



Global Illumination

CS334

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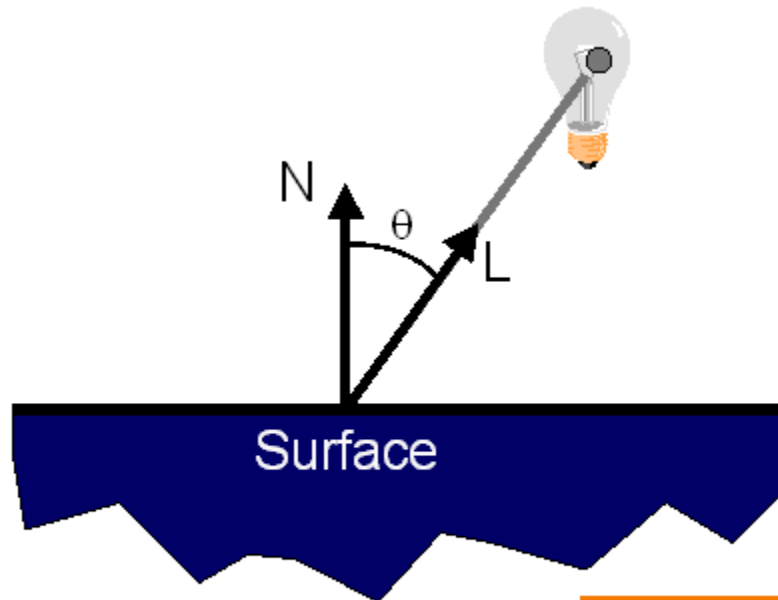
Recall: Lighting and Shading

- Light sources
 - Point light
 - Models an omnidirectional light source (e.g., a bulb)
 - Directional light
 - Models an omnidirectional light source at infinity
 - Spot light
 - Models a point light with direction
- Light model
 - Ambient light
 - Diffuse reflection
 - Specular reflection



Recall: Lighting and Shading

- Diffuse reflection
 - Lambertian model

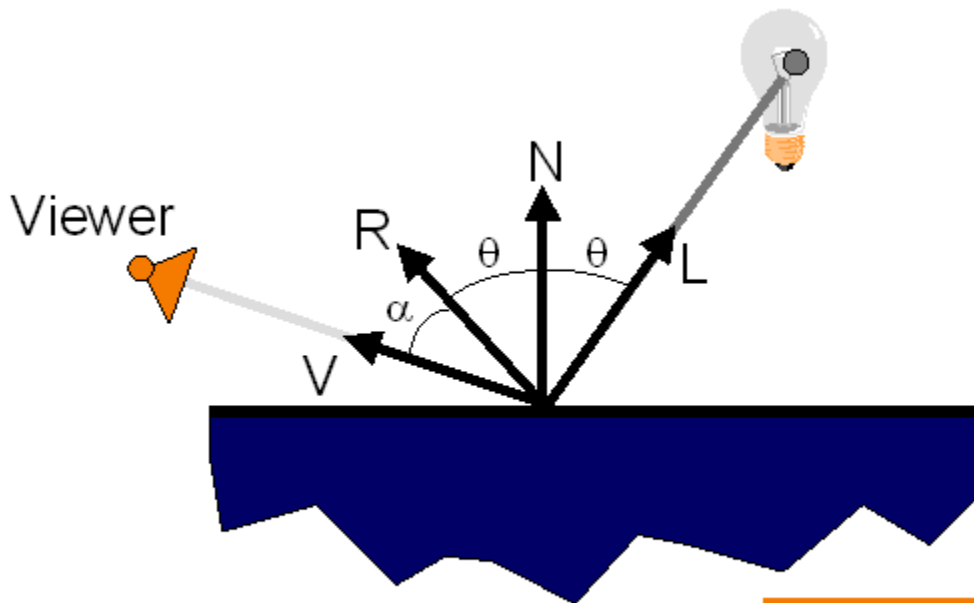


$$I_D = K_D(N \cdot L)I_L$$



Recall: Lighting and Shading

- Specular reflection
 - Phong model



$$I_S = K_S (V \cdot R)^n I_L$$

Recall: Lighting and Shading



- Well....there is much more





For example...

- Reflection -> Bidirectional Reflectance Distribution Functions (BRDF)
- Diffuse, Specular -> Diffuse Interreflection, Specular Interreflection
- Color bleeding
- Transparency, Refraction
- Scattering
 - Subsurface scattering
 - Through participating media
- And more!



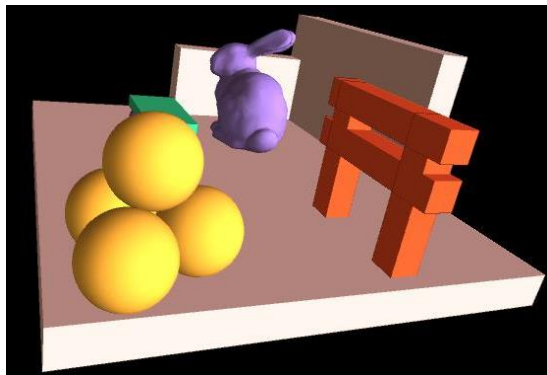
Illumination Models

- So far, you considered mostly local (direct) illumination
 - Light directly from light sources to surface
 - No shadows (actually is a global effect)
- Global (indirect) illumination: multiple bounces of light
 - Hard and soft shadows
 - Reflections/refractions (you kinda saw already)
 - Diffuse and specular interreflections

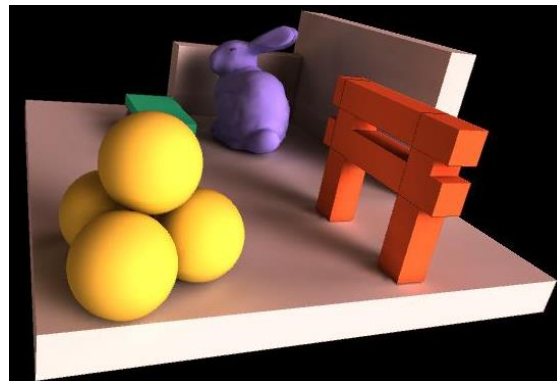
Welcome to Global Illumination



- *Direct illumination + indirect illumination; e.g.*
 - Direct = reflections, refractions, shadows, ...
 - Indirect = diffuse and specular inter-reflection, ...



direct illumination



with global illumination

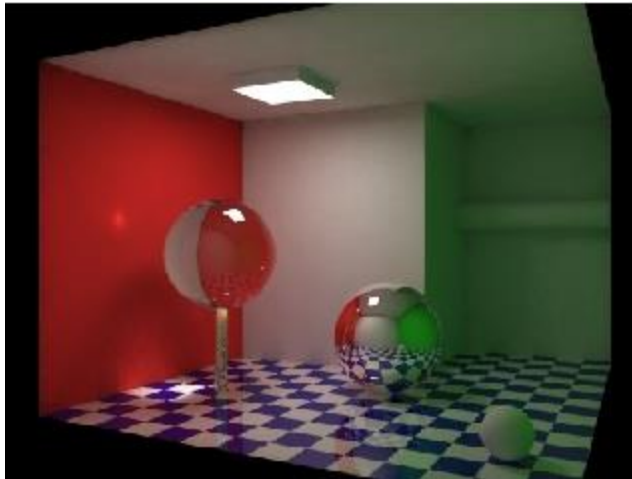


only diffuse inter-reflection



Global Illumination

- *Direct illumination + indirect illumination; e.g.*
 - Direct = reflections, refractions, shadows, ...
 - Indirect = diffuse and specular inter-reflection, ...



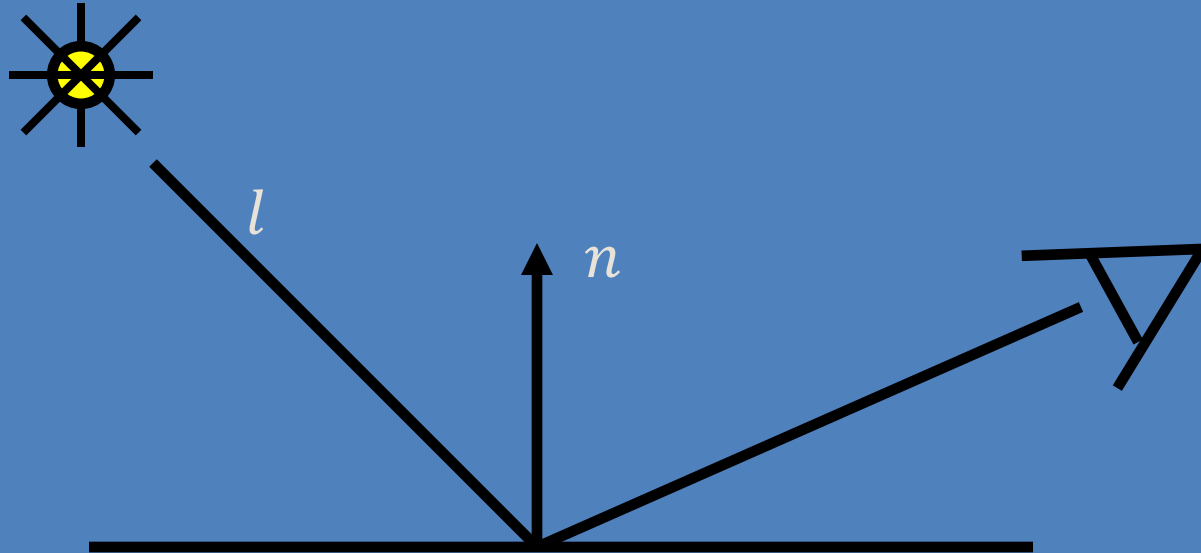
Reflectance Equation

- Lets start with the diffuse illumination equation and generalize...
- Define the all encompassing reflectance equation...
- Then specialize to the subset called the rendering equation...

Reflectance Equation

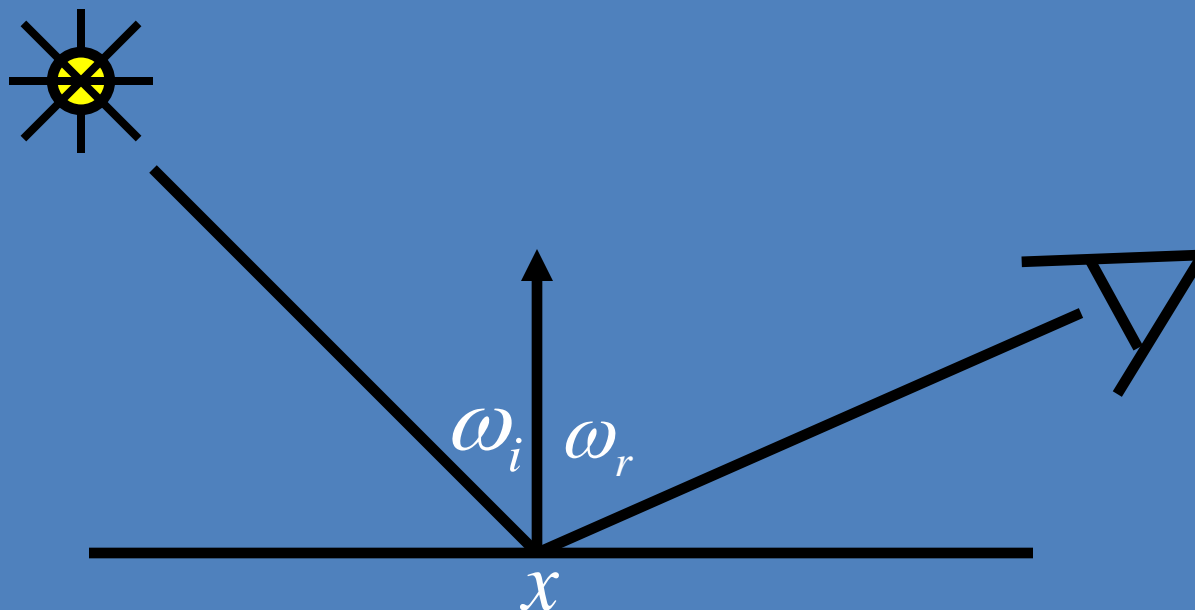
$$\text{diffuse_illumination} = 0 + I_L K_D l \cdot n$$

Reflectance Equation



$$\text{diffuse_illumination} = 0 + I_L K_D l \cdot n$$

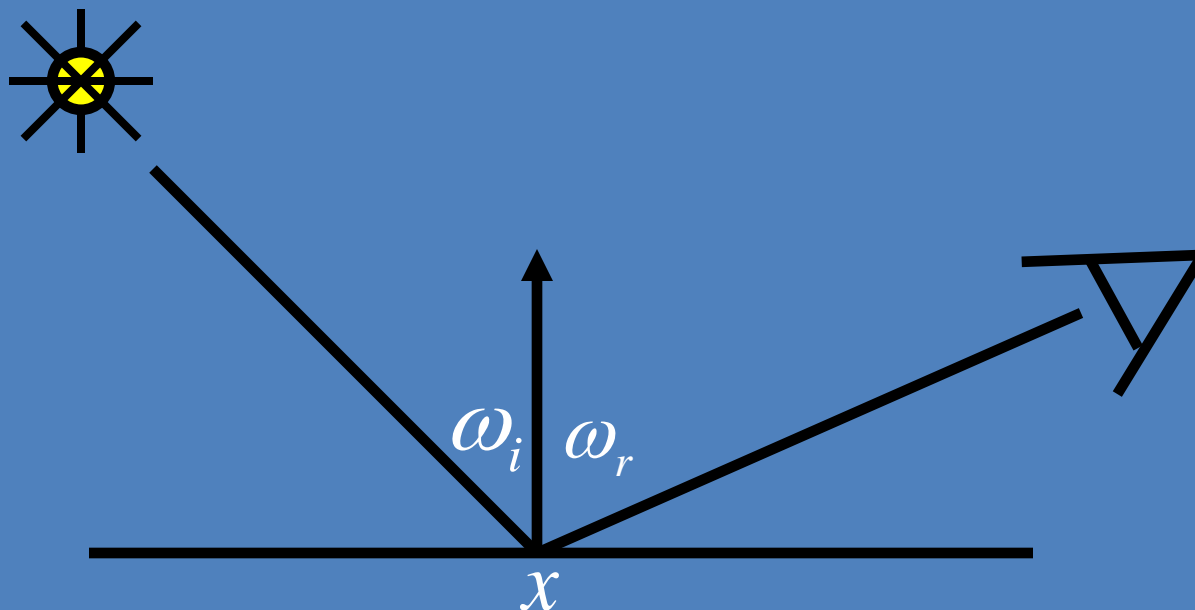
Reflectance Equation



$$L_r(x, \omega_r) = L_e(x, \omega_r) + L_i(x, \omega_i) f(x, \omega_i, \omega_r) (\omega_i \cdot n)$$

$$\text{diffuse_illumination} = 0 + I_L K_D l \cdot n$$

Reflectance Equation



$$L_r(x, \omega_r) = L_e(x, \omega_r) + L_i(x, \omega_i) f(x, \omega_i, \omega_r) (\omega_i \cdot n)$$

Reflected Light
(Output Image)

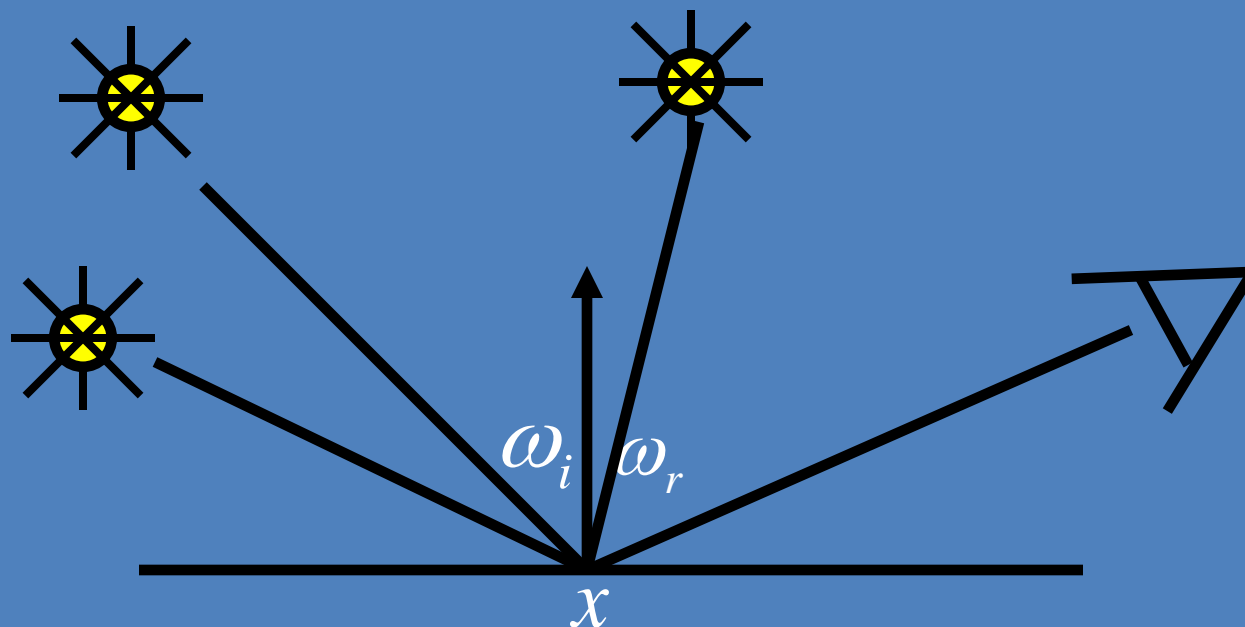
Emission

Incident
Light (from
light source)

BRDF

Cosine of
Incident angle

Reflectance Equation



Sum over all light sources

$$L_r(x, \omega_r) = L_e(x, \omega_r) + \sum L_i(x, \omega_i) f(x, \omega_i, \omega_r) (\omega_i \cdot n)$$

Reflected Light
(Output Image)

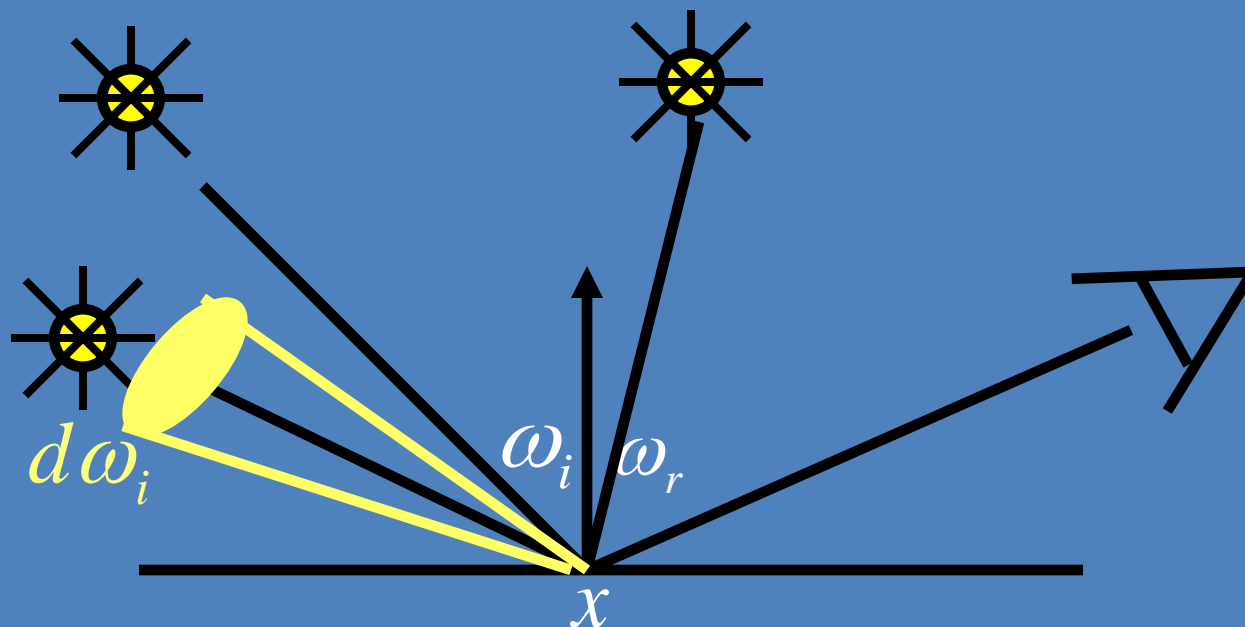
Emission

Incident
Light (from
light source)

BRDF

Cosine of
Incident angle

Reflectance Equation



Replace sum with integral

$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_i(x, \omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

Reflected Light
(Output Image)

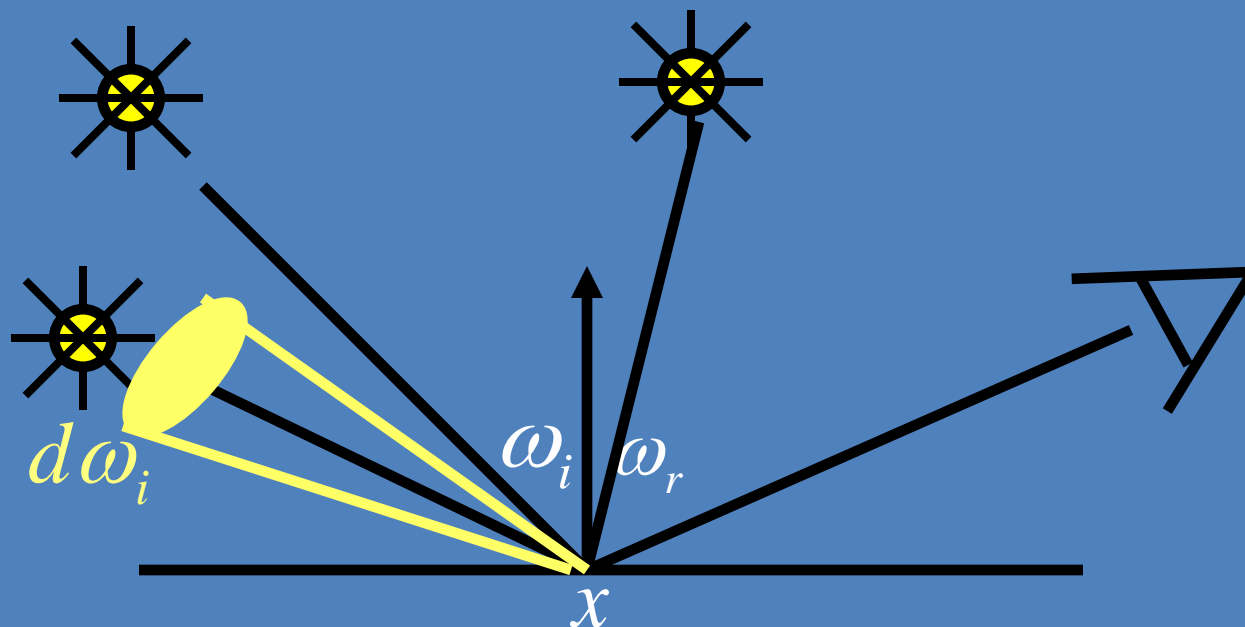
Emission

Incident
Light (from
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Cosine of
Incident angle

Reflectance Equation



$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_i(x, \omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

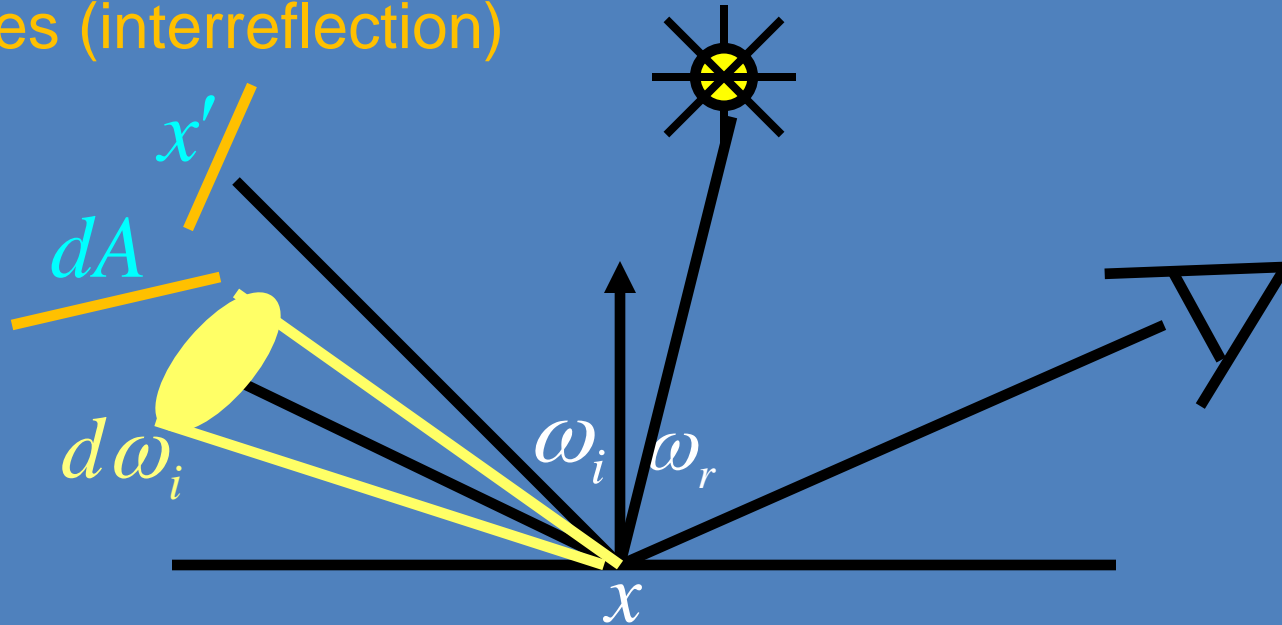
The Challenge

$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_i(x, \omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

- Computing reflectance equation requires knowing the incoming radiance from surfaces
- ...But determining incoming radiance requires knowing the reflected radiance from surfaces

Global Illumination

Surfaces (interreflection)



$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_r(x', -\omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

Reflected Light
(Output Image)

Emission

Reflected
Light (from
prev surface)

BRDF

Cosine of
Incident angle



Rendering Equation (Kajiya 1986)

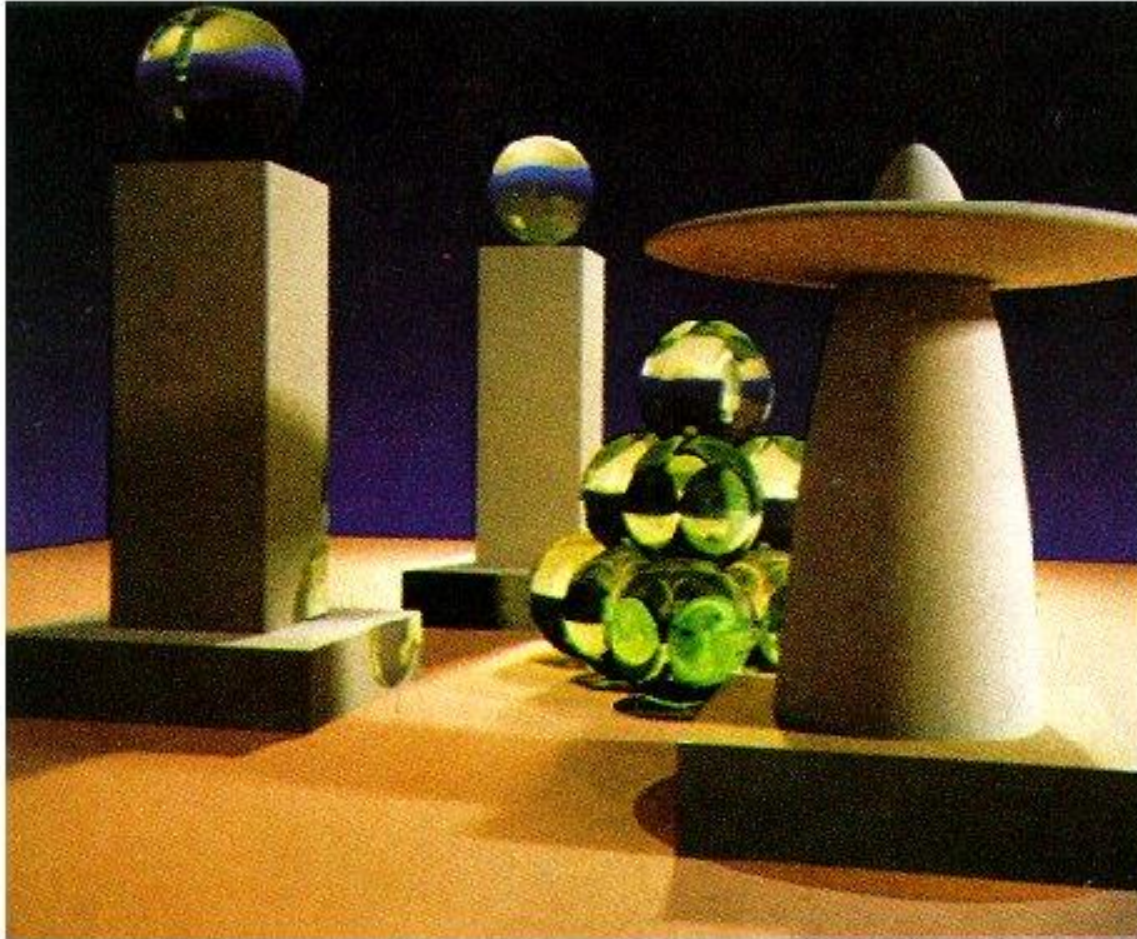
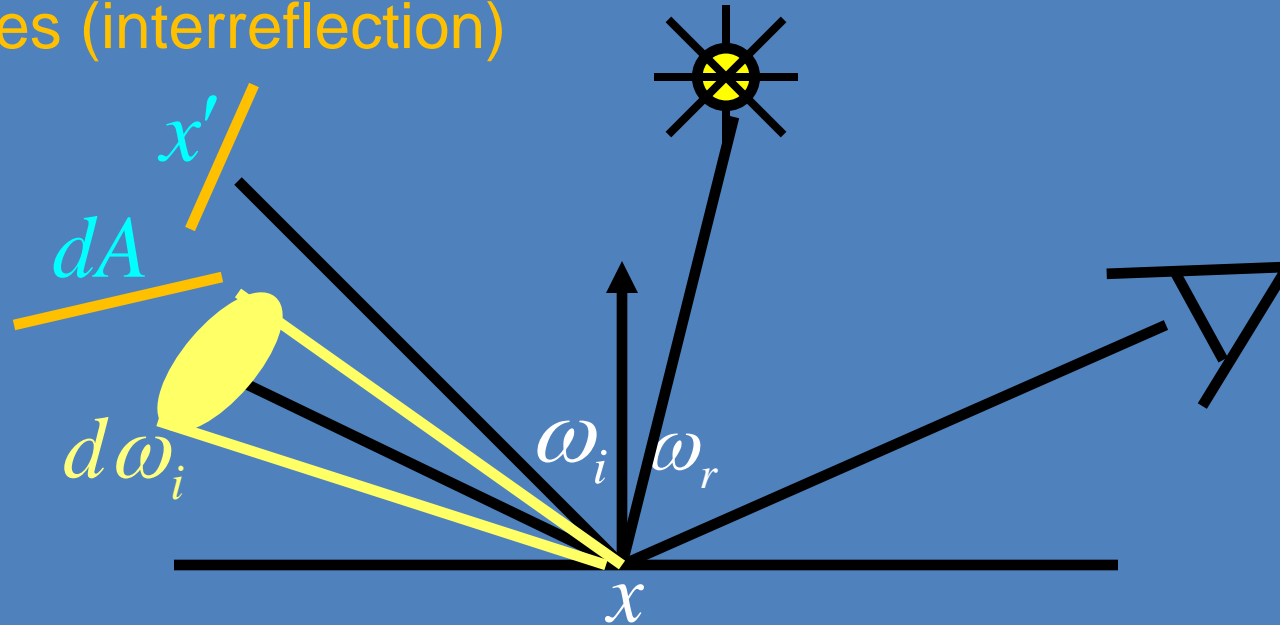


Figure 6. A sample image. All objects are neutral grey. Color on the objects is due to caustics from the green glass balls and color bleeding from the base polygon.

Rendering Equation

Surfaces (interreflection)



$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_r(x', -\omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

Reflected Light
(Output Image)
UNKNOWN

Emission
KNOWN

Reflected
Light
UNKNOWN

BRDF
KNOWN

Cosine of
Incident angle
KNOWN

Rendering Equation

$$L_r(x, \omega_r) = L_e(x, \omega_r) + \int_{\Omega} L_r(x', -\omega_i) f(x, \omega_i, \omega_r) \cos \theta_i d\omega_i$$

Reflected Light (Output Image)	Emission	Reflected Light	BRDF	Cosine of Incident angle
UNKNOWN	KNOWN	UNKNOWN	KNOWN	KNOWN

After applying to simple math and simplifications, it turns we can approximately express the above as

$$L = E + KL$$

L, E are vectors,

K is the light transport matrix

Rendering as a Linear Operator...

$$L = E + KE + K^2E + K^3E + \dots$$

Emission directly
From light sources

Direct Illumination
on surfaces

Global Illumination
(One bounce indirect)
[Mirrors, Refraction]

(Two bounce indirect)
[Caustics, etc...]

Ray Tracing

$$L = E + KE + K^2E + K^3E + \dots$$

Emission directly
From light sources

Direct Illumination
on surfaces

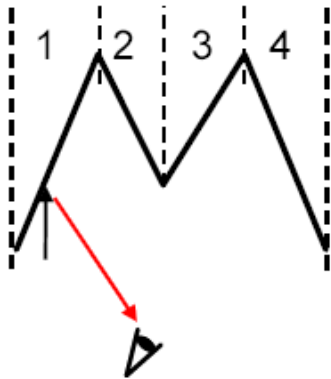
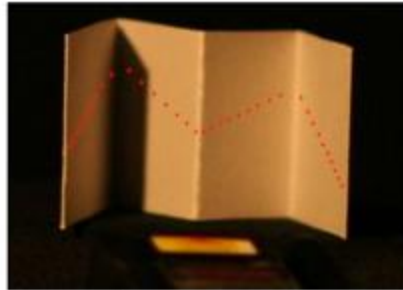
Global Illumination
(One bounce indirect)
[Mirrors, Refraction]

(Two bounce indirect)
[Caustics, etc...]

OpenGL
Shading

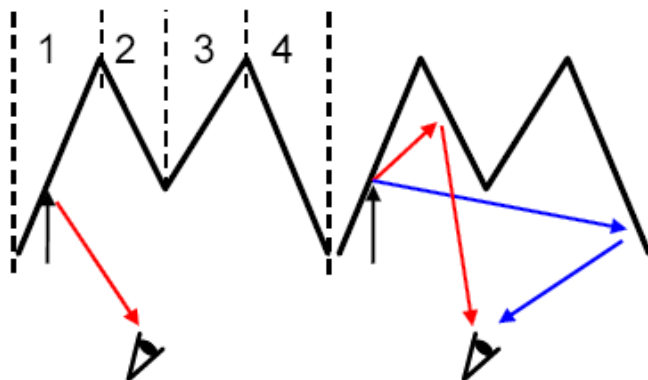
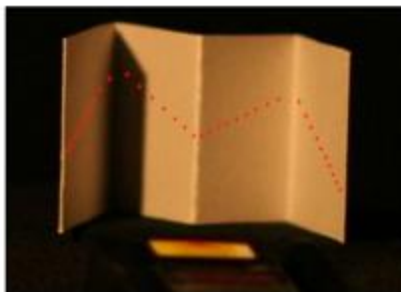


Example



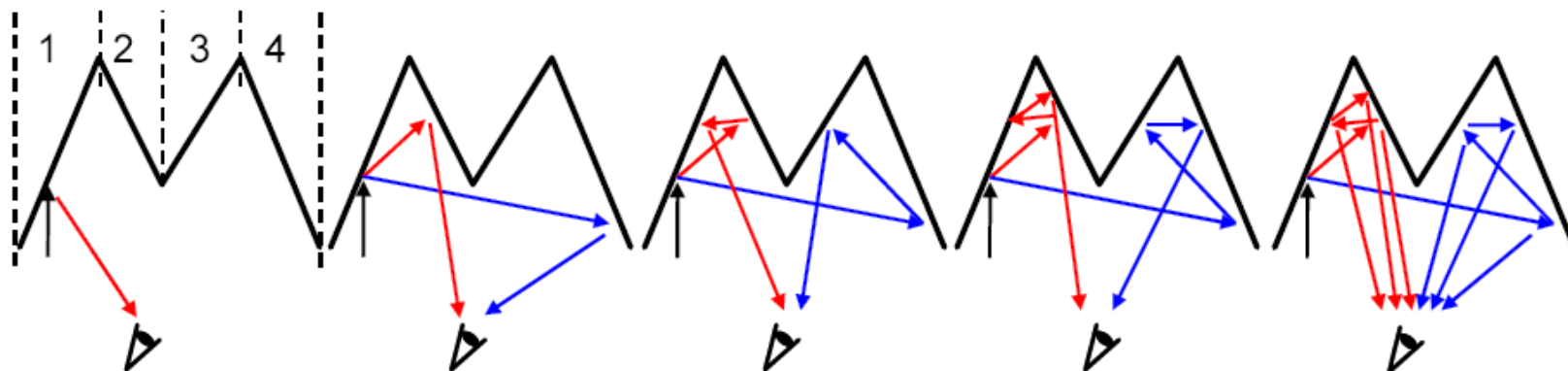
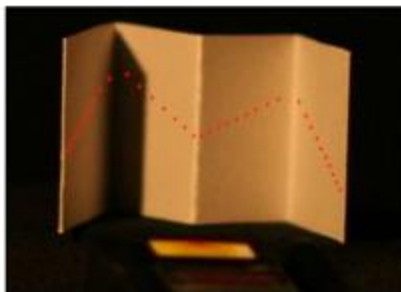


Example





Example





Example

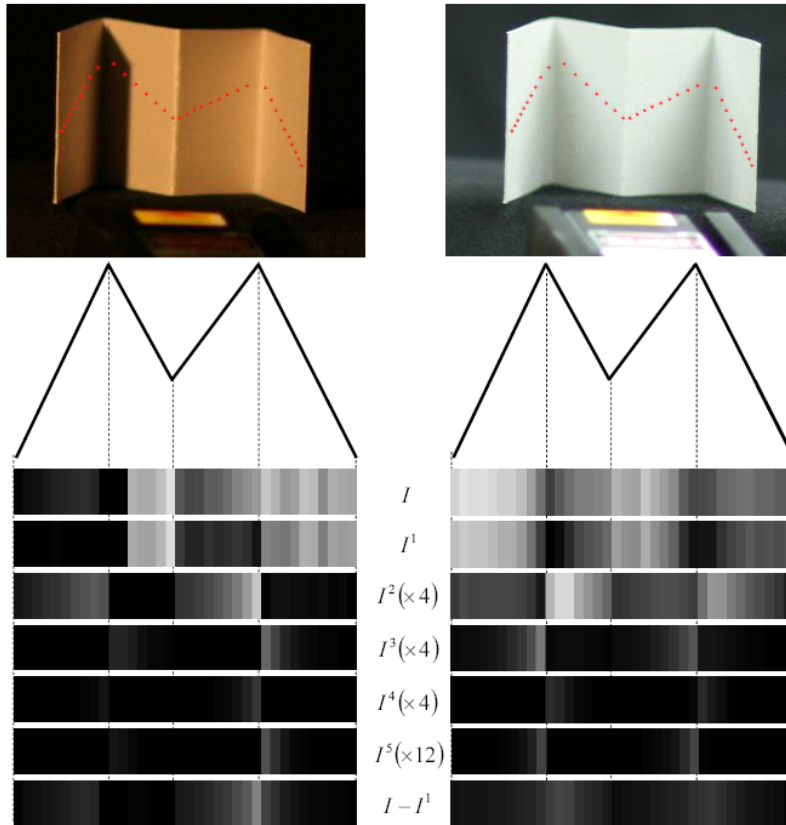


Figure 6: Inverse light transport applied to images I captured under unknown illumination conditions. I is decomposed into direct illumination I^1 and subsequent n -bounce images I^n , as shown. Observe that the interreflections have the effect of increasing brightness in concave (but not convex) junctions of the “M”. Image intensities are scaled linearly, as indicated.

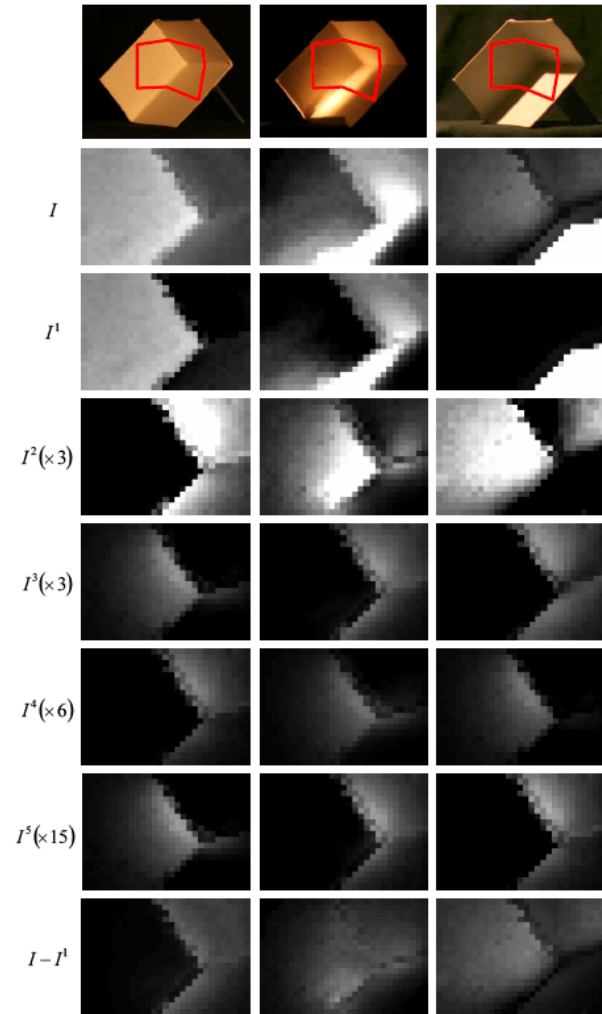


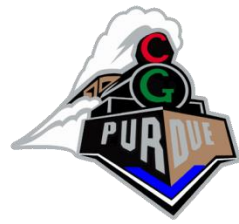
Figure 9: Inverse light transport applied to images captured under unknown illumination conditions: input images I are decomposed into direct illumination I^1 , 2- to 5-bounce images I^2 – I^5 , and indirect illuminations $I - I^1$.

Rendering Equation and Global Illumination Topics



- Local-approximations to Global Illumination
 - Diffuse/Specular
 - Ambient Occlusion
- Global Illumination Algorithms
 - Ray tracing
 - Path tracing
 - Radiosity
- Bidirectional Reflectance Distribution Functions (BRDF)

Rendering Equation and Global Illumination Topics

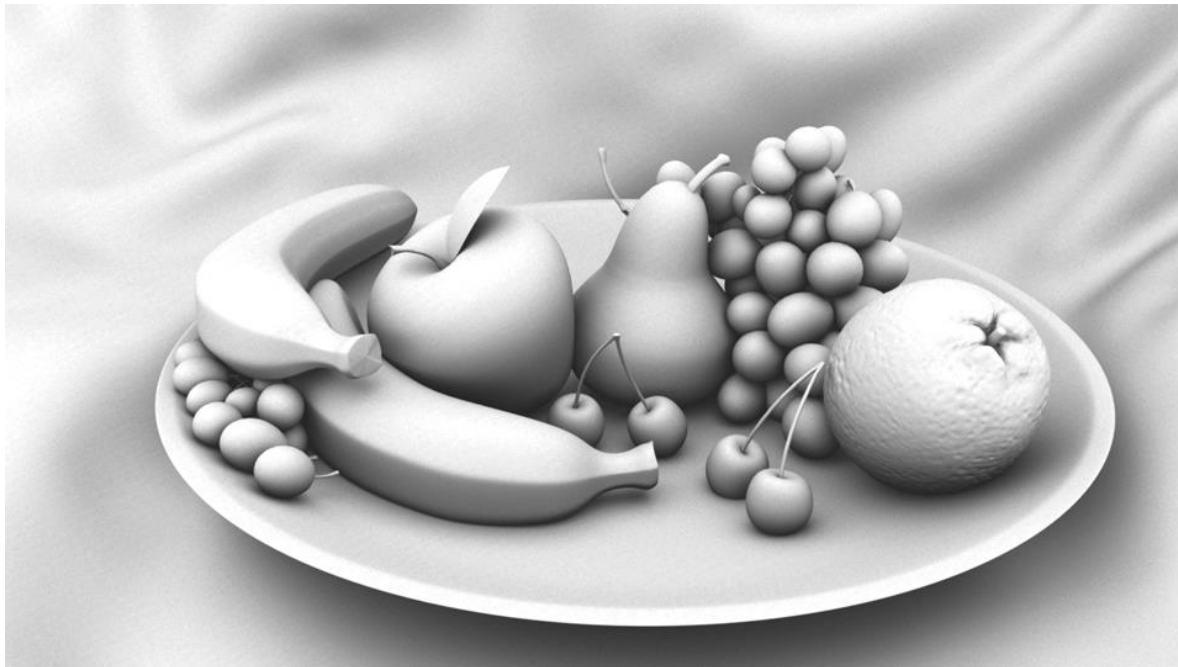


- Local-approximations to Global Illumination
 - Diffuse/Specular
 - **Ambient Occlusion**
- Global Illumination Algorithms
 - Ray tracing
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Ambient Occlusion

- It is a lighting technique to increase the realism of a 3D scene by a “cheap” imitation of global illumination of global illumination

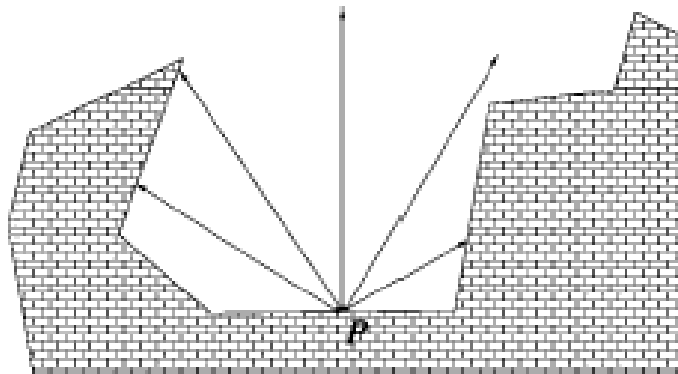


How
does it
work?



History

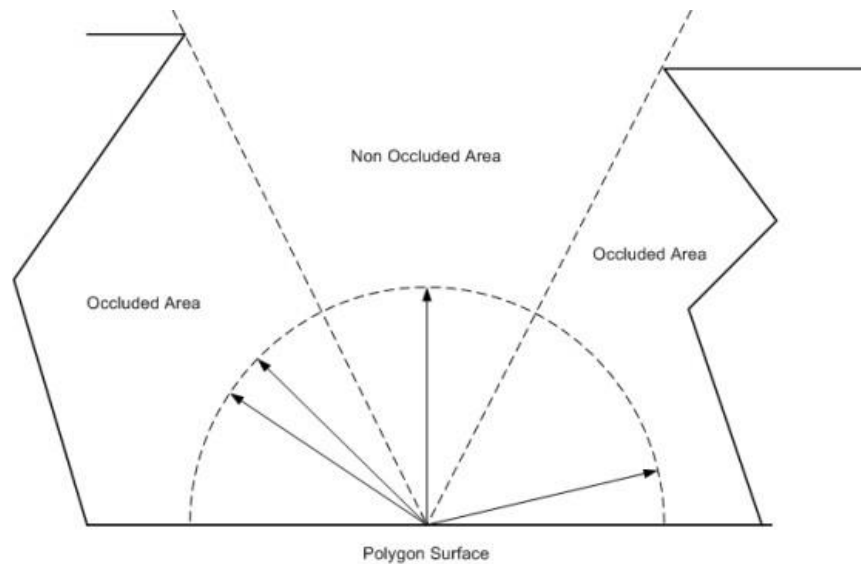
- In 1998, Zhukov introduced *obscurances* in the paper “An Ambient Light Illumination Model.”
- The effect of obscurances : we just need to evaluate the *hiddenness* or occlusion of the point by considering the objects around it.





Occlusion Factor/Map

- Shooting rays outwards
- Determine the occlusion factor at p as a percentage; e.g., $occ(p) \in [0,1]$





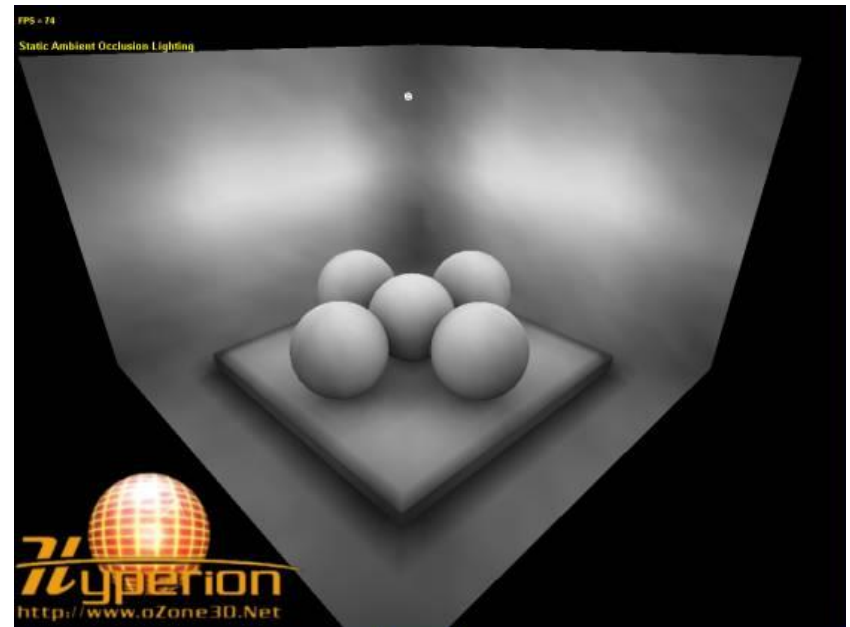
Ambient Occlusion in a Phong Illumination Model

$$I = I_a + I_d + I_s$$

$$I_a = IA \cdot occ(p)$$



Constant ambient intensity rendering



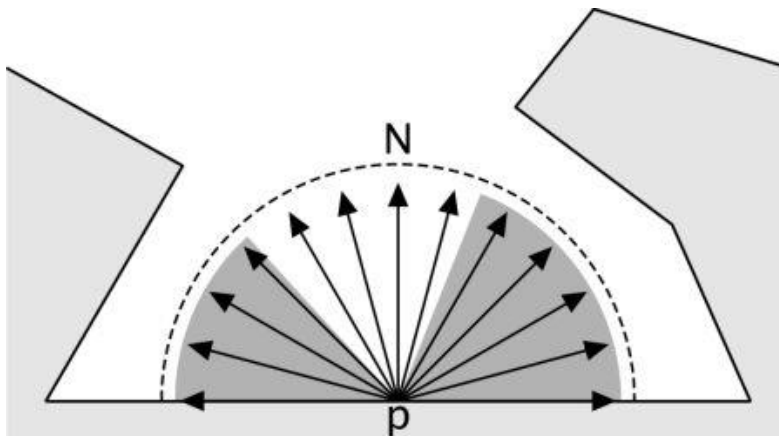
Modulate the intensity by an occlusion factor

Inside-Looking-Out Approach: Ray Casting



- Cast rays from p in uniform pattern across the hemisphere.
- Each surface point is shaded by a ratio of ray intersections to number of original samples.
- Subtracting this ratio from 1 gives us dark areas in the occluded portions of the surface.

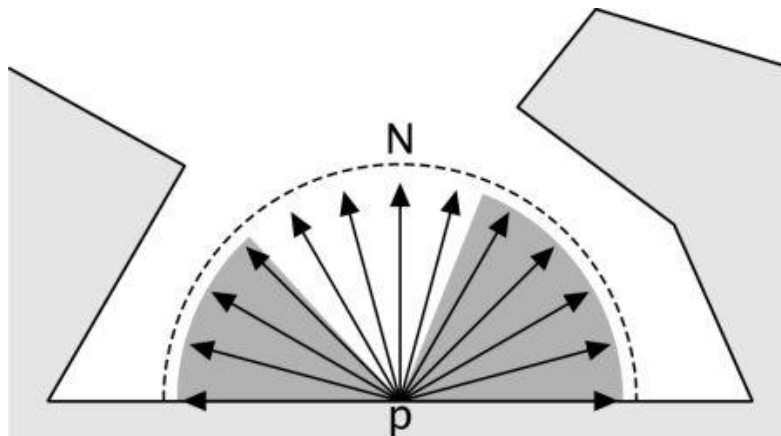
e.g.: Cast 13 rays
9 intersections, so
 $\text{occ}(p) = ?$



Inside-Looking-Out Approach: Ray Casting



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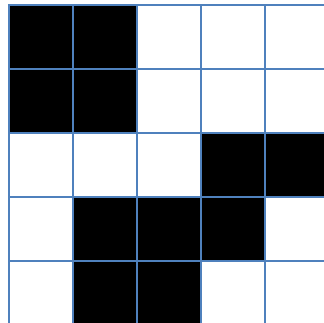


e.g.: Cast 13 rays
9 intersections, so
 $\text{vis}(p)=4/13$;
 $\Rightarrow \text{Color} * 4/13$

Inside-Looking-Out Approach: Hardware Rendering



- Render the view at low-res from p toward normal N
- Rasterize black geometry against a white background
- Take the (cosine-weighted) average of rasterized fragments.



11 black fragments
 \Rightarrow Color * 14/25



Comments

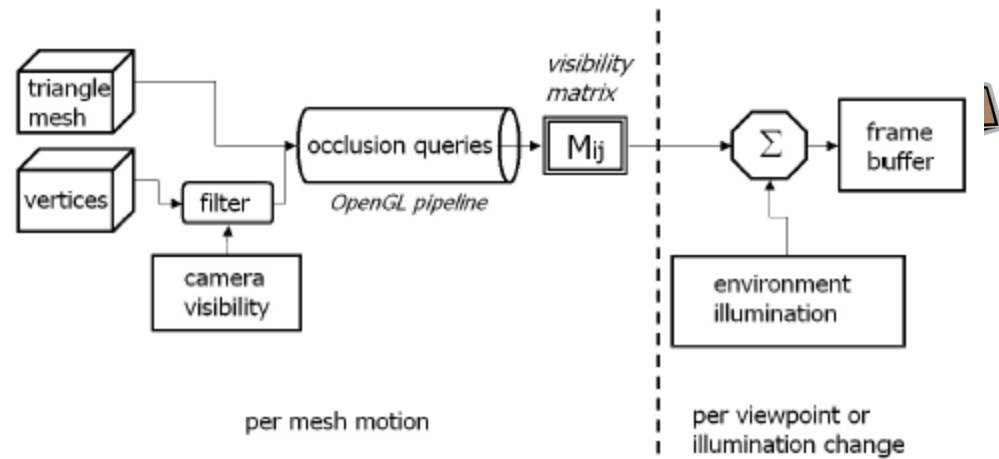
- Potentially huge pre-computation time per scene
- Stores occlusion factor as vertex attributes
 - Thus needs a dense sampling of vertices
- Variations on sampling method
 - “Inside-out” algorithm
 - “outside-in” alternative (not explained)

Outside-Looking-In Approach

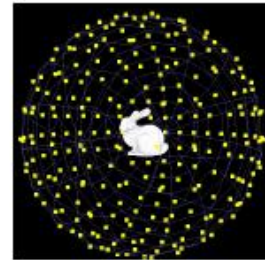
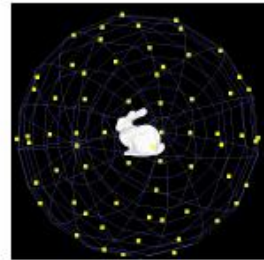
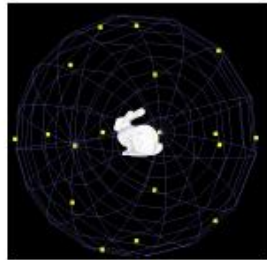
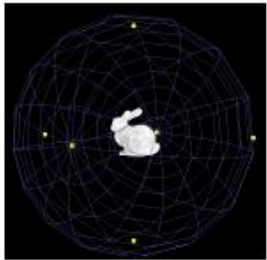


- What would you do?

Outside-Looking-In: One option is [Sattler et. al 2004]

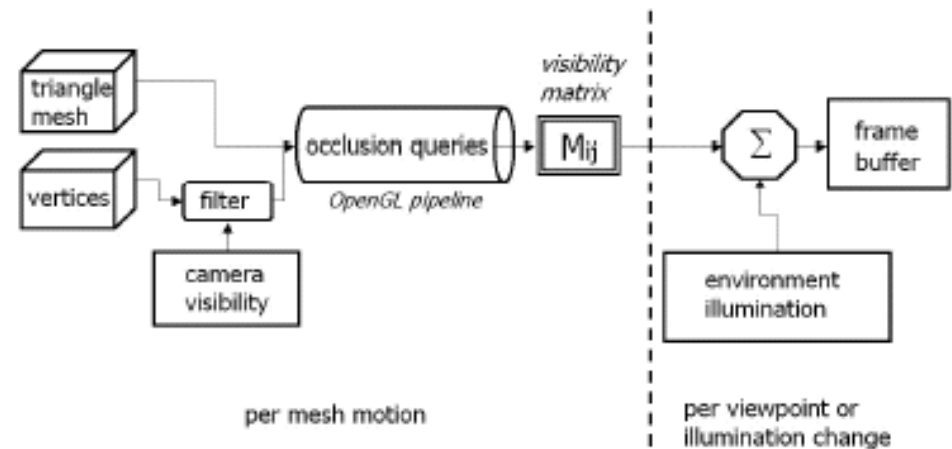


$$c_i = \sum_{j=1}^k M_{ij} I_j$$





```
enable orthographic projection
disable framebuffer
for all light directions  $j$  do
  set camera at light direction  $l_j$ 
  render object into depth buffer with polygon offset
  for all vertices  $i$  do
    begin query  $i$ 
    render vertex  $i$ 
    end query  $i$ 
  end for
  for all vertices  $i$  do
    retrieve result from query  $i$ 
    if result is "visible" then
       $M_{ij} = \mathbf{n}_i \cdot \mathbf{l}_j$ 
    end if
  end for
end for
```



$$M_{ij} = \begin{cases} \mathbf{n}_i \cdot \mathbf{l}_j & : \text{vertex visible} \\ 0 & : \text{vertex invisible} \end{cases}$$

$$c_i = \sum_{j=1}^k M_{ij} I_j$$



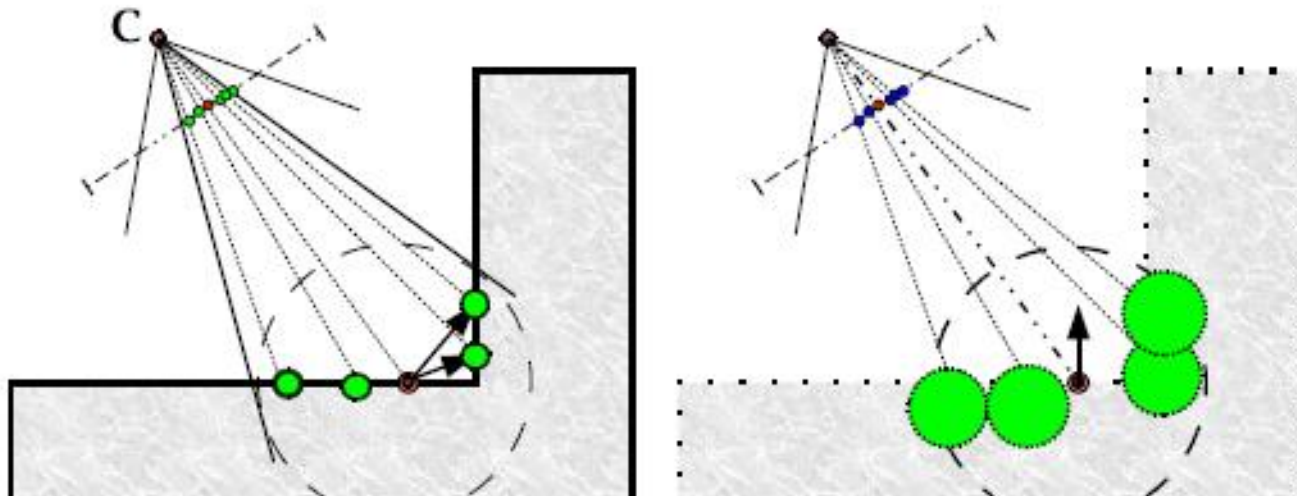
[Sattler et al. 2004]

- For each light on the light sphere
- Take the depth map (for occlusion query)
- Use occlusion query to determine the visibility matrix



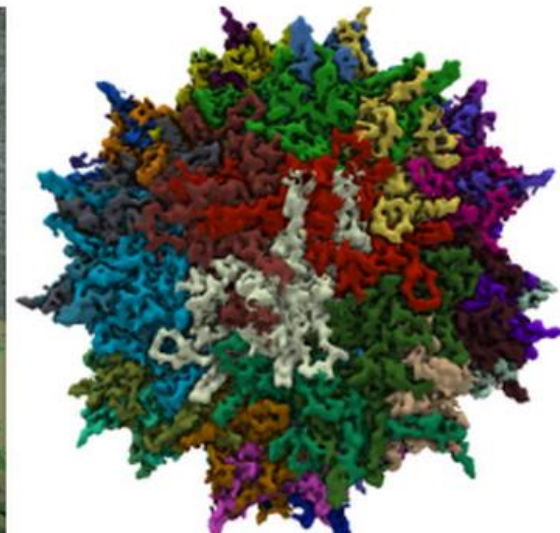
Another option: Screen-Based AO

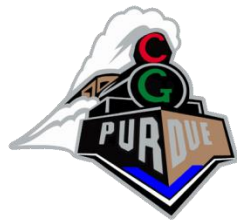
- SHANMUGAM, P., AND ARIKAN, O. 2007. Hardware Accelerated Ambient Occlusion Techniques on GPUs. In Proceedings of ACM Symposium in Interactive 3D Graphics and Games, ACM.





Screen-Based AO

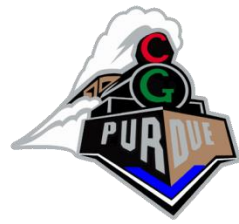




Screen-Based AO

- What would you do?

Rendering Equation and Global Illumination Topics



- Local-approximations to Global Illumination
 - Diffuse/Specular
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- Global Illumination Algorithms
 - Ray tracing
 - Path tracing
 - **Radiosity**
- Bidirectional Reflectance Distribution Functions (BRDF)



Radiosity

- Radiosity, inspired by ideas from heat transfer, is an application of a finite element method to solving the rendering equation for scenes with purely diffuse surfaces.
- The main idea of the method is **to store illumination values on the surfaces of the objects, as the light is propagated starting at the light sources.**

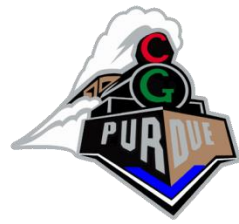
[Radiosity slides heavily based on Dr.
Mario Costa Sousa, Dept. of of
CS, U. Of Calgary]



Radiosity

- Calculating the overall light propagation within a scene, for short **global illumination** is a very difficult problem.
- With a standard ray tracing algorithm, this is a very time consuming task, since a huge number of rays have to be shot.

Radiosity (Computer Graphics)



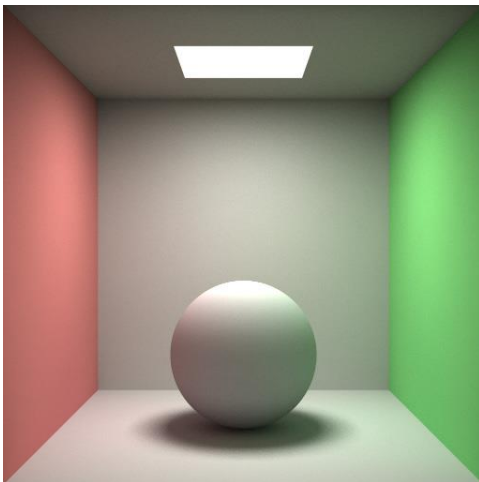
- Assumption #1: surfaces are diffuse emitters and reflectors of energy, emitting and reflecting energy uniformly over their entire area.
- Assumption #2: an equilibrium solution can be reached; that all of the energy in an environment is accounted for, through absorption and reflection.
- Also viewpoint independent: the solution will be the same regardless of the viewpoint of the image.



Radiosity

- Equation:

$$B_i = E_i + \rho_i \sum B_j F_{ij}$$



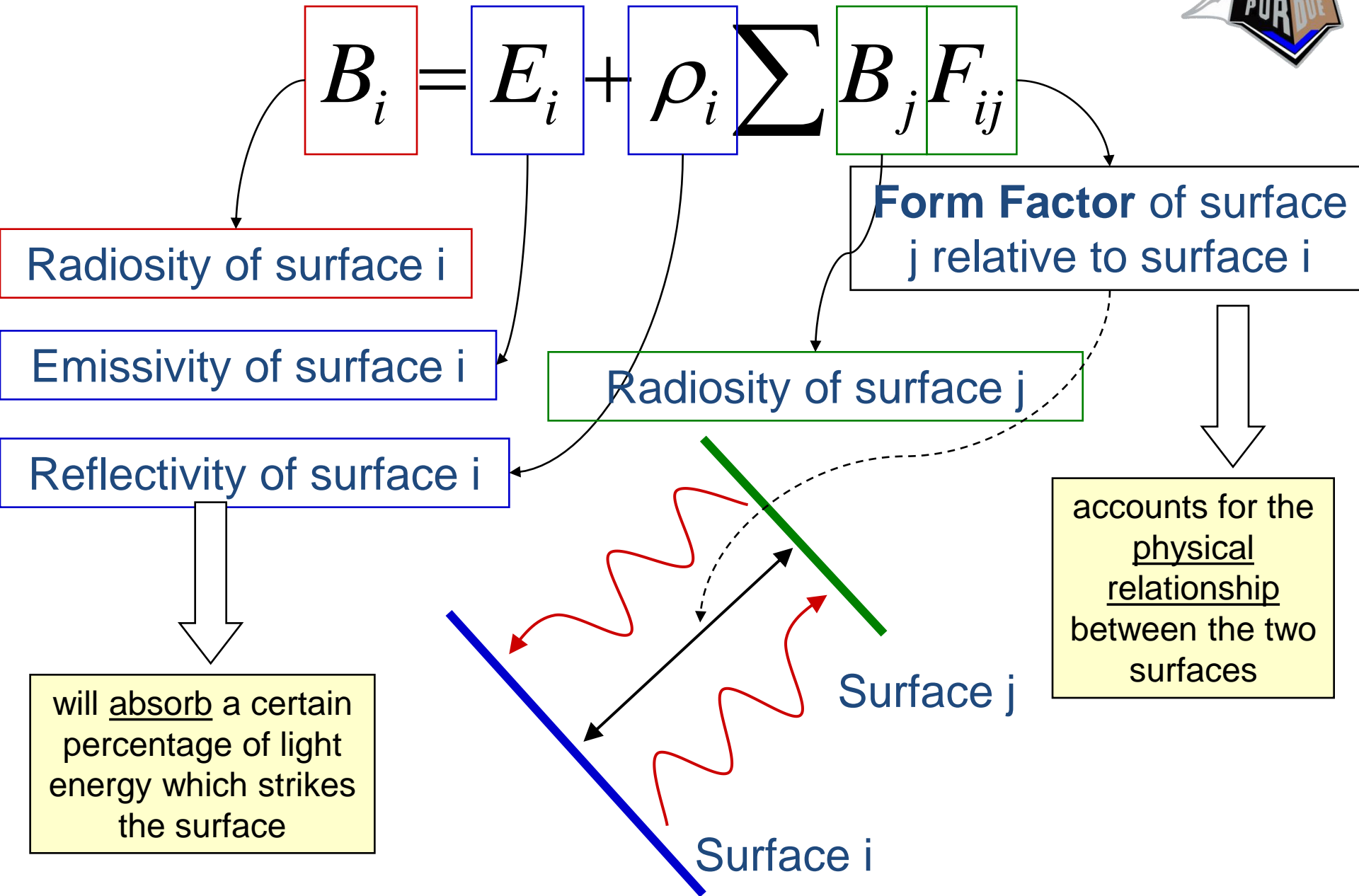
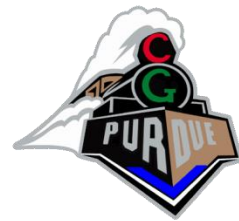


Ray Tracing



Radiosity

The Radiosity Equation

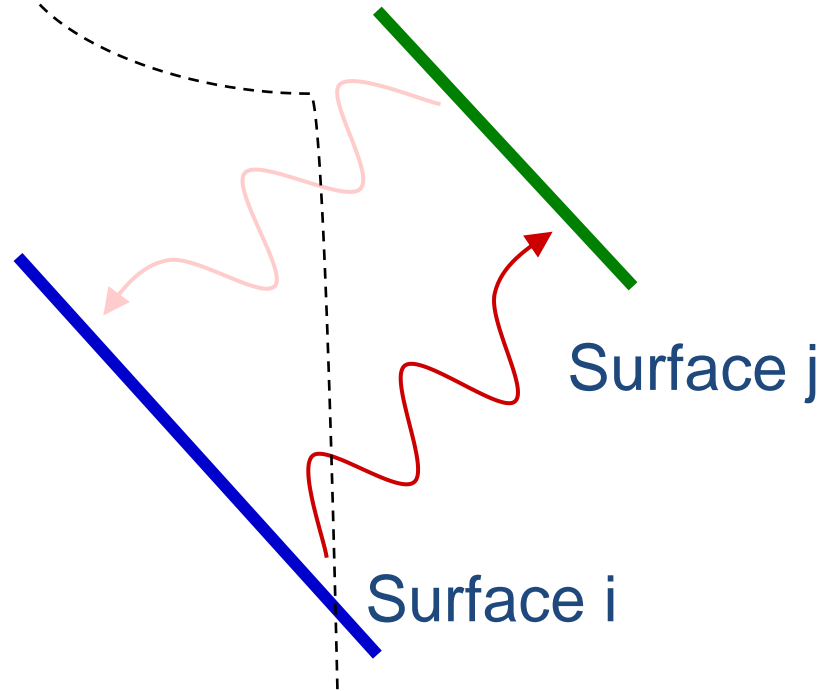


The Radiosity Equation



$$B_i = E_i + \rho_i \sum B_j F_{ij}$$

Energy emitted by surface i

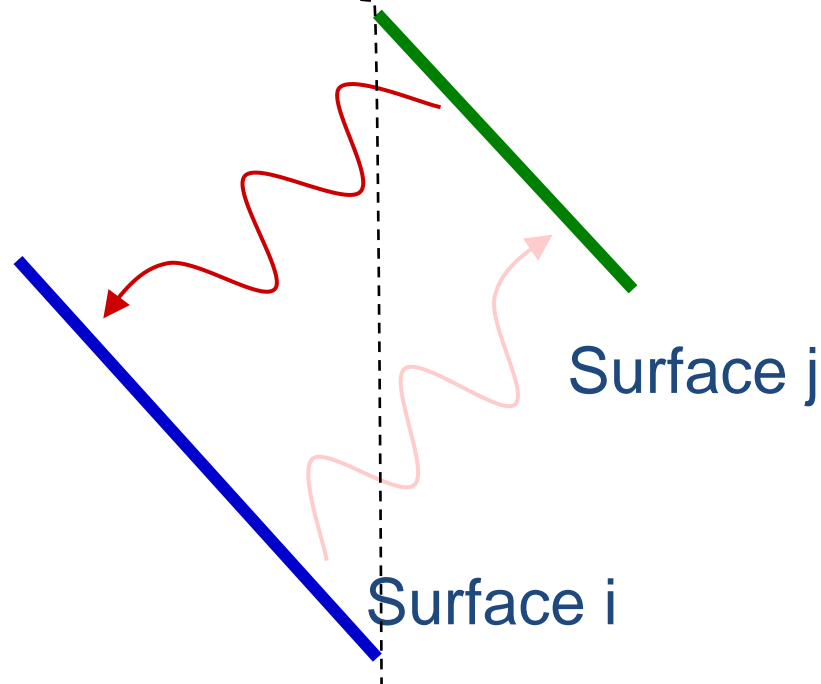


The Radiosity Equation

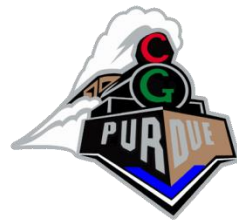


$$B_i = E_i + \rho_i \sum B_j F_{ij}$$

Energy reaching surface i from other surfaces

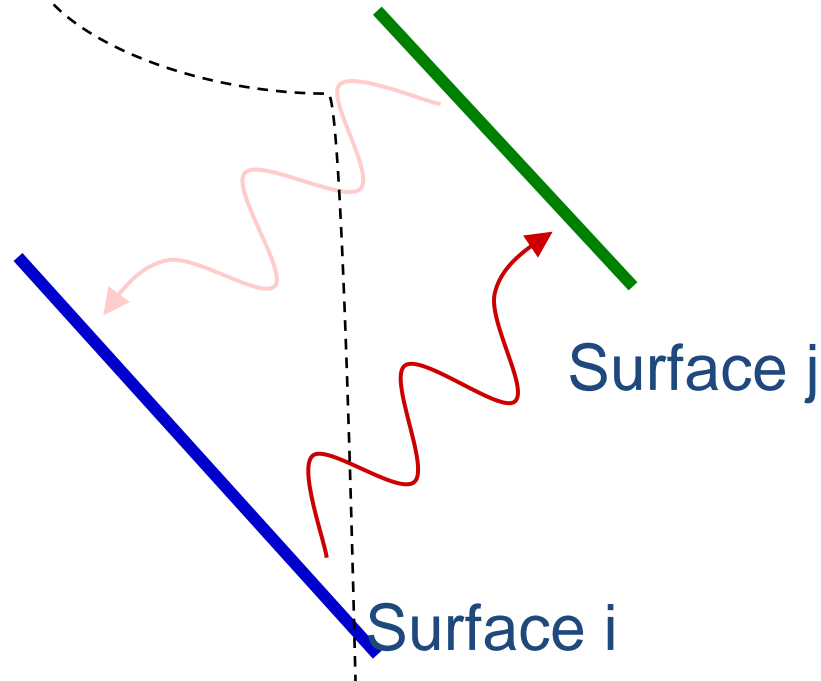


The Radiosity Equation



$$B_i = E_i + \rho_i \sum B_j F_{ij}$$

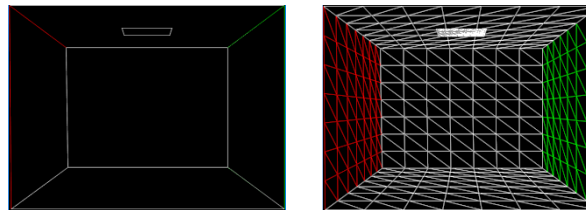
Energy reflected by surface i



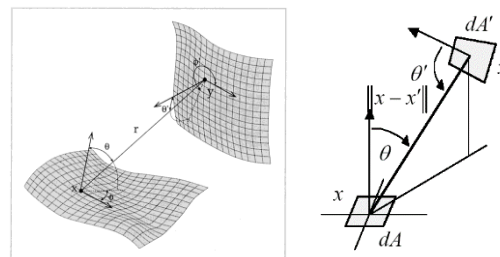
Classic Radiosity Algorithm



Mesh Surfaces into Elements



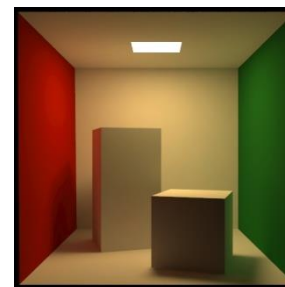
Compute Form Factors
Between Elements



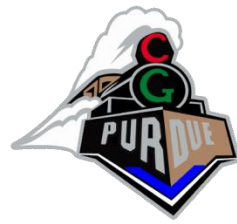
Solve for Radiosities

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \\ x_7 \\ x_8 \\ x_9 \\ x_{10} \end{bmatrix} = \begin{bmatrix} f_{11} & f_{12} & f_{13} & f_{14} & f_{15} & f_{16} & f_{17} & f_{18} & f_{19} & f_{10} \\ f_{21} & f_{22} & f_{23} & f_{24} & f_{25} & f_{26} & f_{27} & f_{28} & f_{29} & f_{20} \\ f_{31} & f_{32} & f_{33} & f_{34} & f_{35} & f_{36} & f_{37} & f_{38} & f_{39} & f_{30} \\ f_{41} & f_{42} & f_{43} & f_{44} & f_{45} & f_{46} & f_{47} & f_{48} & f_{49} & f_{40} \\ f_{51} & f_{52} & f_{53} & f_{54} & f_{55} & f_{56} & f_{57} & f_{58} & f_{59} & f_{50} \\ f_{61} & f_{62} & f_{63} & f_{64} & f_{65} & f_{66} & f_{67} & f_{68} & f_{69} & f_{60} \\ f_{71} & f_{72} & f_{73} & f_{74} & f_{75} & f_{76} & f_{77} & f_{78} & f_{79} & f_{70} \\ f_{81} & f_{82} & f_{83} & f_{84} & f_{85} & f_{86} & f_{87} & f_{88} & f_{89} & f_{80} \\ f_{91} & f_{92} & f_{93} & f_{94} & f_{95} & f_{96} & f_{97} & f_{98} & f_{99} & f_{90} \\ f_{101} & f_{102} & f_{103} & f_{104} & f_{105} & f_{106} & f_{107} & f_{108} & f_{109} & f_{100} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \\ x_7 \\ x_8 \\ x_9 \\ x_{10} \end{bmatrix} + \begin{bmatrix} E_1 \\ E_2 \\ E_3 \\ E_4 \\ E_5 \\ E_6 \\ E_7 \\ E_8 \\ E_9 \\ E_{10} \end{bmatrix}$$

Reconstruct and
Display Solution



Solving for radiosity solution



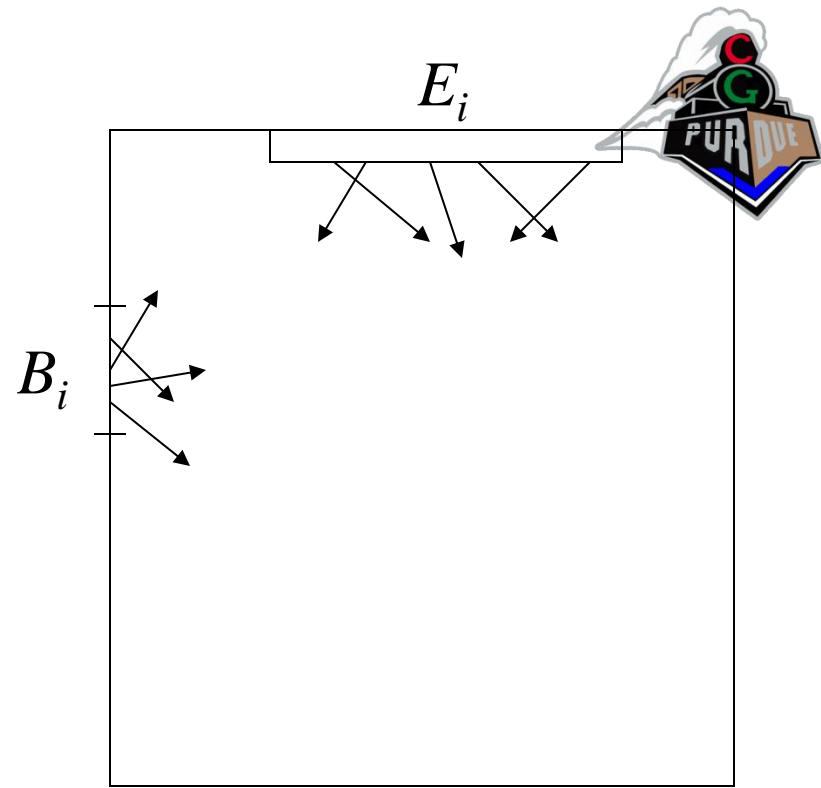
- The "Full Matrix" Radiosity Algorithm
- Gathering & Shooting

Radiosity Matrix

$$B_i = E_i + \rho_i \sum_{j=1}^n F_{ij} B_j$$

What is the matrix form?
(like “Ax=b”)

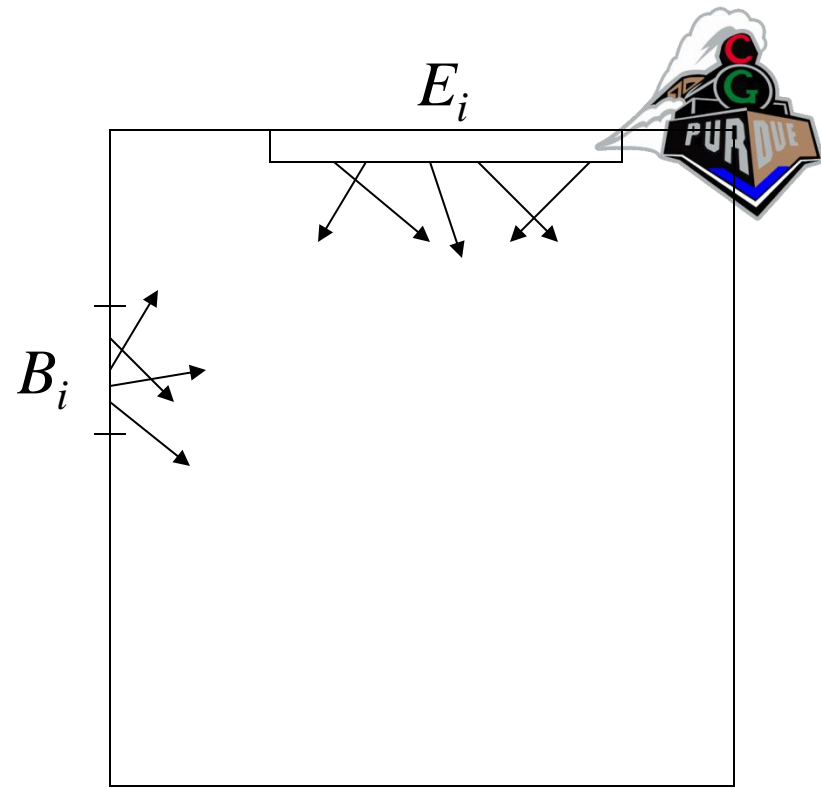
$$B_i - \rho_i \sum_{j=1}^n F_{ij} B_j = E_i$$



Radiosity Matrix

$$B_i = E_i + \rho_i \sum_{j=1}^n F_{ij} B_j$$

$$B_i - \rho_i \sum_{j=1}^n F_{ij} B_j = E_i$$



$$\begin{bmatrix} 1 - \rho_1 F_{11} & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\ -\rho_2 F_{21} & 1 - \rho_2 F_{22} & \cdots & -\rho_2 F_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ -\rho_n F_{n1} & -\rho_n F_{n2} & \cdots & 1 - \rho_n F_{nn} \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ \vdots \\ B_n \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \vdots \\ E_n \end{bmatrix}$$



Radiosity Matrix

- The "full matrix" radiosity solution calculates the form factors between each pair of surfaces in the environment, then forms a series of simultaneous linear equations.

$$\begin{bmatrix} 1 - \rho_1 F_{11} & -\rho_1 F_{12} & \cdots & -\rho_1 F_{1n} \\ -\rho_2 F_{21} & 1 - \rho_2 F_{22} & \cdots & -\rho_2 F_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ -\rho_n F_{n1} & -\rho_n F_{n2} & \cdots & 1 - \rho_n F_{nn} \end{bmatrix} \begin{bmatrix} B_1 \\ B_2 \\ \vdots \\ B_n \end{bmatrix} = \begin{bmatrix} E_1 \\ E_2 \\ \vdots \\ E_n \end{bmatrix}$$

- This matrix equation is solved for the "B" values, which can be used as the final intensity (or color) value of each surface.



Solving for radiosity solution

- The "Full Matrix" Radiosity Algorithm
- Gathering & Shooting

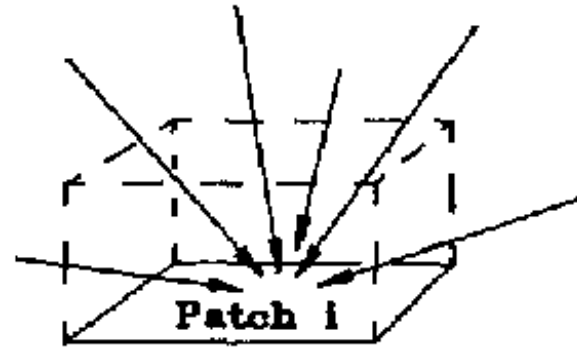
-
- A diagram showing a grid of dashed lines. A central point is marked where several solid lines intersect. The area around this point is labeled "Patch 1".

$$\begin{bmatrix} \mathbf{x} \\ \mathbf{y} \end{bmatrix} = \begin{bmatrix} \mathbf{x} \\ \mathbf{0} \end{bmatrix} + \begin{bmatrix} \mathbf{0} \\ \mathbf{y} \end{bmatrix}$$

$$B_i = E_i + \sum_{j=1}^n (\rho_i F_{ij}) B_j$$

$$B_i \text{ due to } B_j = \rho_i B_j F_{ij}$$

Gathering



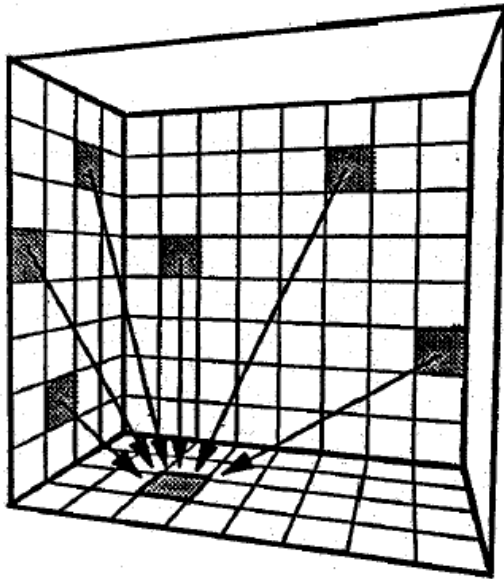
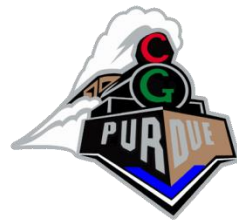
GATHERING

- Gathering light through a hemi-cube allows one patch radiosity to be updated.

$$\begin{array}{c}
 \left[\begin{array}{c} \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \end{array} \right] = \left[\begin{array}{c} \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \end{array} \right] + \left[\begin{array}{c} \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \\ \text{XXXXXXXXXX} \end{array} \right] \left[\begin{array}{c} \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \\ \mathbf{x} \end{array} \right]
 \end{array}$$

$$B_i = E_i + \sum_{j=1}^n (\rho_i F_{ij}) B_j$$

Gathering

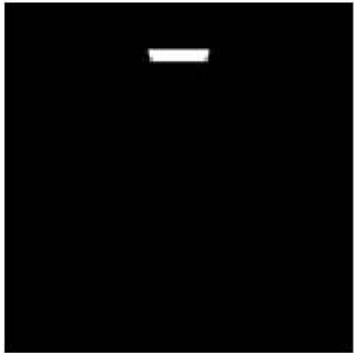


```
for(i=0; i<n; i++)  
    B[i] = Be[i];  
  
while( !converged ) {  
    for(i=0; i<n; i++) {  
        E[i] = 0;  
        for(j=0; j<n; j++)  
            E[i] += F[i][j]*B[j];  
        B[i] = Be[i]+rho[i]*E[i];  
    }  
}
```

Row of F times B

Calculate one row of F and discard

■ Successive Approximation



L_e



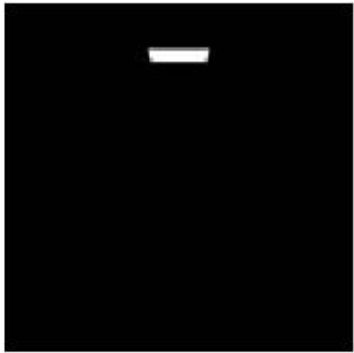
$K \circ L_e$



$K \circ K \circ L_e$



$K \circ K \circ K \circ L_e$



L_e



$L_e + K \circ L_e$

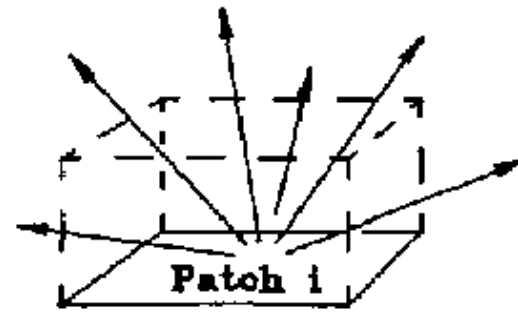


$L_e + \dots K^2 \circ L_e$



$L_e + \dots K^3 \circ L_e$

Shooting



SHOOTING

- Shooting light through a single hemi-cube allows the whole environment's radiosity values to be updated simultaneously.

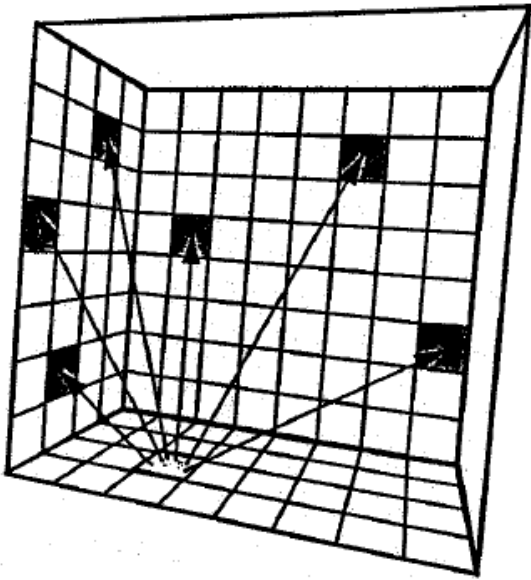
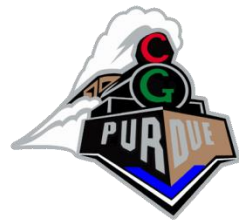
$$\begin{bmatrix} x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \end{bmatrix} = \begin{bmatrix} x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \end{bmatrix} + \begin{bmatrix} x \end{bmatrix} \begin{bmatrix} x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \\ x \end{bmatrix}$$

Four red arrows point from the four vectors in the equation down to the corresponding terms in the radiosity equation below.

$$\text{For all } j \implies B_j = B_j + B_i (\rho_j E_{ji})$$

$$\text{where } F_{ji} = \frac{F_{ij} A_i}{A_j}$$

■ Shooting



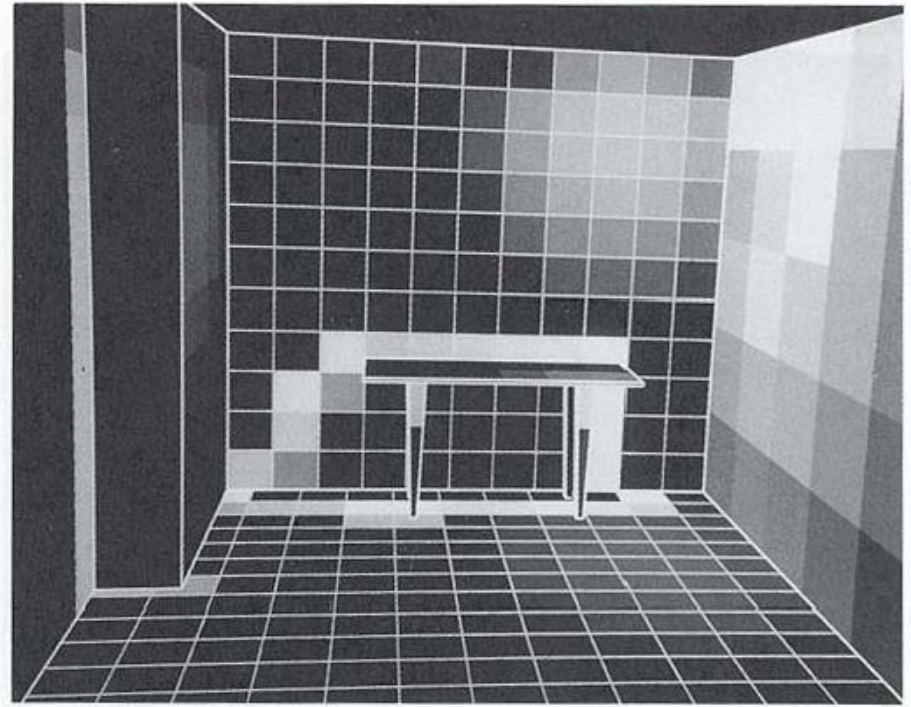
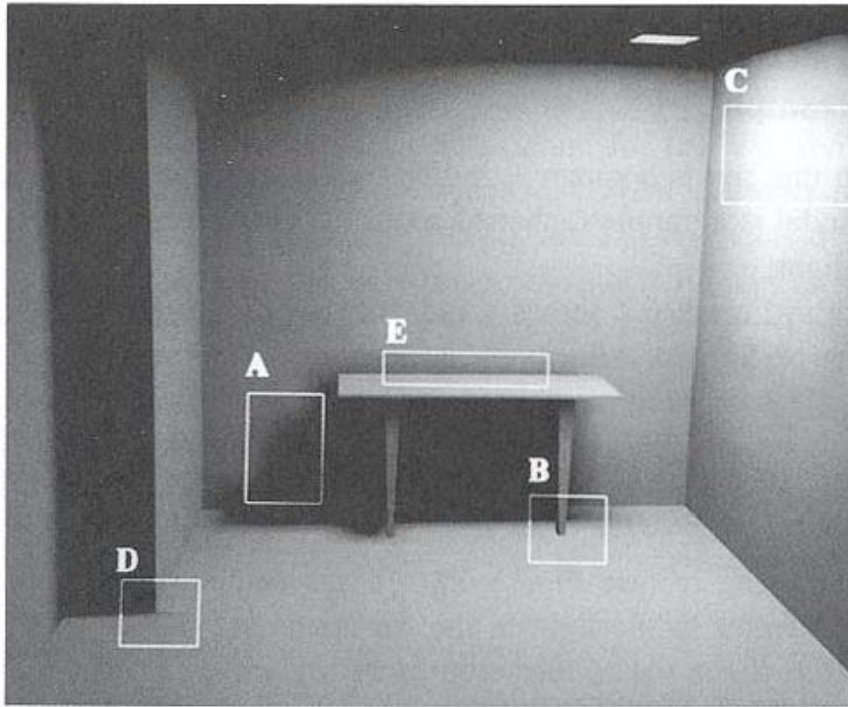
```
for(i=0; i<n; i++) {  
    B[i] = dB[i] = Be[i];  
    while( !converged ) {  
        set i st dB[i] is the largest;  
        for(j=0;j<n;j++)  
            if(i!=j) {  
                db =rho[j]*F[j][i]*dB[i];  
                dB[j] += db;  
                B[j] += db;  
            }  
        dB[i]=0;  
    }  
}
```

Brightness order

Column of F times B



Artifacts



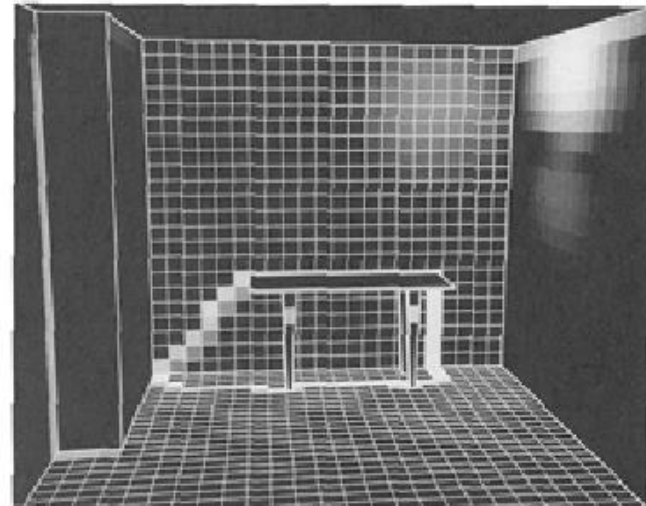
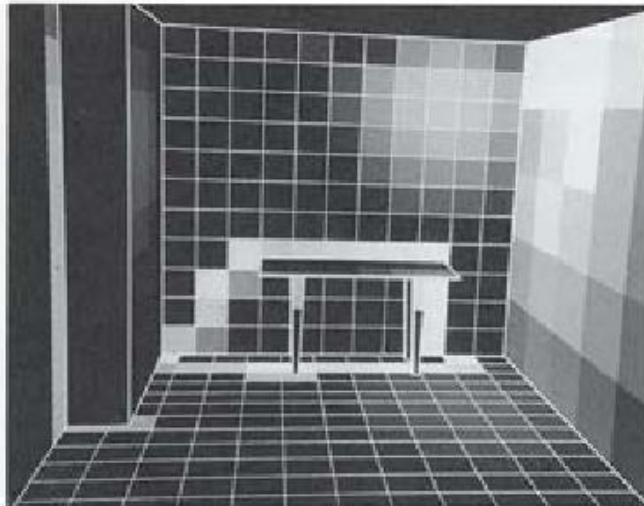
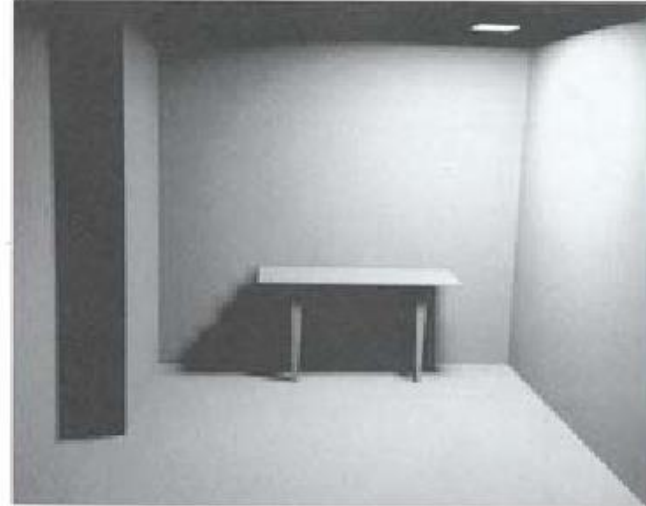
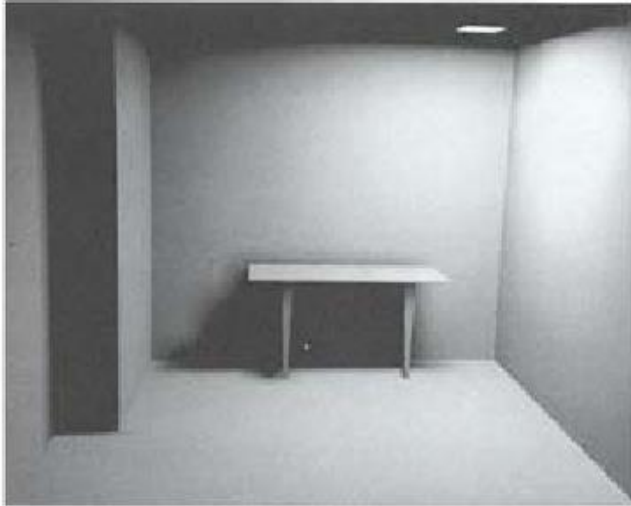
Error Image

- A. Blocky shadows**
- B. Missing features**
- C. Mach bands**
- D. Inappropriate shading discontinuities**
- E. Unresolved discontinuities**

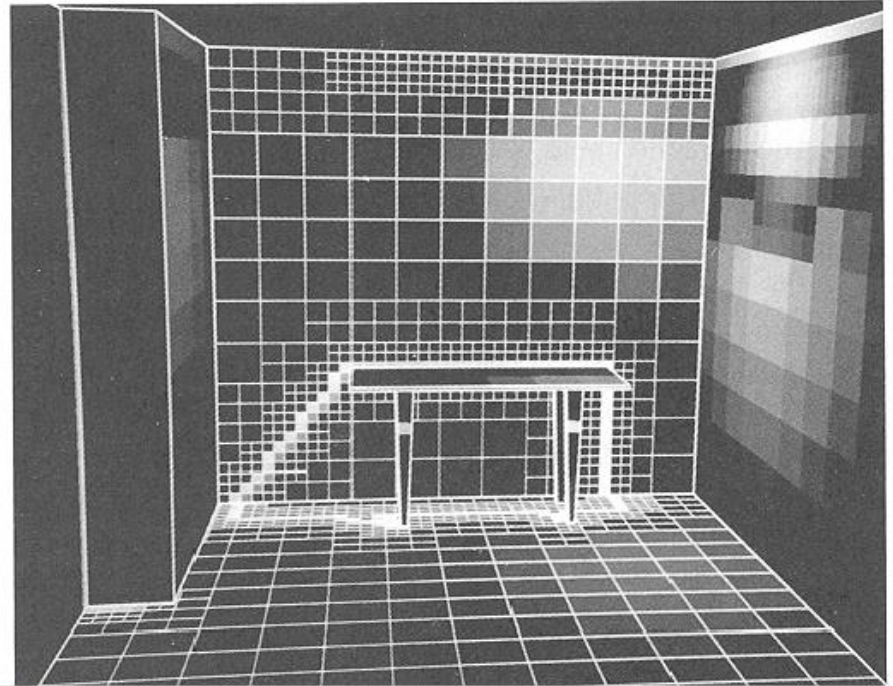
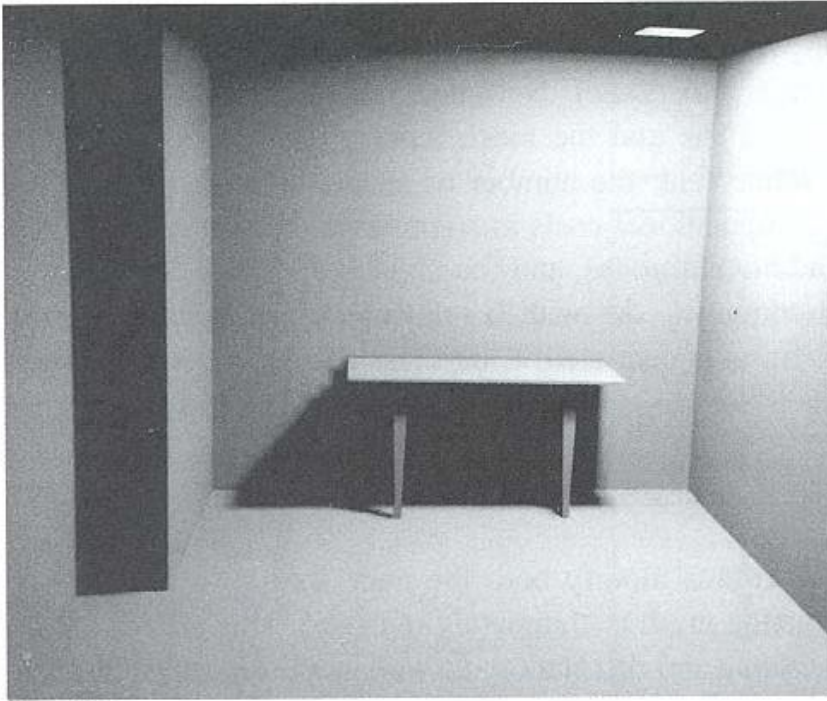
What can you do?



Increase Resolution



Adaptively Mesh

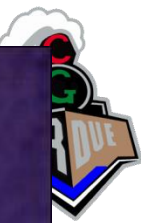




e.g., Discontinuity Meshing

More examples...

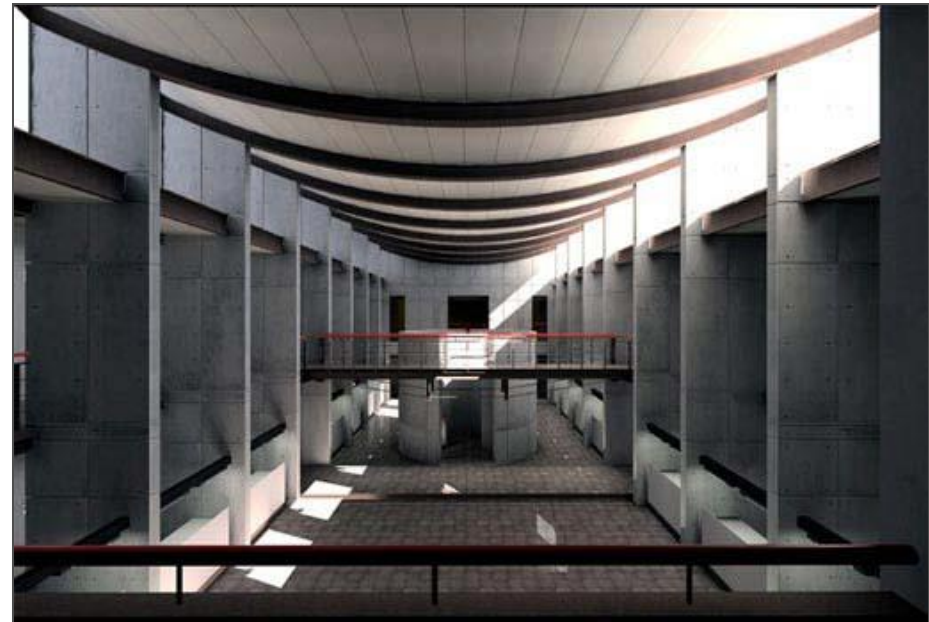


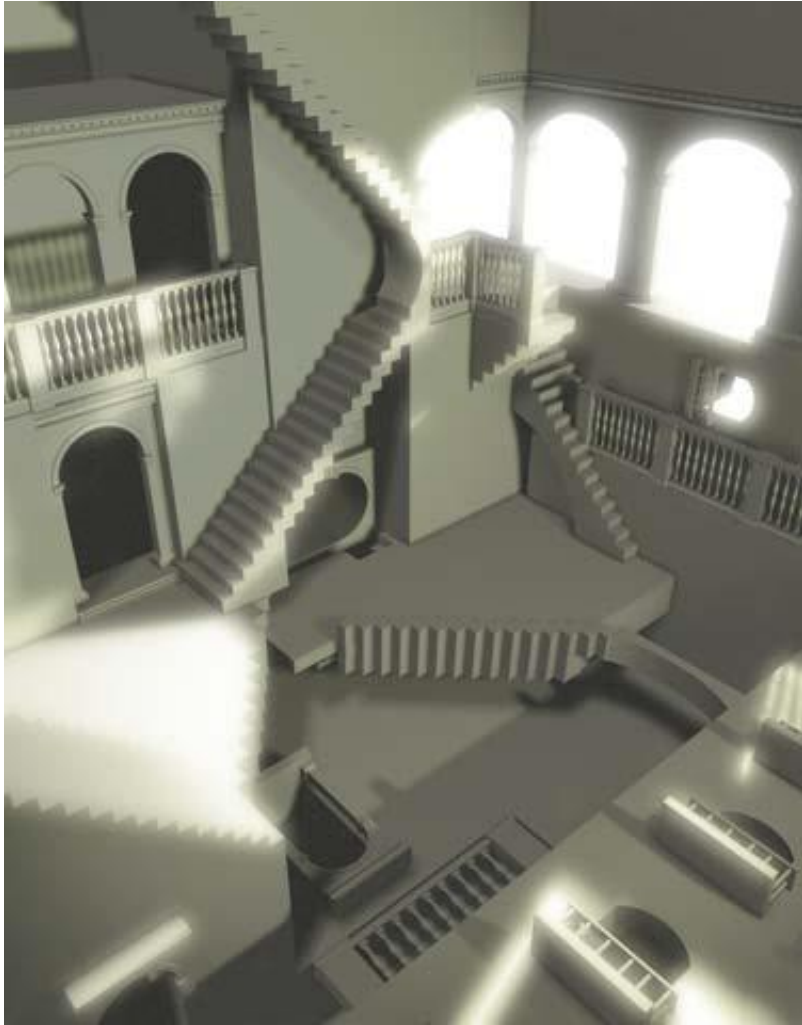
















Rendering Equation and Global Illumination Topics



- Local-approximations to Global Illumination
 - Diffuse/Specular
 - Ambient Occlusion
- Global Illumination Algorithms
 - Ray tracing
 - Path tracing
 - Radiosity
- **Bidirectional Reflectance Distribution Functions (BRDF)**

Materials Demo...



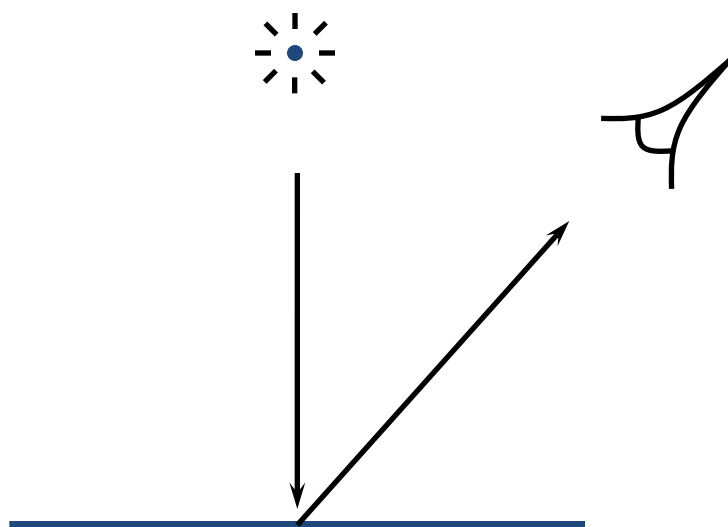


Measuring BRDFs

- BRDF is 4-dimensional, though simpler measurements (0D/1D/2D/3D) are often useful

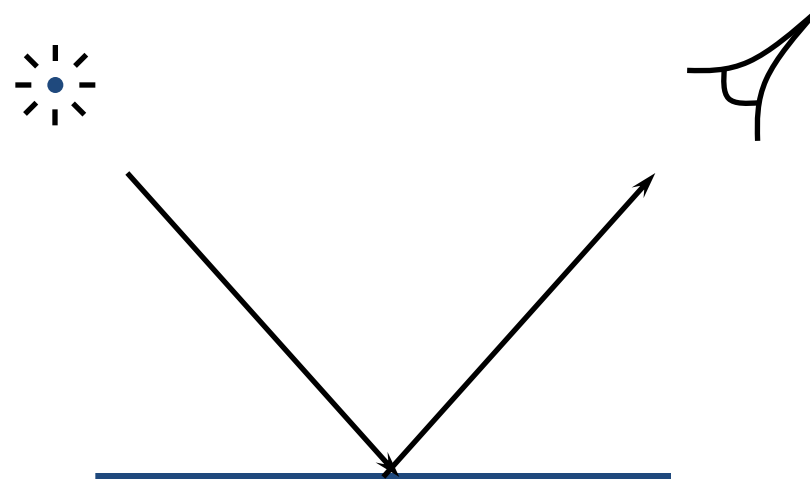


Measuring Reflectance



$0^\circ/45^\circ$

Diffuse Measurement



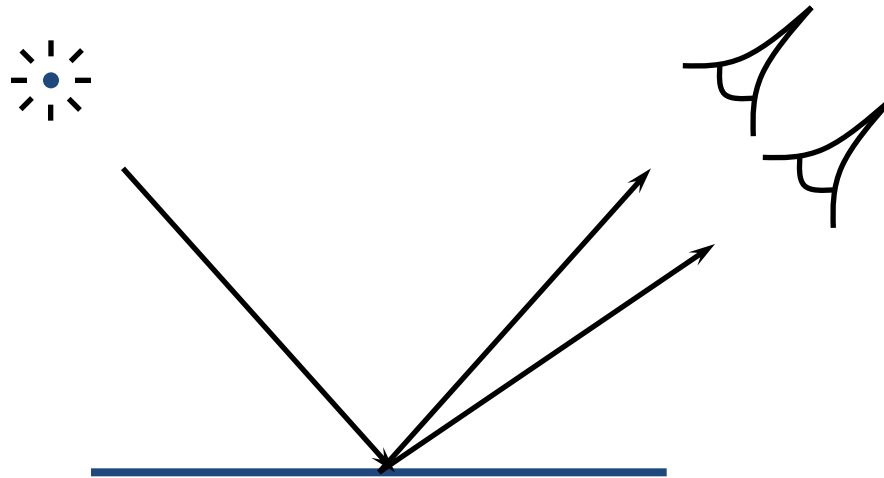
$45^\circ/45^\circ$

Specular Measurement



Gloss Measurements

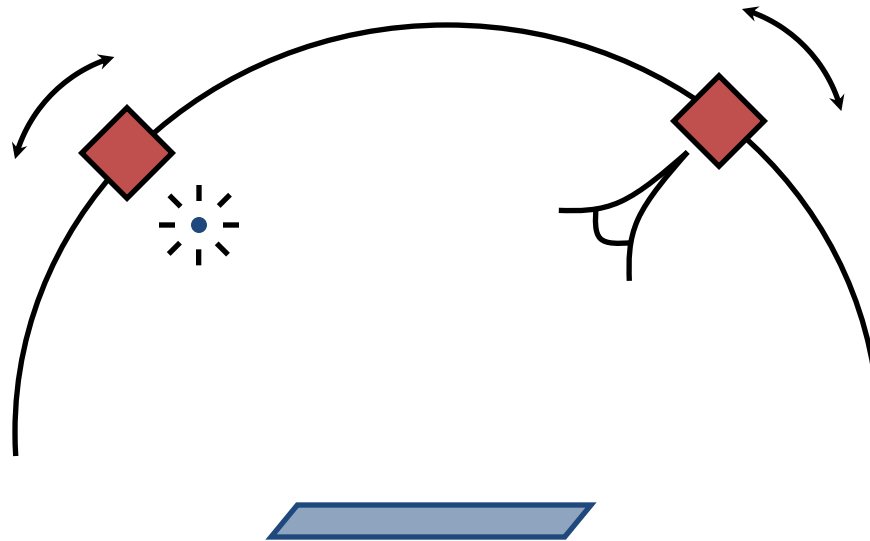
- “Haze” is the width of a specular peak





BRDF Measurements

- Next step up: measure over a 1- or 2-D space



Gonioreflectometers

- Or a 4D space

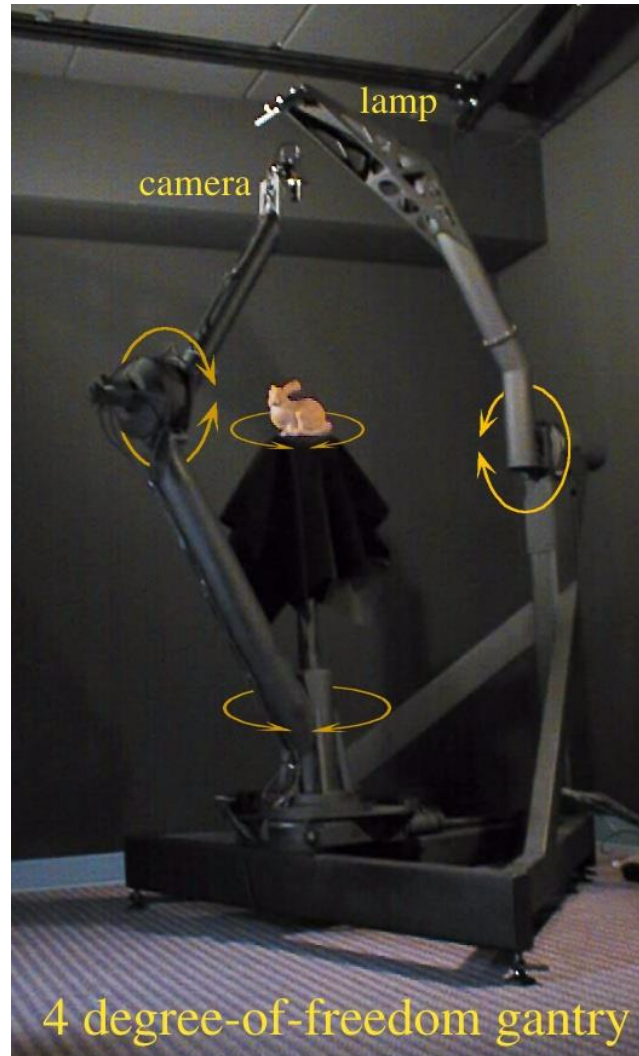


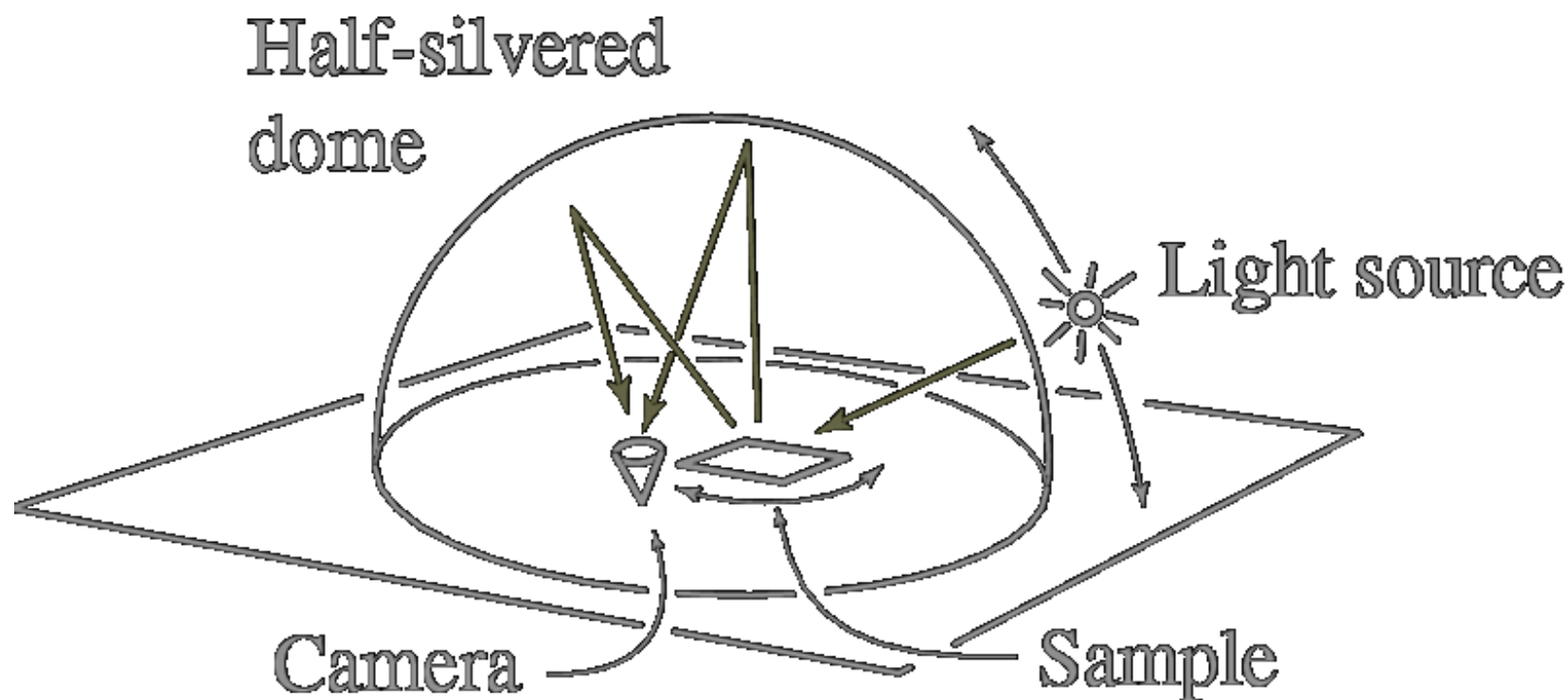


Image-Based BRDF Measurement

- A camera acquires with each picture a 2D image of sampled measurements
 - Requires mapping light angles to camera pixels



Ward's BRDF Measurement Setup





Ward's BRDF Measurement Setup

- Each picture captures light from a hemisphere of angles





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Measurement

- 20-80 million reflectance measurements per material
- Each tabulated BRDF entails $90 \times 90 \times 180 \times 3 = 4,374,000$ measurement bins

