

CS490D:  
Introduction to Data Mining  
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Multi-Relational Data Mining



## What is MRDM?

- Problem: Data in multiple tables
  - Want rules/patterns/etc. across tables
- Solution: Represent as single table
  - Join the data
  - Construct a single view
  - Use standard data mining techniques
- Example: “Customer” and “Married-to”
  - Easy single-table representation
- Bad Example: *Ancestor of*



## Basis of Solutions: Inductive Logic Programming

- ILP Rule:
  - $\text{customer}(\text{CID}, \text{Name}, \text{Age}, \text{yes}) \leftarrow$   
 $\text{Age} > 30 \wedge \text{purchase}(\text{CID}, \text{PID}, \text{D}, \text{Value}, \text{PM}) \wedge$   
 $\text{PM} = \text{credit card} \wedge \text{Value} > 100$
- Learning methods:
  - Database represented as clauses (rules)
  - Unification: Given rule (function/clause), discover values for which it holds



## Example

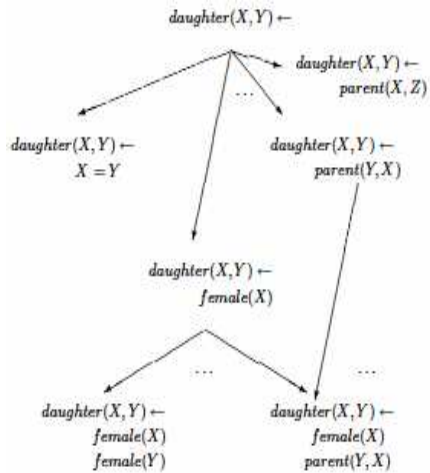
- How do we learn the “daughter” relationship?
  - Is this classification? Association?
- Covering Algorithm: “guess” at rule explaining only positive examples
  - Remove positive examples explained by rule
  - Iterate

Training examples	Background knowledge
$\text{daughter}(\text{mary}, \text{ann}). \oplus$	$\text{parent}(\text{ann}, \text{mary}). \text{female}(\text{ann}).$
$\text{daughter}(\text{eve}, \text{tom}). \oplus$	$\text{parent}(\text{ann}, \text{tom}). \text{female}(\text{mary}).$
$\text{daughter}(\text{tom}, \text{ann}). \ominus$	$\text{parent}(\text{tom}, \text{eve}). \text{female}(\text{eve}).$
$\text{daughter}(\text{eve}, \text{ann}). \ominus$	$\text{parent}(\text{tom}, \text{ian}).$



## How to make a good “guess”

- Clause subsumption:  
Generalize
  - More general clause  
(daughter(mary,Y)  
subsumes  
daughter(mary,ann)
- Start with general hypotheses and move to more specific



## Issues

- Search space – efficiency
- Noisy data
  - positive examples labeled as negative
  - Missing data (e.g., a daughter with no parents in the database)
- What else might we want to learn?



# WARMR: Multi-relational association rules

Algorithm WARMR( $r, \mathcal{L}, key, minfreq, Q$ )

Input: Database  $r$ ; Declarative language bias  $\mathcal{L}$  and  $key$ ;  
threshold  $minfreq$ ;

Output: All queries  $Q \in \mathcal{L}$  with frequency  $\geq minfreq$

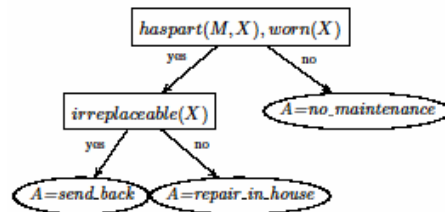
1. Initialize level  $d := 1$
2. Initialize the set of candidate queries  $Q_d := \{?-key\}$
3. Initialize the set of (in)frequent queries  $\mathcal{F} := \emptyset; \mathcal{I} := \emptyset$
4. While  $Q_d$  not empty
  5. Find frequency of all queries  $Q \in Q_d$
  6. Move those with frequency below  $minfreq$  to  $\mathcal{I}$
  7. Update  $\mathcal{F} := \mathcal{F} \cup Q_d$
  8. Compute new candidates:  
 $Q_{d+1} = \text{WARMRgen}(\mathcal{L}; \mathcal{I}; \mathcal{F}; Q_d)$
  9. Increment  $d$
10. Return  $\mathcal{F}$

Function WARMRgen( $\mathcal{L}; \mathcal{I}; \mathcal{F}; Q_d$ );

1. Initialize  $Q_{d+1} := \emptyset$
2. For each  $Q_j \in Q_d$ , and for each refinement  $Q'_j \in \mathcal{L}$  of  $Q_j$ :  
Add  $Q'_j$  to  $Q_{d+1}$ , unless:
  - (i)  $Q'_j$  is more specific than some query  $\in \mathcal{I}$ , or
  - (ii)  $Q'_j$  is equivalent to some query  $\in Q_{d+1} \cup \mathcal{F}$
3. Return  $Q_{d+1}$



# Multi-Relational Decision Trees



$\text{maintenance}(M, A) \leftarrow \text{haspart}(M, X), \text{worn}(X),$   
 $\text{irreplaceable}(X)!, A = \text{send\_back}$   
 $\text{maintenance}(M, A) \leftarrow \text{haspart}(M, X), \text{worn}(X), !,$   
 $A = \text{repair\_in\_house}$   
 $\text{maintenance}(M, A) \leftarrow A = \text{no\_maintenance}$

procedure DIVIDEANDCONQUER( $TestsOnYesBranchesSoFar, DeclarativeBias, Examples$ )

if TERMINATIONCONDITION( $Examples$ )

then

$NewLeaf = \text{CREATE\_NEW\_LEAF}(Examples)$

return  $NewLeaf$

else

$PossibleTestsNow = \text{GENERATE\_TESTS}(TestsOnYesBranchesSoFar, DeclarativeBias)$

$BestTest = \text{FIND\_BEST\_TEST}(PossibleTestsNow, Examples)$

$(Split_1, Split_2) = \text{SPLIT\_EXAMPLES}(Examples, TestsOnYesBranchesSoFar, BestTest)$

$LeftSubtree = \text{DIVIDEANDCONQUER}(TestsOnYesBranchesSoFar \wedge BestTest, Split_1)$

$RightSubtree = \text{DIVIDEANDCONQUER}(TestsOnYesBranchesSoFar, Split_2)$

return  $(BestTest, LeftSubtree, RightSubtree)$