# Image Based Rendering 

an overview

## Photographs

- We have tools that acquire and tools that display photographs at a convincing quality level






## Photographs

- We have tools that acquire and tools that display photographs at a convincing quality level, for almost 100 years now




## RGB in early 1900's



## Plenoptic function

- Defines all the rays
- through any point in space $(x, y, z)$
- with any orientation $(\theta, \varphi)$
- over all wavelenghts $(\lambda)$
- at any given moment in time ( t )

$$
\rho=P(x, y, z, \phi, \varphi, \lambda, t)
$$

## IBR summary

Representation of plenoptic function

implicit


## Lightfield - Lumigraph approach [Levoy96, Gortler96]

- Take all photographs you will ever need to display
- Model becomes database of rays
- Rendering becomes database querying


## Overview

- Introduction
- Lightfield - Lumigraph
- definition
- construction
- compression


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## From 7D to 4D

## $\rho=P(x, y, z, \phi, \varphi, \lambda, t)$

- Static scene, t constant
- $\lambda$ approximated with RGB
- consider only convex hull of objects, so the origin of the ray does not matter


## 4D Lightfield / Lumigraph



## Discreet 4D Lightfield



## Lightfield: set of images with COPs on regular grid



## or Lightfield: set of images of a point seen at various angles



## Depth correction of rays



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## Construction from dense set of photographs



## Construction from sparse set of photographs



## Filling in gaps using pull-push algorithm

- Pull phase

- low res levels are created
- gaps are shrunk
- Push phase
- gaps at high res levels are filled using low res levels


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## Compression

- Large size uncompressed: 1.125 GB
$-32 \times 32(\mathrm{~s}, \mathrm{t}) \times 256 \times 256$ (u, v) x 6 faces x 3 B
- Compression
- jpeg + mpeg (200:1 to 6MB)
- or vector quantization + entropy encoding


## Vector Quantization (VQ)

- Principle
- codebook made of codewords
- replace actual word with closest codeword
- Implementation
- training on representative set of words to derive best codebook
- compression: replacing word with index to closest codeword
- decompression: retrieve indexed codeword from codebook


## Lightfield compression using VQ




View morphing

## Motivation - rendering from images


[Seitz96]

- Given
- left image
- right image
- Create intermediate images
- simulates camera movement


## Previous work

- Panoramas ([Chen95], etc)
- user can look in any direction at few given locations
- Image-morphing ([Wolberg90], [Beier92], etc)
- linearly interpolated intermediate positions of features
- input: two images and correspondences
- output: metamorphosis of one image into other as sequence of intermediate images


## Previous work limitations

- Panoramas ([Chen95], etc.)
- no camera translations allowed
- Image morphing ([Wolberg90], [Beier92], etc.)
- not shape-preserving
- image morphing is also a morph of the object
- to simulate rendering with morphing, the object should be rigid when camera moves


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- Introduction
- Image morphing
- View morphing
- image pre-warping
- image morphing
- image post-warping


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## Early IBR research



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## View morphing

- Shape preserving morph
- Three step algorithm

1. Prewarp first and last images to parallel views
2. Image morph between prewarped images
3. Postwarp to interpolated view

## Step 1: prewarp to parallel views



- Parallel views
- same image plane
- image plane parallel to segment connecting the two centers of projection
- Prewarp
- compute parallel views $\mathrm{I}_{0 \mathrm{p}}, \mathrm{I}_{\mathrm{np}}$
- rotate $I_{0}$ and $\mathrm{I}_{\mathrm{n}}$ to parallel views
- prewarp corrs. $\left(\mathrm{P}_{0}, \mathrm{P}_{\mathrm{n}}\right)->\left(\mathrm{P}_{\mathrm{op}}, \mathrm{P}_{\mathrm{np}}\right)$


## Step 2: morph parallel images



- Shape preserving
- Use prewarped correspondences
- Interpolate $\mathrm{C}_{\mathrm{k}}$ from $\mathrm{C}_{0} \mathrm{C}_{\mathrm{n}}$



## Overview

- Introduction
- Image morphing
- View morphing, more details
- image pre-warping
- image morphing
- image post-warping


## Step 1: prewarp to parallel views



- Parallel views
- use $C_{0} C_{n}$ for $x$ ( $a_{p}$ vector)
- use $\left(a_{0} \times b_{0}\right) \times\left(a_{n} \times b_{n}\right)$ as y $\left(-b_{p}\right)$
- pick $a_{p}$ and $b_{p}$ to resemble $a_{0} b_{0}$ as much as possible
- use same pixel size
- use wider field of view


## Step 1: prewarp to parallel views



- prewarping using texture mapping
- create polygon for image plane
- consider it texture mapped with the image itself
- render the "scene" from prewarped view
- if you go this path you will have to implement clipping with the COP plane
- you have texture mapping already
- alternative: prewarping using reprojection of rays
- look up all the rays of the prewarped view in the original view


## Step 1: prewarp to parallel views



- prewarping correspondences
- for all pairs of correspondence $\mathrm{P}_{0} \mathrm{P}_{\mathrm{n}}$
- project $\mathrm{P}_{0}$ on $\mathrm{I}_{0 \mathrm{p}}$, computing $\mathrm{P}_{\mathrm{O}_{\mathrm{p}}}$
- project $\mathrm{P}_{\mathrm{n}}$ on $\mathrm{I}_{\mathrm{n} p}$, computing $\mathrm{P}_{\mathrm{np}}$
- prewarped correspondence is $\mathrm{P}_{\mathrm{op}} \mathrm{P}_{\mathrm{np}}$


## Step 2: morph parallel images



- Image morphing
- use prewarped correspondences to compute a correspondence for all pixels in $\mathrm{I}_{0 \mathrm{p}}$
- linearly interpolate $\mathrm{I}_{0 \mathrm{p}}$ to intermediate positions
- useful observation
- corresponding pixels are on same line in prewarped views
- preventing holes
- use larger footprint (ex $2 \times 2$ )
- or linearly interpolate between consecutive samples
- or postprocess morphed image looking for background pixels and replacing them with neighboring values
- visibility artifacts
- collision of samples
- zbuffer on disparity
- holes
morph $I_{n p}$ to $I_{k p}$
use additional views


## Step 3: Postwarping



- create intermediate view
- $\mathrm{C}_{\mathrm{k}}$ is known
- current view direction is a linear interpolation of the start and end view directions
- current up vector is a linear interpolation of the start and end up vectors
- rotate morphed image to intermediate view
- same as prewarping



## Overview

- Introduction
- Depth extraction methods
- Reconstruction for IBRW
- Visibility without depth
- Sample selection


## Overview

- Introduction
- comparison to other IBR methods
-3 D warping equation
- reconstruction


## IBR by Warping (IBRW)

- Images enhanced with per-pixel depth [McMillan95]




## 3D warping equations

$$
\begin{aligned}
& u_{2}=\frac{w_{11}+w_{12} \cdot u_{1}+w_{13} \cdot v_{1}+w_{14} \cdot \delta\left(u_{1}, v_{1}\right)}{w_{31}+w_{32} \cdot u_{1}+w_{33} \cdot v_{1}+w_{34} \cdot \delta\left(u_{1}, v_{1}\right)} \\
& v_{2}=\frac{w_{21}+w_{22} \cdot u_{1}+w_{23} \cdot v_{1}+w_{24} \cdot \delta\left(u_{1}, v_{1}\right)}{w_{31}+w_{32} \cdot u_{1}+w_{33} \cdot v_{1}+w_{34} \cdot \delta\left(u_{1}, v_{1}\right)}
\end{aligned}
$$



## A complete IBR method

- Façade system
- (coarse) geometric model needed
- Panoramas
- viewer confined to center of panorama
- View morphing
- correspondences needed
- IBRW
- rendering to arbitrary new views


## DeltaSphere - depth\&color acquisition device



- Lars Nyland et al.





## Reconstructing by splatting

- Estimate shape and size of footprint of warped samples
- expensive to do accurately
- lower image quality if crudely approximated
- Samples are z-buffered


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- Depth from structured light
- Depth from focus / defocus
- Laser rangefinders


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## Depth from stereo

- two cameras with known parameters
- infer 3D location of point seen in both images
- sub problem: correspondences
- for a point seen in the left image, find its projection in the right image



## Depth from stereo: déjà-vu math

$$
\begin{aligned}
& \dot{P}=\dot{C}_{1}+\left(\bar{c}_{1}+u_{1} \bar{a}_{1}+v_{1} \bar{b}_{1}\right) w_{1} \\
& \dot{P}=\dot{C}_{2}+\left(\bar{c}_{2}+u_{2} \bar{a}_{2}+v_{2} \bar{b}_{2}\right) w_{2}
\end{aligned}
$$



- unknowns are $\mathrm{w}_{1}$ and $\mathrm{w}_{2}$
- overconstrained system
- the $\mathrm{u}_{2} \mathrm{v}_{2}$ coordinates of a point seen at $\mathrm{u}_{1} \mathrm{~V}_{1}$ are constrained to an epipolar line


## Epipolar line

- $\mathrm{C}_{1}, \mathrm{C}_{2}, \mathrm{P}_{1}$ define a plane
- $\mathrm{P}_{2}$ will be on that plane
- $\mathrm{P}_{2}$ is also on the image plane ${ }_{2}$
- So $\mathrm{P}_{2}$ will be on the line defined by the two planes' intersection



## Search for correspondences on epipolar line

- Reduces the dimensionality of the search space
- Walk on epipolar segment rather than search in entire image



## Parallel views

- Preferred stereo configuration
- epipolar lines are horizontal, easy to search



## Parallel views

- Limit search to epipolar segment
- from $\mathrm{u}_{2}=\mathrm{u}_{1}$ ( P is infinitely far away) to 0 ( P is close)



## Depth precision analysis

- $1 / \mathrm{z}$ linear with disparity $\left(\mathrm{u}_{1}-\mathrm{u}_{2}\right)$
- better depth resolution for nearby objects
- important to determine correspondences with subpixel accuracy



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## Depth from stereo problem

- Correspondences are difficult to find
- Structured light approach
- replace one camera with projector
- project easily detectable patterns
- establishing correspondences becomes a lot easier


## Depth from structured light

$$
\begin{aligned}
& \dot{P}=\dot{C}_{1}+\left(\bar{c}_{1}+u_{1} \bar{a}_{1}+v_{1} \bar{b}_{1}\right) w_{1} \\
& \dot{P}=\dot{C}_{2}+\left(\bar{c}_{2}+u_{2} \bar{a}_{2}+v_{2} \bar{b}_{2}\right) w_{2}
\end{aligned}
$$

- $\mathrm{C}_{1}$ is a projector
- Projects a pattern centered at $\mathrm{u}_{1} \mathrm{v}_{1}$

- Pattern center hits object scene at
- Camera $\mathrm{C}_{2}$ sees pattern at $\mathrm{u}_{2} \mathrm{v}_{2}$, easy to find
-3D location of P is determined



## Depth from structured light challenges

- Associated with using projectors
- expensive, cannot be used outdoors, not portable
- Difficult to identify pattern
- I found a corner, which corner is it?
- Invasive, change the color of the scene
- one could use invisible light, IR


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## Depth of field

- Thin lenses
- rays through lens center (C) do not change direction
- rays parallel to optical axis go



## Depth of field

- For a given focal length, only objects that are at a certain depth are in focus



## Out of focus

- When object at different depth
- One point projects to several
locations in the image
- Out of focus, blurred image



## Focusing

- Move lens to focus for new depth
- Relationship between focus and
depth can be exploited to extract depth



## Determine $z$ for points in focus

$$
\frac{a}{f}=\frac{h_{i}}{h}=\frac{a+f}{z}
$$



## Depth from defocus

- Take images of a scene with various camera parameters
- Measuring defocus variation, infer range to objects
- Does not need to find the best focusing planes for the various objects
- Examples by Shree Nayar, Columbia U


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## Laser range finders

- Send a laser beam to measure the distance - like RADAR, measures time of flight


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(5)

