Sorting

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Sorting

A fundamental algorithm of significant importance to many applications.

There is no *single* best sorting algorithm – it is application specific.

Algorithms range from $O(n^2)$ to seemingly $O(n)$ under certain conditions.

General sorting of arbitrary unorganized keys is at best $O(n \log n)$

- If you can do better, please patent it, then let us know (me first)
What is the easiest sorting algorithm to program?

- (using a standard built-in library is not a valid answer 😊)
Sorting 101

Live demo
Bubble Sort

“The easiest sorting algorithm to program”

Algorithm:

repeat
    for x = 1 to N-1
        if (A[x] > A[x+1]) then swap
    end
until (no more swaps)
Bubble Sort

What is the big-Oh?
- O(n^2)

Algorithm:
```
repeat
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    for x = 1 to N-1
      if (A[x] > A[x+1]) then swap
  end
  until (no more swaps)
```

Bubble Sort

What is the worst-case input?
- When array is in reverse order

**Algorithm:**
```
repeat
  for x = 1 to N-1
    if (A[x] > A[x+1]) then swap
  end
until (no more swaps)
```
Bubble Sort

Summary
- $O(n^2)$
- Worst case is when input is in reverse order

When is the algorithm useful?
- If need to implement something quick and dirty
- If only have access to immediately neighboring array element and have a small memory cache
Improvements?

How can you do better than standard bubble sort?

- Let's remove the “restriction” of only swapping with the immediate neighbor.
- Instead and starting at the beginning of the array, let's find the smallest guy in the rest of the array and swap it with the current element.
Selection Sort

Algorithm:
1. Find the minimum value in the array
2. Swap it with the value in the first position
3. Do again starting at the second position but only with later array elements
4. Repeat until end of array

What is the big-oh?
- $O(n^2)$

When/why is this better than bubble sort?
- Application specific, but for instance if data can only be accessed “in a forward fashion” and previously processed array elements are not accessible anymore (e.g., tape? network?)
Improvements?

How can you do better than bubble sort or selection sort?

- Instead of “swapping” an element with a later element, let’s “insert” the next element into place.
- This is the “natural sorting algorithm” often used by Homo Sapiens to sort items (e.g., exams, notes, bones)
Insertion Sort

“Natural sorting algorithm”…live demo
Insertion Sort

Algorithm:
- Starting at the beginning of the array, find the next smallest element
- Insert at the beginning (all other elements must be shifted)
- Find the next smallest element and repeat

What is the big-oh?
- $O(n^2)$
Insertion Sort

Why/when is it good?
- Stable
  - does not change the order of equal keys
- In-place
  - Only requires O(1) extra space
- Online
  - Can sort an array as it receives it
- (the combination of these characteristics makes insertion sort interesting)

Note: if using linked lists, the “insert” operation is easy!
**Insertion Sort**

- What happens when array is almost sorted?
  - Not much “shifting is needed”
  - Performance becomes (near) $O(n)$

- Can you reduce the amount of shifting?
  - Yes, don’t shift by 1-item but shift by $k$-items, then $k/2$, etc, until by 1-item
  - Average performance ranges from $O(n \log^2 n)$ to $O(n^2)$ – this is called “Shell Sort”
Further Improvements?

Lots of other variants to $O(n^2)$ sorting algorithms exist, each with different pros/cons...