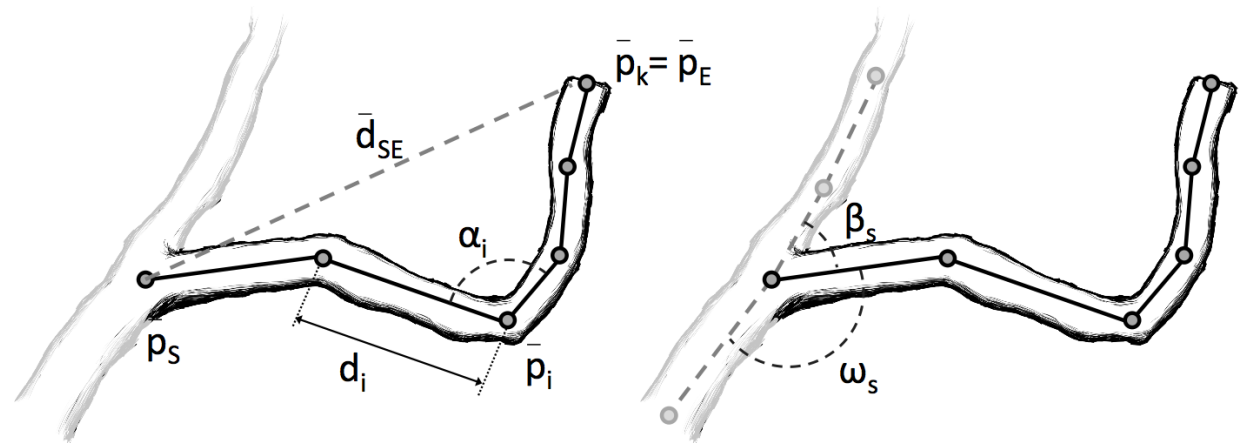
Height, radius, principal directions, leaf-branch density



Geometric Distance

- Statistics of branch geometry computed from the tree graph
- Sample weight based on length and thickness of a branch
- Descriptors are defined as mean and variance of these samples

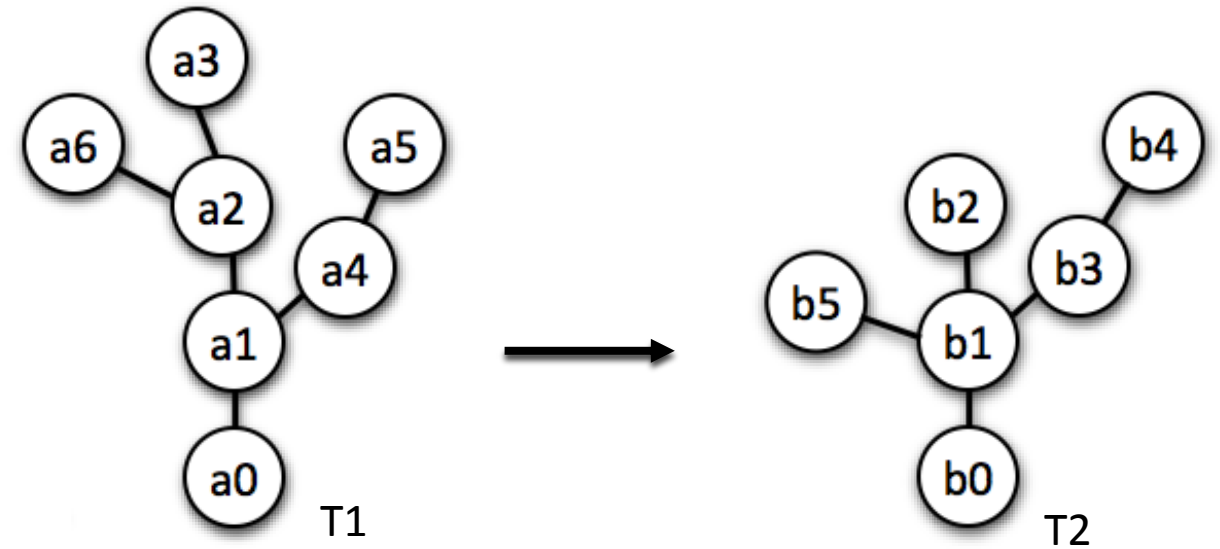
Name	Formula
Length	$\sum_{i=1}^k d_i$
Thickness	$\max_{\forall d_i} t_i$
Deformation	$\sum_{i=1}^{k-1} \alpha_i$
Straightness	$\frac{ d_{SE} }{b_L}$
Slope	$\angle \bar{d}_{SE}$
Sibling Angle	β_S
Parent Angle	ω_S



Structural Distance

[Zhang 1996, Ferraro and Godin 2000]

- Transform graph T1 into graph T2
- Costs for transforming the nodes (edit distance)
- Possible transformations: **assign, insert, delete**
- Quickly loses accuracy when geometric resolution differs



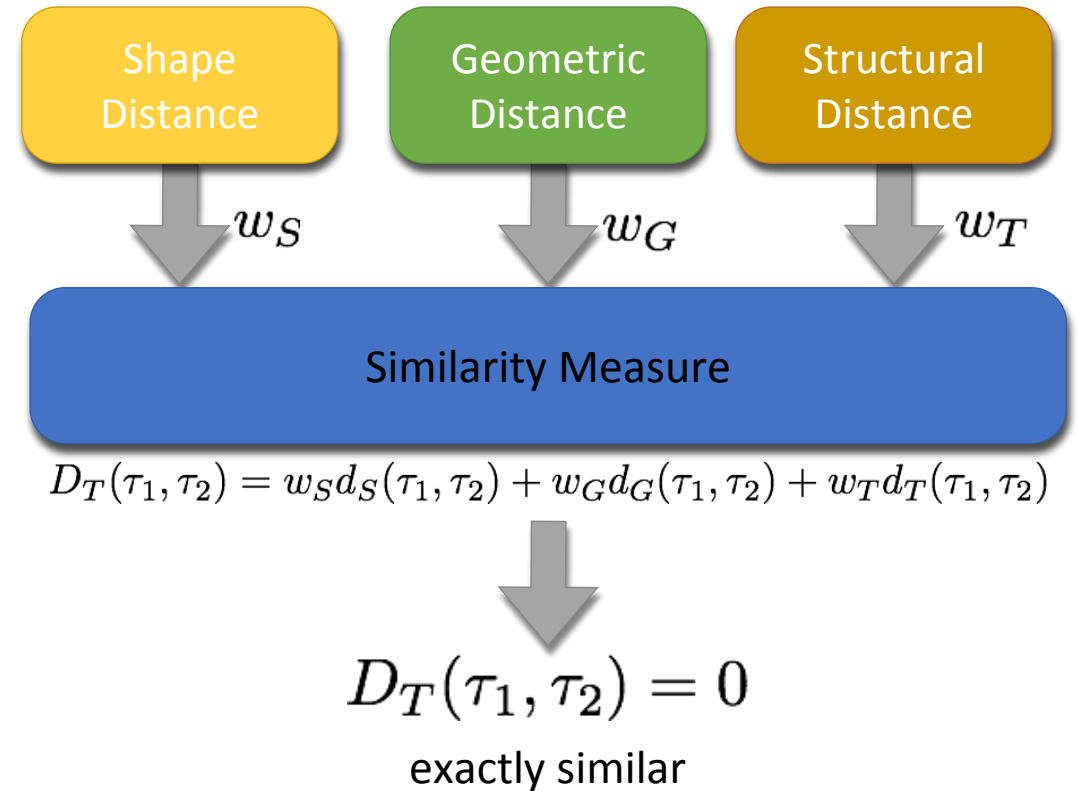
$$d_T(\tau_1, \tau_2) = \frac{d_N(t_1, t_2)}{2 \max(d_N(t_1, \epsilon), d_N(\epsilon, t_2))}$$

Labels and arrows in the diagram:

- Trees**: Points to τ_1 and τ_2 .
- Edit distance**: Points to $d_N(t_1, t_2)$.
- Structure-based distance**: Points to $d_T(\tau_1, \tau_2)$.
- Roots**: Points to ϵ .

Similarity Measure

- The sum of shape-, geometry and structure-based distances
- Corresponding weights for each distance (w_S , w_G , w_T)
- Results generated with equal weight

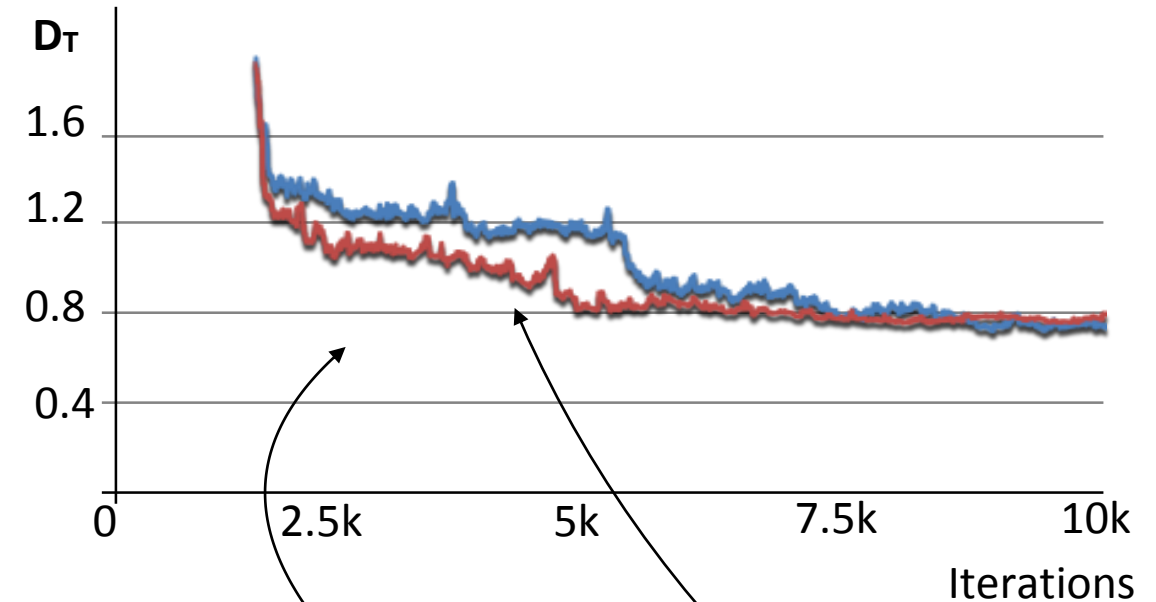


Optimization of Parameters

- Find parameter set that generates „similar enough“ tree models
- Simulated annealing
- Stochastic sampling based on Metropolis-Hastings
- Solve approximate optimization problem:

$$\operatorname{argmin}_{\bar{\varphi}_{\mathcal{M},t}} \left(\sum_{\omega_j} D_T(\tau^r, \tau^{\mathcal{M}}(\omega_j)) \right)$$

[Metropolis et al. 1953]



Performance

LiDAR

t[min]:
43
nodes:
359



Xfrog

t[min]: 270
nodes:
2307



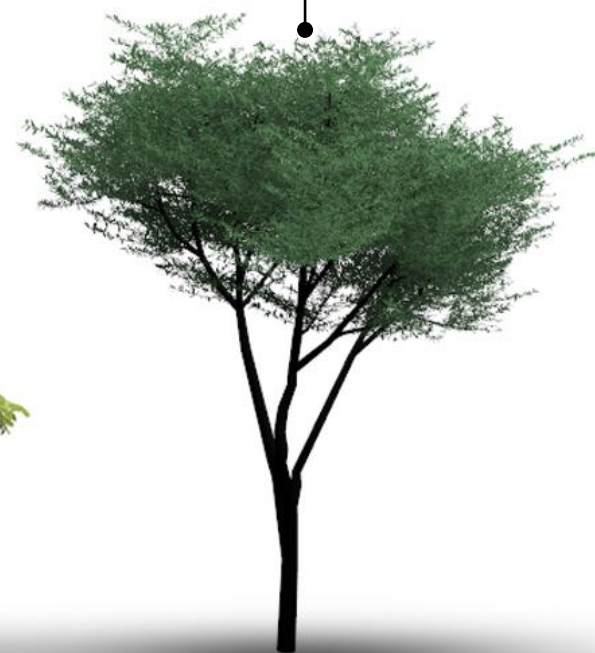
L-System

t[min]:
12
nodes:
464



LiDAR

t[min]:
85
nodes:
587



Results



Environment



Interpolation of Parameters



Different Species





Modeling Plant Life in Computer Graphics

User-assisted Modeling

Siggraph 2016 Course

Sören Pirk, Bedrich Benes, Takashi Ijiri, Yangyan Li,
Oliver Deussen, Baoquan Chen, Radomír Měch

Overview

- User-Assisted Plant Modeling [10 minutes]
 - Interactive Flower Modeling (**Ijiri**)
 - Sketch-based Tree Modeling (**Ijiri**)



Introduction

Plants and Trees

- Free form curves and surfaces
- Highly repetitive structures

For modeling them

- Free form components
- Local structures
- Overall shapes

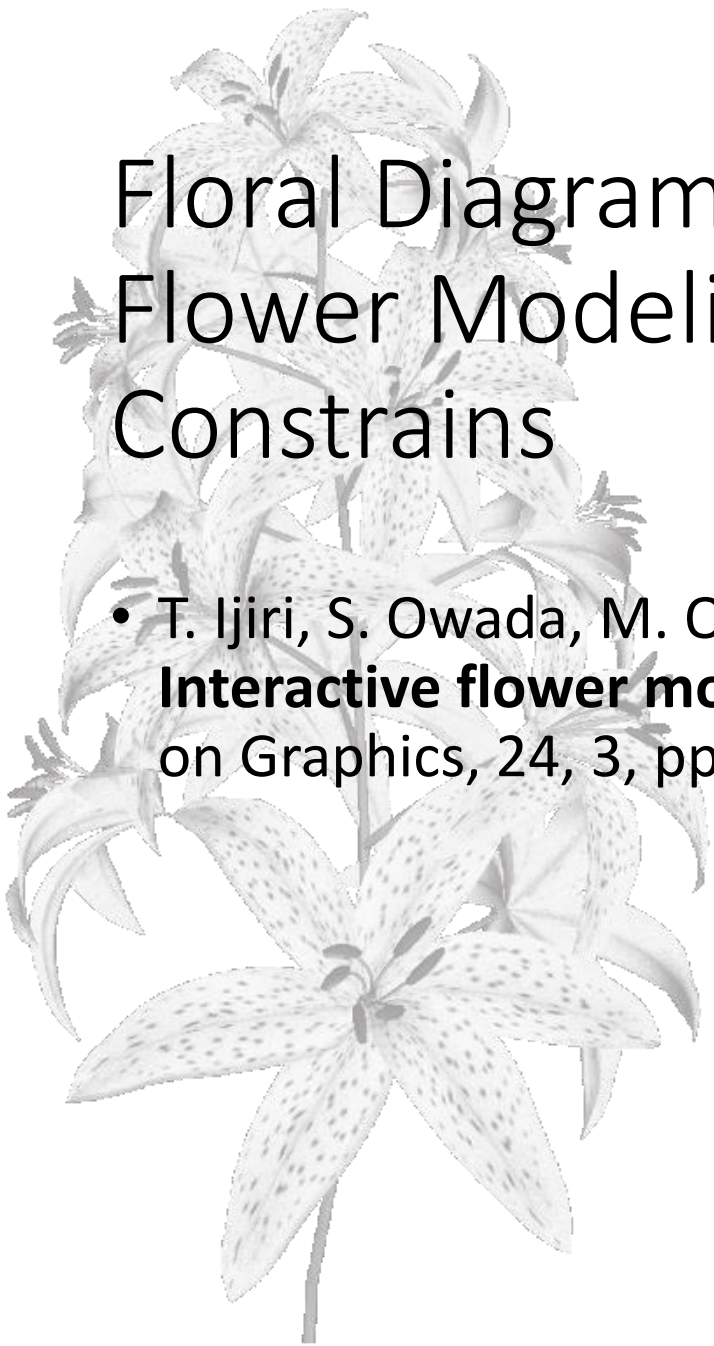
→ Sketch is well suited





Floral Diagrams and Inflorescences: Interactive Flower Modeling Using Botanical Structural Constrains

- T. Ijiri, S. Owada, M. Okabe, and T. Igarashi: **Floral diagrams and inflorescences: Interactive flower modeling using botanical structural constraints.** Transactions on Graphics, 24, 3, pp. 720-726, 2005.



Background

Flower Modeling is difficult



Many free form components

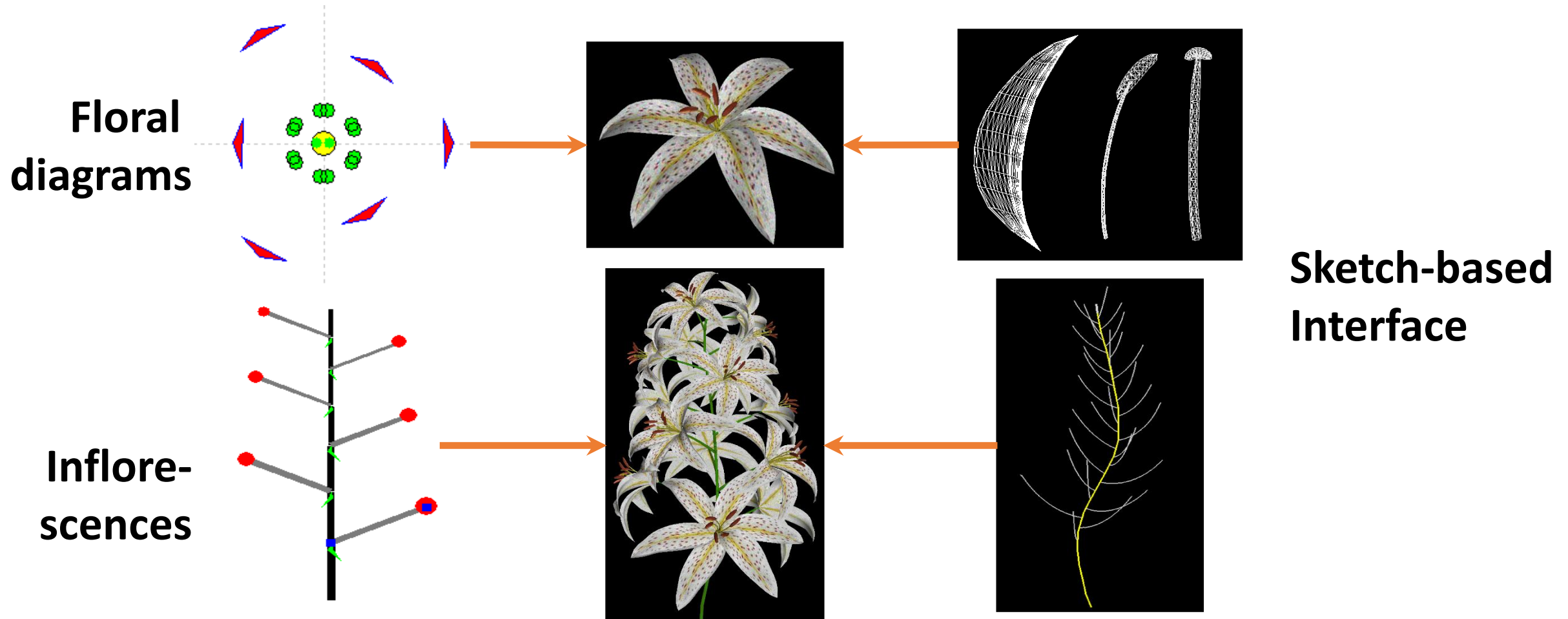


Structure specific to species

Goal : Easy-to-use interactive flower modeling framework

Key idea

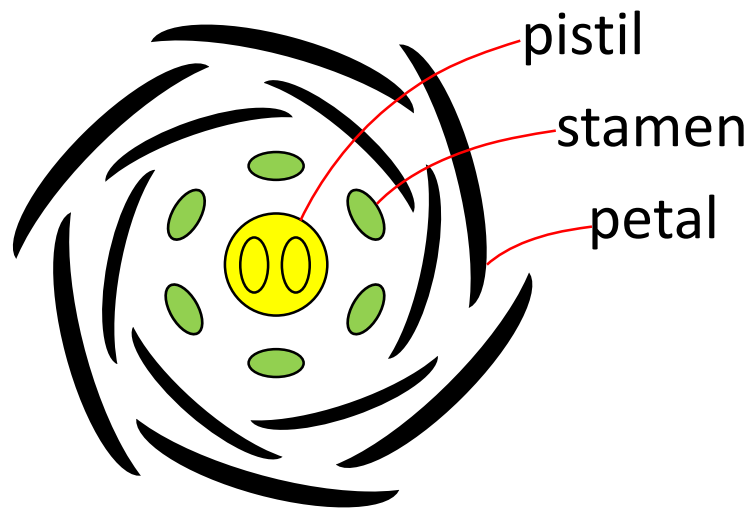
- Separate “structural specification” and “Geometry modeling”



Design editor by using botanical representation

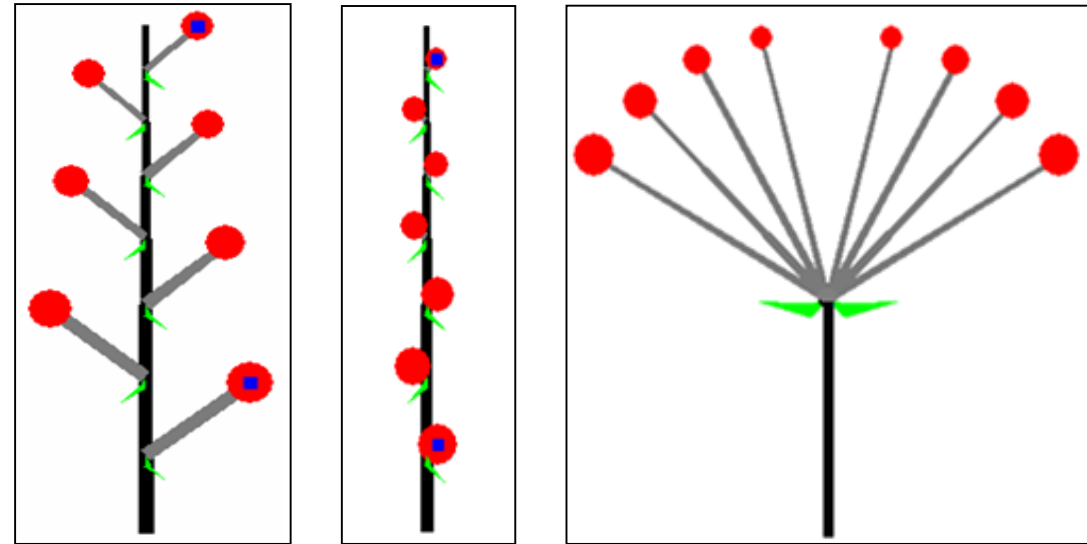
Floral Diagrams

Arrangement of flower components



Inflorescences

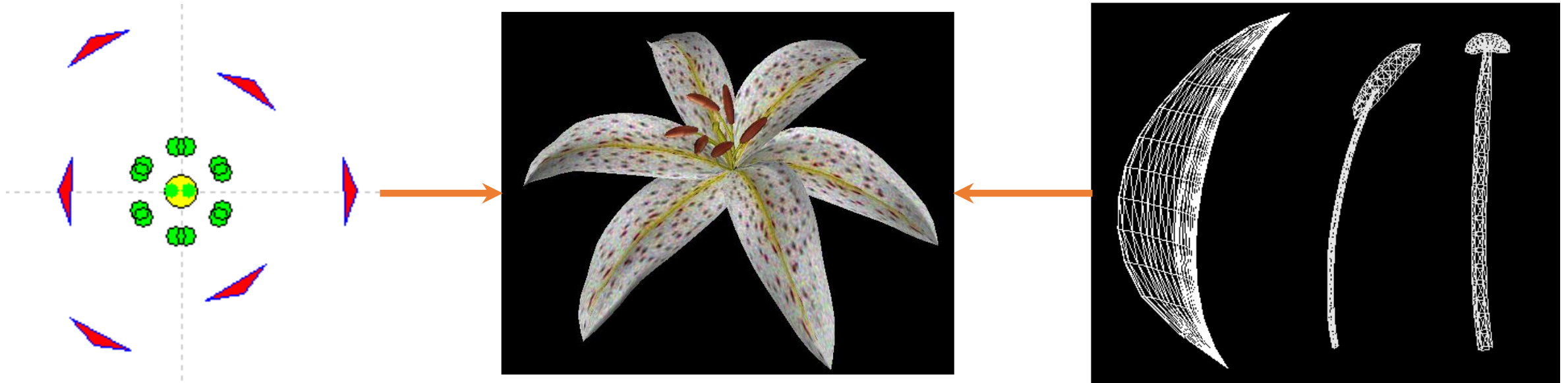
A branch bearing a lot of small flowers



[Bell. Plants form, *Timber press*, 1991]

→ Design structure editors based on them

Modeling process (Demo)





Summary

Easy to use flower modeling tool

Divide modeling process

- + structure editing

- + geometry modeling

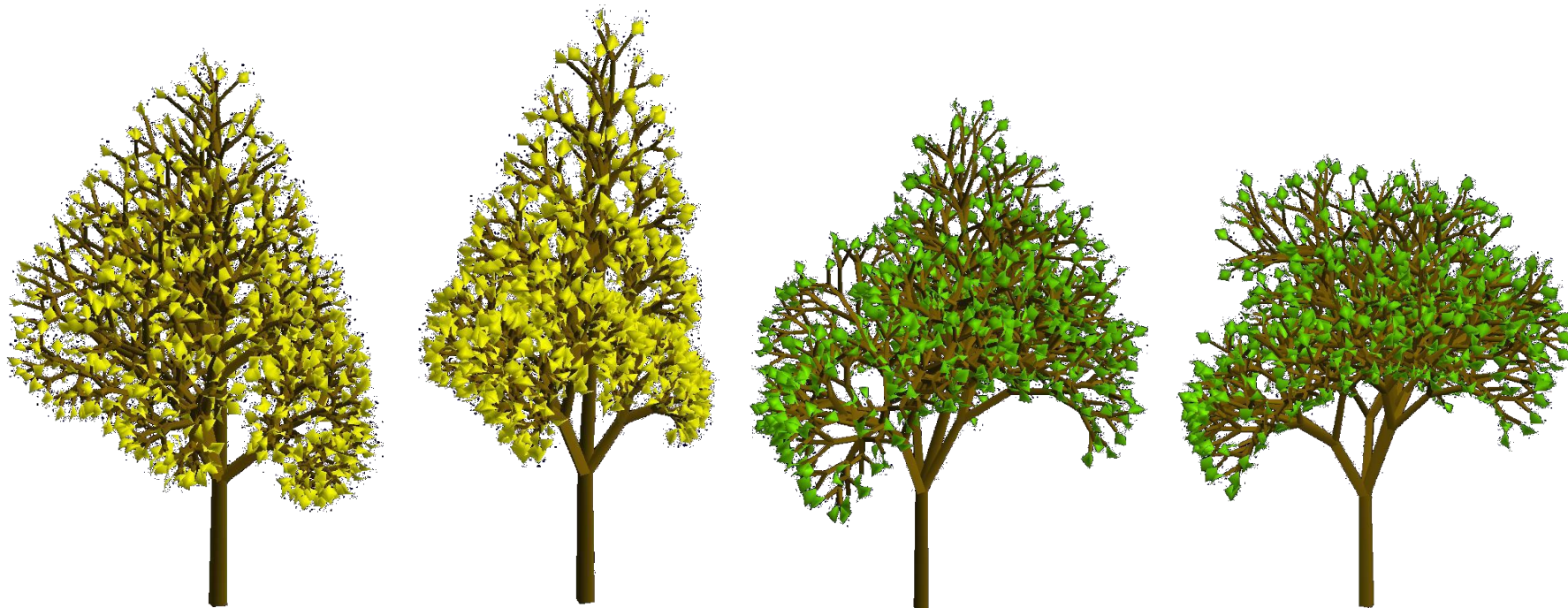


The Sketch L-System: Global Control of Tree Modeling using Free-form Strokes

- Ijiri T., Owada S., Igarashi T.: **The sketch L-system: Global control of tree modeling using free-form strokes.** In Smart Graphics 2006, Vol. Volume 4073 of *Lecture Notes in Computer Science*, Springer, pp. pp.138-146.

Our Goal

- Easy-to-use tree modeling framework
- Large **variations** of trees with a little effort



Our idea

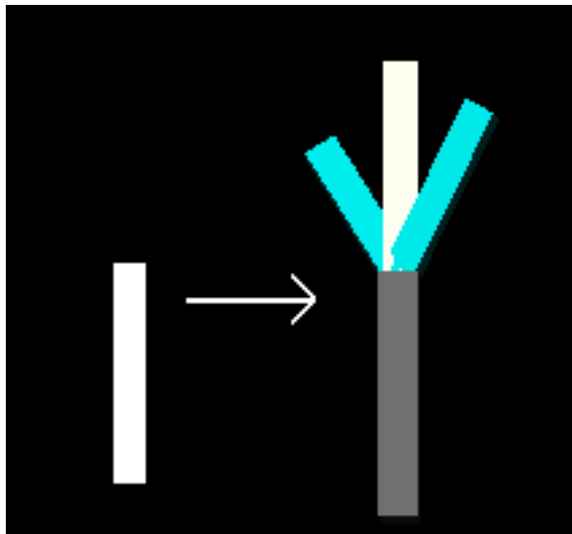
Combine two frameworks !!

- L-System → Describe complicated branching structures
- Sketch → Specify global appearance

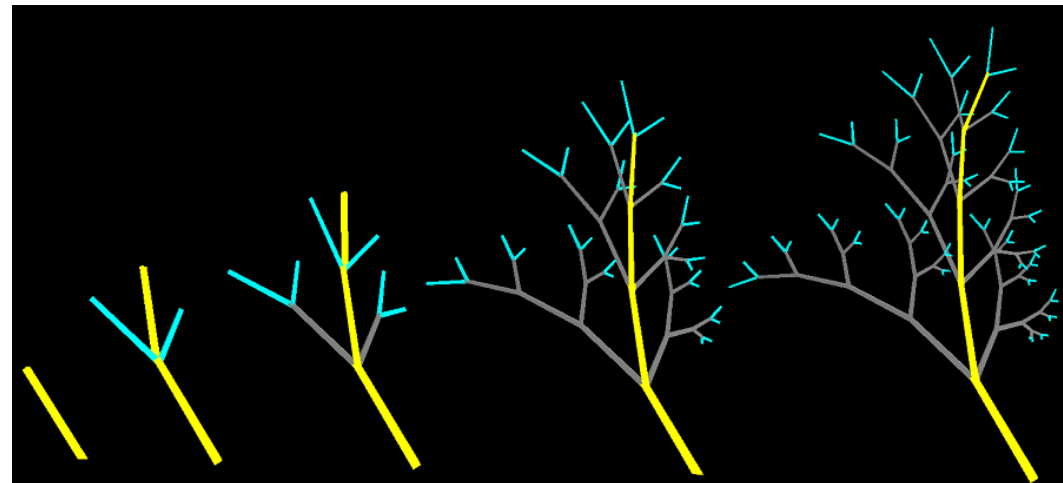
	L-System	Sketch
Detail structure	Good	Bad
Overall Shape	Bad	Good

Introduce two elements to L-System

- Interaction module
 - Its growing direction is decided by the stroke
- Sketch interface for controlling growth of L-System
 - Central axis & depth of recursion



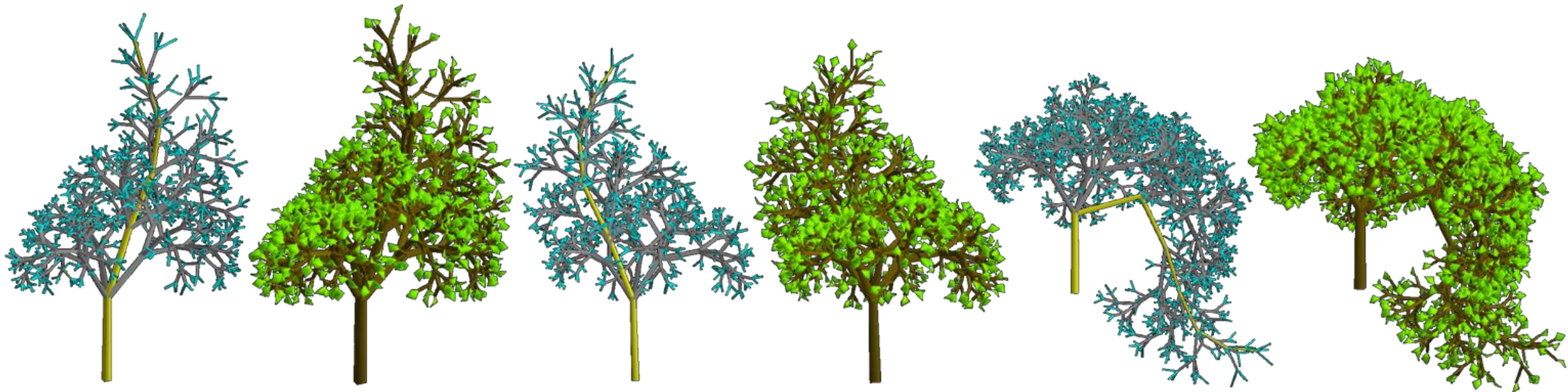
Interaction module



Sketch interface

Summary

- Combined sketch and L-system
- Large variation of trees with a little effort
- Only a simple trial and many future work
 - Specify overall shapes, Specify the shape of 2nd branches





Conclusion : user assisted modeling

- **Sketch based Interface** : global shapes
 - **Procedural approach** : local structures
- **Their combination becomes powerful tool for plant modeling**

Many sketch based plant modeling tools appear

Sketch-based tree modeling

[Longay et al. SBIM 2012]

[Wither et al. 2009]

[Chen et al. SIGGRAPH ASIA 2008]

[Okabe et al. EuroGraphics 2005]

Sketch-based plant modeling

[Anastacio et al. CG 2005]

Sketch-based Ornament modeling

[LU et al. SIGGRAPH 2014]

[MECH and MILLER, JCGT, 2012]

Additional references

Sketch based tree modeling

LONGAY, S., RUNIONS, A., BOUDON, F., AND PRUSINKIEWICZ, P. Treesketch: Interactive procedural modeling of trees on a tablet. In Proc. SBIM, 107–120, 2012

Jamie Wither, Frederic Boudon, Marie-Paule Cani, Christophe Godin. Structure from silhouettes: a new paradigm for fast sketch-based design of trees. Computer Graphics Forum, Wiley, 28 (2), pp.541-550, 2009

Xuejin Chen, Boris Nerburt, Ying-Qing Xu, Oliver Deussen, Sing Bing Kang. Sketch-Based Tree Modeling Using Markov Random Field. ACM Siggraph Asia and Transaction on Graphics, Vol. 27, No. 5, 2008

OKABE, M., OWADA, S., AND IGARASHI, T. Interactive design of botanical trees using freehand sketches and example based editing. Comput. Graph. Forum 24, 3, 487–496, 2005.

Sketch-based plant modeling

ANASTACIO, F., PRUSINKIEWICZ, P., AND SOUSA, M. Sketch-based parameterization of L-systems using illustration inspired construction lines and depth modulation. Comput. Graph. 33, 4, 440–451, 2009

Sketch-based Ornament modeling

LU, J., BARNES, C., WAN, C., ASENTE, P., MECH, R., AND FINKELSTEIN, A. Decobrush: Drawing structured decorative patterns by example. ACM Transactions on Graphics, 2014.

MECH, R., AND MILLER, G. The Deco framework for interactive procedural modeling. Journal of Computer Graphics Techniques (JCGT) 1, 1 (Dec), 43–99, 2012.

Modeling Plant Life in Computer Graphics

Conclusion

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What did we learn?

- **Introduction to vegetation modeling** in computer graphics.
- **Plant anatomy, plant growth, and environmental response** as a way to model plant geometry.
- Environmental response algorithms, such as **space colonization and self-organizing model**.





What did we learn?

- Algorithms for tree and flower **reconstruction from various data sources**, such as point sets, images, videos and CT.
- **Inverse Procedural Modeling** of Trees.
- **Sketch-based interface** for plant modeling.



Open problems

1. Modeling

Can we algorithmically describe a shape of a plant?

2. Controllability

How can an artist generate a plant with a desired shape?

3. Evaluation

How can we say the model is real?

4. Reconstruction

How can we get a model from a real-world sample?

Q&A

Course material available at:

<http://goo.gl/PaJjy4>