

Image/View Morphing and Warping

CS334

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- Given
 - left image
 - right image
- Create intermediate images
 - simulates camera movement

Related Work



- Panoramas (e.g., QuicktimeVR, etc)
 - user can look in any direction at few given locations but camera translations are *not* allowed...





- Image morphing (2D)
- View morphing (2D+)
- Image warping (3D)





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 Identify correspondences between input/output image

 Produce a sequence of images that allow a smooth transition from the input image to the output image



















1. Correspondences

2. Linear interpolation

$$P_k = (1 - \frac{k}{n})P_0 + \frac{k}{n}P_n$$













Image morphing is not shape preserving









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View Morphing









View Morphing



- Shape preserving morph
- Three step algorithm
 - Prewarp first and last images to parallel views
 - Image morph between prewarped images
 - Postwarp to interpolated view

Step 1: prewarp to parallel views

- Parallel views
 - same image plane
 - image plane parallel to segment connecting the two centers of projection
 - Prewarp
 - compute parallel views I_{0p} , I_{np}
 - rotate I₀ and I_n to parallel views
 - prewarp correspondence is
 (P₀, P_n) -> (P_{op}, P_{np})



Step 2: morph parallel images



- Shape preserving
- Use prewarped correspondences
- Interpolate C_k from C₀ C_n



Step 3: postwarp image





- Postwarp morphed image
 - create intermediate view
 - C_k is known
 - interpolate view direction and tilt
 - rotate morphed image to intermediate view



View morphing









View morphing



 View morphing is shape preserving

View Morphing Examples



• Using computer vision/stereo reconstruction techniques













Image Transformations





• Intuitively, how do you compute the matrix M by which to transform P_0 to P_{0p} ?





 A geometric relationship between input (u,v) and output pixels (x,y)

– Forward mapping: (x,y) = (X(u,v), Y(u,v))

- Inverse mapping: (u,v) = (U(x,y), V(x,y))



Image Transformations

General matrix form is

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

and operates in the "homogeneous coordinate system".



Affine Transformations

• Matrix form is

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

and accommodates translations, rotations, scale, and shear.

How many unknowns? How to create matrix?



Affine Transformations

 Transformation can be inferred from correspondences; e.g.,

$$\begin{bmatrix} u_i \\ v_i \\ w_i \end{bmatrix} \Leftrightarrow \begin{bmatrix} x_i \\ y_i \\ z_i \end{bmatrix}$$

• Given ≥3 correspondences can solve for T



• Matrix form is

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

- and it accommodates foreshortening of distant line and convergence of lines to a vanishing point;
- also, straight lines are maintained but not their mutual angular relationships, and
- only parallel lines parallel to the projection plane remain parallel



$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

- How many unknowns?
- How many correspondences are needed?



Direct Linear Transform

$$\begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ w \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

• Set w = 1 and z = 1, then have

$$\alpha \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & 1 \end{bmatrix} \begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

- Divide line 1 and 2 by 3
- Rearrange terms to form...

Example











Example











"Image Stitching"

• A colloquial term for the same thing...





See blackboard...

$$\begin{aligned} &\alpha(a_{11}u + a_{12}v + a_{13}) = x\\ &\alpha(a_{21}u + a_{22}v + a_{23}) = y\\ &\alpha(a_{31}u + a_{32}v + a_{33}) = 1 \end{aligned}$$

Divide 1st and 2nd line by 3rd line:

$$(a_{11}u + a_{12}v + a_{13}) = x(a_{31}u + a_{32}v + a_{33})$$

 $(a_{21}u + a_{22}v + a_{23}) = y(a_{31}u + a_{32}v + a_{33})$

Rearrange terms:

$$a_{11}u + a_{12}v + a_{13} - a_{31}xu - a_{32}yv - a_{33}x = 0$$

$$a_{21}u + a_{22}v + a_{23} - a_{31}xu - a_{32}yv - a_{33}y = 0$$



See blackboard...

 $a_{11}u + a_{12}v + a_{13} - a_{31}xu - a_{32}yv - a_{33}x = 0$ $a_{21}u + a_{22}v + a_{23} - a_{31}xu - a_{32}yv - a_{33}y = 0$

Assume
$$a_{33} = 1$$
,
 $a_{11}u + a_{12}v + a_{13} - a_{31}xu - a_{32}yv = x$
 $a_{21}u + a_{22}v + a_{23} - a_{31}xu - a_{32}yv = y$

Setup for 4+ points, yields 8 equations for 8 unknowns...

Perspective/Projective Transformation

• Solve Direct Linear Transform (DLT):

$$\begin{pmatrix} u_0 \ v_0 \ 1 \ 0 \ 0 \ 0 \ -u_0 x_0 - v_0 x_0 \\ u_1 \ v_1 \ 1 \ 0 \ 0 \ 0 \ -u_1 x_1 - v_1 x_1 \\ u_2 \ v_2 \ 1 \ 0 \ 0 \ 0 \ -u_2 x_2 - v_2 x_2 \\ u_3 \ v_3 \ 1 \ 0 \ 0 \ 0 \ -u_3 x_3 - v_3 x_3 \\ 0 \ 0 \ 0 \ u_0 \ v_0 \ 1 \ -u_0 y_0 - v_0 y_0 \\ 0 \ 0 \ 0 \ u_1 \ v_1 \ 1 \ -u_1 y_1 - v_1 y_1 \\ 0 \ 0 \ 0 \ u_2 \ v_2 \ 1 \ -u_2 y_2 - v_2 y_2 \\ 0 \ 0 \ 0 \ u_3 \ v_3 \ 1 \ -u_3 y_3 - v_3 y_3 \end{pmatrix} A = b$$
where *A* in unknow

where A is the vector of unknown coefficients a_{ii}





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- View morphing (2D+)
- Image warping (3D)

3D Image Warping



- Goal: "warp" the pixels of the image so that they appear in the correct place for a new viewpoint
- Advantage:
 - Don't need a geometric model of the object/environment
 - Can be done in time proportional to screen size and (mostly) independent of object/environment complexity
- Disadvantage:
 - Limited resolution
 - Excessive warping reveals several visual artifacts (see examples)





Some pictures courtesy of SIGGRAPH '99 course notes (Leonard McMillan)







McMillan & Bishop Warping Equation: $X_2 = \delta(X_1) P_2^{-1} (C_1 - C_2) + P_2^{-1} P_1 X_1$

Move pixels based on distance to eye ~Texture mapping

 Per-pixel distance values are used to warp pixels to their correct location for the current eye position



 Images enhanced with per-pixel depth [McMillan95]





 $P = C_1 + (c_1 + u_1 \overline{a_1} + v_1 \overline{b_1})w_1$ $P = C_2 + (c_2 + u_2 \overline{a_2} + v_2 \overline{b_2})w_2$





3D Image Warping Equations⁴

$$u_{2} = \frac{w_{11} + w_{12} \cdot u_{1} + w_{13} \cdot v_{1} + w_{14} \cdot \delta(u_{1}, v_{1})}{w_{31} + w_{32} \cdot u_{1} + w_{33} \cdot v_{1} + w_{34} \cdot \delta(u_{1}, v_{1})}$$
$$v_{2} = \frac{w_{21} + w_{22} \cdot u_{1} + w_{23} \cdot v_{1} + w_{24} \cdot \delta(u_{1}, v_{1})}{w_{31} + w_{32} \cdot u_{1} + w_{33} \cdot v_{1} + w_{34} \cdot \delta(u_{1}, v_{1})}$$











- DeltaSphere
 - Lars Nyland et al.









Disocclusions



• Disocclusions (or exposure events) occur when unsampled surfaces become visible...



What can we do?

Disocclusions



• Bilinear patches: fill in the areas



What else?



Rendering Order

/ The warping equation determines where points go...



... but that is not sufficient

Occlusion Compatible Rendering Order



- Epipolar geometry
- Project the new viewpoint onto the original image and divide the image into 1, 2 or 4 "sheets"







Occlusion Compatible Rendering Order



• A raster scan of each sheet produces a back-to-front ordering of warped pixels

Splatting



- One pixel in the source image does not necessarily project to one pixel in the destination image
 - e.g., if you are walking towards something, the sample might get larger...
- A solution: estimate shape and size of footprint of warped samples
 - expensive to do accurately
 - square/rectangular approximations can be done quickly (3x3 or 5x5 splats)
 - occlusion-compatible rendering will take care of oversized splats
 - BUT large splats can make the image seem blocky/low-res





• Lars Nyland et al.





courtesy 3rd Tech Inc.





300° x 300° panorama
this is the reflected light





300° x 300° panoramathis is the range light



spherical range panoramas





planar re-projection

Courtesy 3rd Tech Inc.





Courtesy 3rd Tech Inc.





Complete Jeep model



Courtesy 3rd Tech Inc.



