

# <u>Graphics Pipeline</u>: Transformation, Shading/Lighting, Projection, Texturing, and more!

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# **Computer Graphics Pipeline**

Geometry

**Modeling Transformation** Transform into 3D world coordinate system Simulate illumination and reflectance Lighting **Viewing Transformation** Transform into 3D *camera* coordinate system Clipping Clip primitives outside camera's view Projection Transform into 2D camera coordinate system Scan Conversion Draw pixels (incl. texturing, hidden surface...) Image



# Modeling Transformations

- Most popular transformations in graphics
  - Translation
  - Rotation
  - Scale
  - Projection
- In order to use a single matrix for all, we use homogeneous coordinates...

## Modeling Transformations





$$\begin{bmatrix} x'\\y'\\z'\\w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & tx\\0 & 1 & 0 & ty\\0 & 0 & 1 & tz\\0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\w \end{bmatrix}$$

Translation

$$\begin{bmatrix} x'\\y'\\z'\\w \end{bmatrix} = \begin{bmatrix} -1 & 0 & 0 & 0\\0 & 1 & 0 & 0\\0 & 0 & 1 & 0\\0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\w \end{bmatrix}$$

Mirror over X axis



# Modeling Transformations

#### Rotate around Z axis:

$$\begin{bmatrix} x'\\y'\\z'\\w \end{bmatrix} = \begin{bmatrix} \cos\Theta & -\sin\Theta & 0 & 0\\ \sin\Theta & \cos\Theta & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\w \end{bmatrix}$$

Rotate around Y axis:

$$\begin{bmatrix} x'\\y'\\z'\\w \end{bmatrix} = \begin{bmatrix} \cos\Theta & 0 & -\sin\Theta & 0\\0 & 1 & 0 & 0\\\sin\Theta & 0 & \cos\Theta & 0\\0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\w \end{bmatrix}$$

And many more...

Rotate around X axis:

$$\begin{bmatrix} x'\\y'\\z'\\w \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0\\ 0 & \cos\Theta & -\sin\Theta & 0\\ 0 & \sin\Theta & \cos\Theta & 0\\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x\\y\\z\\w \end{bmatrix}$$



## Diffuse









(mostly)

## Specular++











#### **Environment Mapping**





#### Subsurface Scatterring



## Others



#### Transparency









Radiosity

Ambient occlusion

#### Others









- Light sources
  - Point light
    - Models an omnidirectional light source (e.g., a bulb)
  - Directional light
    - Models an omnidirectional light source at infinity
  - Spot light
    - Models a point light with direction
- Light model
  - Ambient light
  - Diffuse reflection
  - Specular reflection



- Diffuse reflection
  - Lambertian model



- Diffuse reflection
  - Lambertian model





- Diffuse reflection
  - Lambertian model





- Specular reflection
  - Phong model



- Specular reflection
  - Phong model





- Specular reflection
  - Phong model







## **Viewing Transformation**











#### **Perspective Projection**





$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} fX/Z \\ fY/Z \end{pmatrix} \checkmark \qquad \begin{pmatrix} fX \\ fY \\ Z \end{pmatrix} = \begin{bmatrix} f & 0 & 0 & 0 \\ 0 & f & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{pmatrix} X \\ Y \\ Z \\ 1 \end{pmatrix}$$



## **Projection Transformations**



void glFrustum(GLdouble left, GLdouble right, GLdouble bottom, GLdouble top, GLdouble near, GLdouble far);



## **Projection Transformations**



void gluPerspective(GLdouble fovy, GLdouble aspect, GLdouble
near, GLdouble far);



## **Projection Transformations**



void glOrtho(GLdouble left, GLdouble right, GLdouble bottom, GLdouble top, GLdouble near, GLdouble far);

void gluOrtho2D(GLdouble left, GLdouble right, GLdouble bottom, GLdouble top);





- Determine which fragments get generated
- Interpolate parameters (colors, textures, normals, etc.)





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• How?



- Determine which fragments get generated
- Interpolate parameters (colors, textures, normals, etc.)



Barycentric coords amongst many other ways...



## Barycentric coordinates





## Barycentric coordinates



Two equations, two unknowns: use 2x2 matrix inversion...

# Additional concept: Texture mapping

- Model surface-detail with images
  - wrap object with photograph(s)
  - graphics object itself is a simpler model but "looks" more complex





## Texture mapping



– wrap object with photograph(s)

 graphics object itself is a simpler model but "looks" more complex





## Texture coordinates

- Mechanism for attaching the texture map to the surface modeled
  - a pair of floats (s, t) for each triangle vertex
  - corners of the image are (0, 0), (0, 1), (1, 1), and (1, 0)
  - tiling indicated with tex. coords. > 1
  - *texels* color samples in texture maps

#### Texture coordinates









#### Texels: texture elements





#### **Texture mapping** Problem: how to $P_2(s_2, t_2)$ compute the texture $P(s, t) \xrightarrow{P_1(s_1, t_1)}$ coordinates for an interior pixel? а $P_{3}(s_{3}, t_{3})$ $P_2$ С Ρ **0**3 b X





## Parameter Interpolation

• Texture coordinates, colors, normals, etc.



• How?

– Again, use barycentric coordinates...